

Maharashtra Board Solutions Class 12

Physics: Chapter 13- AC Circuits

Class 12 - Chapter 13 AC Circuits



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Maharashtra Board Solutions Class 12

Physics: Chapter 13- AC Circuits

Class 12: Physics Chapter 13 solutions. Complete Class 12 Physics Chapter 13 Notes.

Maharashtra Board Solutions Class 12 Physics: Chapter 13- AC Circuits

Maharashtra Board 12th Physics Chapter 13, Class 12 Physics Chapter 13 solutions

1. Choose the correct option.

i) If the RMS current in a 50 Hz AC circuit is 5A, the value of the current 1300 seconds after its value becomes zero is

(A) $52\sqrt{2}$ A

(B) $532\sqrt{2}$ A

(C) 56 A

(D) $52\sqrt{2}$ A

Answer:

(B) $532\sqrt{2}$ A

ii) A resistor of $500\ \Omega$ and an inductance of 0.5 H are in series with an AC source which is given by $V = 100\sqrt{2}\sin(1000t)$. The power factor of the combination

(A) $\frac{1}{2}$

(B) $\frac{1}{3}$

(C) 0.5

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(D) 0.6

Answer:

(A) $12\sqrt{}$

iii) In a circuit L, C & R are connected in series with an alternating voltage of frequency f. the current leads the voltage by 45° . The value of C is

(A) $\frac{1}{\pi f (2\pi fL - R)}$

(B) $\frac{1}{2\pi f (2\pi fL - R)}$

(C) $\frac{1}{\pi f (2\pi fL + R)}$

(D) $\frac{1}{2\pi f (2\pi fL + R)}$

Answer:

(B) $12\pi f(2\pi fL - R)$

iv) In an AC circuit, e and i are given by $e = 150 \sin (150t)$ V and $i = 150 \sin (150 t + \pi/3)$ A. the power dissipated in the circuit is

(A) 106W

(B) 150W

(C) 5625W

(D) Zero

Answer:

(C) 5625W

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v) In a series LCR circuit the phase difference between the voltage and the current is 45° . Then the power factor will be

(A) 0.607

(B) 0.707

(C) 0.808

(D) 1

Answer:

(B) 0.707

2. Answer in brief.

i) An electric lamp is connected in series with a capacitor and an AC source is glowing with a certain brightness. How does the brightness of the lamp change on increasing the capacitance ?

Answer:

Impedance, $Z = \sqrt{R^2 + \frac{1}{\omega^2 C^2}}$, where R is the resistance of the lamp, ω is the angular frequency of AC and C is the capacitance of the capacitor connected in series with the AC source and the lamp. When C is increased, Z decreases. Hence, Z increases.

Power factor, $\cos \Phi = \frac{R}{Z}$

As Z increases, the power factor decreases.

Now, the average power over one cycle,

$$P_{av} = V_{rms} I_{rms} \cos \Phi$$

$$= V_{rms} \left(\frac{V_{rms}}{Z} \right) \cos \Phi$$

$$= \frac{V^2}{Z} \cos \Phi$$

$\therefore P_{av}$ decreases as Z increases and $\cos \Phi$ decreases.

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As the current through the lamp ($V_{rms}Z$) decreases, the brightness of the lamp will decrease when C is increased.

ii) The total impedance of a circuit decreases when a capacitor is added in series with L and R . Explain why ?

Answer:

For an LR circuit, the impedance,

$Z_{LR} = \sqrt{R^2 + X_L^2}$, where X_L is the reactance of the inductor.

When a capacitor of capacitance C is added in series with L and R , the impedance,

$Z_{LCR} = \sqrt{R^2 + (X_L - X_C)^2}$ because in the case of an inductor the current lags behind the voltage by a phase angle of $\pi/2$ rad while in the case of a capacitor the current leads the voltage by a phase angle of $\pi/2$ rad. The decrease in net reactance decreases the total impedance ($Z_{LCR} < Z_{LR}$).

iii) For very high frequency AC supply, a capacitor behaves like a pure conductor. Why ?

Answer:

The reactance of a capacitor is $X_C = \frac{1}{2\pi fC}$, where f is the frequency of the AC supply and C is the capacitance of the capacitor. For very high frequency, f , X_C is very small. Hence, for very high frequency AC supply, a capacitor behaves like a pure conductor.

iv) What is wattless current ?

Answer:

The current that does not lead to energy consumption, hence zero power consumption, is called wattless current.

In the case of a purely inductive circuit or a purely capacitive circuit, average power consumed over a complete cycle is zero and hence the corresponding alternating current in the circuit is called wattless current.

[Note : In this case, the power factor is zero.]

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v) What is the natural frequency of L C circuit ? What is the reactance of this circuit at this frequency

Answer:

The natural frequency of LC circuit is $\frac{1}{2\pi\sqrt{LC}}$,

where L is the inductance and C is the capacitance. The reactance of this circuit at this frequency is

$$\begin{aligned}\frac{1}{2\pi fC} - \frac{1}{2\pi fL} &= \frac{1}{\frac{2\pi C}{2\pi\sqrt{LC}}} - \frac{1}{\frac{2\pi L}{2\pi\sqrt{LC}}} \\ &= \frac{1}{\sqrt{\frac{C}{L}} - \sqrt{\frac{C}{L}}} = \frac{1}{\text{zero}} = \infty.\end{aligned}$$

Question 3.

In a series LR circuit $X_L = R$ and power factor of the circuit is P_1 . When capacitor with capacitance C such that $X_L = X_C$ is put in series, the power factor becomes P_2 . Calculate P_1 / P_2 .

Answer:

For a series LR circuit, power factor,

$$\cos \phi = \frac{R}{\sqrt{R^2 + X_L^2}}$$

$$\text{If } X_L = R, \text{ power factor } P_1 = \frac{R}{\sqrt{2R^2}} = \frac{1}{\sqrt{2}}$$

For a series LCR circuit, power factor,

$$\cos \phi = \frac{R}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$\text{If } X_L = X_C, \text{ power factor } P_2 = \frac{R}{R} = 1.$$

$$\therefore \frac{P_1}{P_2} = \frac{1}{\sqrt{2}}.$$

Question 4.

When an AC source is connected to an ideal inductor show that the average power supplied by the source over a complete cycle is zero.

Answer:

In an AC circuit containing only an ideal inductor, the current i lags behind the emf e by a phase angle of $\pi/2$ rad. Here, for $e = e_0 \sin \omega t$, we have, $i = i_0 \sin(\omega t - \pi/2)$

Instantaneous power, $P = ei$

$$= (e_0 \sin \omega t) [i_0 (\sin \omega t \cos \pi/2 - \cos \omega t \sin \pi/2)]$$

$$= -e_0 i_0 \sin \omega t \cos \omega t \text{ as } \cos \pi/2 = 0 \text{ and } \sin \pi/2 = 1.$$

Average power over one cycle,

$$P_{av} = \frac{\text{work done in one cycle}}{\text{time for one cycle}}$$

$$= \frac{\int_0^T P dt}{T}$$

$$= \frac{\int_0^T [e_0 i_0 \cos \phi \sin^2 \omega t \pm e_0 i_0 \sin \phi \sin \omega t \cos \omega t] dt}{T}$$

$$= \frac{e_0 i_0}{T} \left[\cos \phi \int_0^T \sin^2 \omega t dt \pm \sin \phi \int_0^T \sin \omega t \cos \omega t dt \right]$$

$$\text{Now, } \int_0^T \sin^2 \omega t dt = \int_0^T \left(\frac{1 - \cos 2\omega t}{2} \right) dt$$

$$= \int_0^T \frac{1}{2} dt - \int_0^T \frac{\cos 2\omega t}{2} dt = \frac{T}{2} - \frac{1}{2} \left(\frac{\sin 2\omega t}{2\omega} \right)_0^T$$

$$\begin{aligned}
 &= \frac{T}{2} - \frac{1}{4\omega} (\sin 2\omega T - \sin 0) \\
 &= \frac{T}{2} - \frac{1}{4\omega} \left[\sin 2 \left(\frac{2\pi}{T} \right) T - 0 \right] \\
 &= \frac{T}{2} - \frac{1}{4\omega} [0 - 0] = \frac{T}{2}
 \end{aligned}$$

Also,

$$\begin{aligned}
 \int_0^T \sin \omega t \cos \omega t dt &= \frac{1}{2} \int_0^T \sin 2\omega t dt = \frac{1}{2} \left[\frac{-\cos 2\omega t}{2\omega} \right]_0^T \\
 &= -\frac{1}{4\omega} \left[\cos 2 \left(\frac{2\pi}{T} \right) T - \cos 0 \right] = -\frac{1}{4\omega} [1 - 1] = 0
 \end{aligned}$$

$$\text{Hence, } P_{av} = \frac{e_0 i_0}{T} \cos \phi \times \frac{T}{2} = \frac{e_0 i_0}{2} \cos \phi$$

$$= \frac{e_0}{\sqrt{2}} \cdot \frac{i_0}{\sqrt{2}} \cos \phi$$

$$= e_{rms} i_{rms} \cos \phi = e_{rms} i_{rms} (RZ), \text{ where the impedance } Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$\therefore P_{av} = 0$, i.e., the circuit does not dissipate power.

Question 5.

Prove that an ideal capacitor in an AC circuit does not dissipate power

Answer:

In an AC circuit containing only an ideal inductor, the current i lags behind the emf e by a phase angle of $\pi/2$ rad. Here, for $e = e_0 \sin \omega t$, we have, $i = i_0 \sin(\omega t - \pi/2)$

Instantaneous power, $P = ei$

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$$= (e_0 \sin \omega t) [i_0 (\sin \omega t \cos \pi/2 + \cos \omega t \sin \pi/2)]$$

$$= -e_0 i_0 \sin \omega t \cos \omega t \text{ as } \cos \pi/2 = 0 \text{ and } \sin \pi/2 = 1.$$

Average power over one cycle, P_{av}

$$P_{av} = \frac{\text{work done in one cycle}}{\text{time for one cycle}}$$

$$= \frac{\int_0^T P dt}{T}$$

$$= \frac{\int_0^T [e_0 i_0 \cos \phi \sin^2 \omega t \pm e_0 i_0 \sin \phi \sin \omega t \cos \omega t] dt}{T}$$

$$= \frac{e_0 i_0}{T} \left[\cos \phi \int_0^T \sin^2 \omega t dt \pm \sin \phi \int_0^T \sin \omega t \cos \omega t dt \right]$$

$$\text{Now, } \int_0^T \sin^2 \omega t dt = \int_0^T \left(\frac{1 - \cos 2\omega t}{2} \right) dt$$

$$= \int_0^T \frac{1}{2} dt - \int_0^T \frac{\cos 2\omega t}{2} dt = \frac{T}{2} - \frac{1}{2} \left(\frac{\sin 2\omega t}{2\omega} \right)_0^T$$

$$\begin{aligned}
 &= \frac{T}{2} - \frac{1}{4\omega} (\sin 2\omega T - \sin 0) \\
 &= \frac{T}{2} - \frac{1}{4\omega} \left[\sin 2 \left(\frac{2\pi}{T} \right) T - 0 \right] \\
 &= \frac{T}{2} - \frac{1}{4\omega} [0 - 0] = \frac{T}{2}
 \end{aligned}$$

Also,

$$\begin{aligned}
 \int_0^T \sin \omega t \cos \omega t dt &= \frac{1}{2} \int_0^T \sin 2\omega t dt = \frac{1}{2} \left[\frac{-\cos 2\omega t}{2\omega} \right]_0^T \\
 &= -\frac{1}{4\omega} \left[\cos 2 \left(\frac{2\pi}{T} \right) T - \cos 0 \right] = -\frac{1}{4\omega} [1 - 1] = 0
 \end{aligned}$$

$$\text{Hence, } P_{av} = \frac{e_0 i_0}{T} \cos \phi \times \frac{T}{2} = \frac{e_0 i_0}{2} \cos \phi$$

$$= \frac{e_0}{\sqrt{2}} \cdot \frac{i_0}{\sqrt{2}} \cos \phi$$

$$= e_{rms} i_{rms} \cos \phi = e_{rms} i_{rms} (RZ), \text{ where the impedance } Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$\therefore P_{av} = 0$, i.e., the circuit does not dissipate power.

Question 6.

(a) An emf $e = e_0 \sin \omega t$ applied to a series $L - C - R$ circuit derives a current $I = I_0 \sin \omega t$ in the circuit. Deduce the expression for the average power dissipated in the circuit.

(b) For circuits used for transporting electric power, a low power factor implies large power loss in transmission. Explain.

Answer:

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(a) Instantaneous power,

$$P = ei$$

$$= (e_0 \sin \omega t) [i_0 (\sin \omega t \pm \Phi)]$$

$$= e_0 i_0 \sin \omega t (\sin \omega t \cos \Phi \pm \cos \omega t \sin \Phi)$$

$$= e_0 i_0 \sin^2 \omega t \pm e_0 i_0 \sin \Phi \sin \omega t \cos \omega t$$

Average power over one cycle,

$$P_{av} = \frac{\text{work done in one cycle}}{\text{time for one cycle}}$$

$$= \frac{\int_0^T P dt}{T}$$

$$= \frac{\int_0^T [e_0 i_0 \cos \phi \sin^2 \omega t \pm e_0 i_0 \sin \phi \sin \omega t \cos \omega t] dt}{T}$$

$$= \frac{e_0 i_0}{T} \left[\cos \phi \int_0^T \sin^2 \omega t dt \pm \sin \phi \int_0^T \sin \omega t \cos \omega t dt \right]$$

$$\text{Now, } \int_0^T \sin^2 \omega t dt = \int_0^T \left(\frac{1 - \cos 2\omega t}{2} \right) dt$$

$$= \int_0^T \frac{1}{2} dt - \int_0^T \frac{\cos 2\omega t}{2} dt = \frac{T}{2} - \frac{1}{2} \left(\frac{\sin 2\omega t}{2\omega} \right)_0^T$$

$$\begin{aligned}
 &= \frac{T}{2} - \frac{1}{4\omega} (\sin 2\omega T - \sin 0) \\
 &= \frac{T}{2} - \frac{1}{4\omega} \left[\sin 2 \left(\frac{2\pi}{T} \right) T - 0 \right] \\
 &= \frac{T}{2} - \frac{1}{4\omega} [0 - 0] = \frac{T}{2}
 \end{aligned}$$

Also,

$$\begin{aligned}
 \int_0^T \sin \omega t \cos \omega t dt &= \frac{1}{2} \int_0^T \sin 2\omega t dt = \frac{1}{2} \left[\frac{-\cos 2\omega t}{2\omega} \right]_0^T \\
 &= -\frac{1}{4\omega} \left[\cos 2 \left(\frac{2\pi}{T} \right) T - \cos 0 \right] = -\frac{1}{4\omega} [1 - 1] = 0
 \end{aligned}$$

$$\text{Hence, } P_{av} = \frac{e_0 i_0}{T} \cos \phi \times \frac{T}{2} = \frac{e_0 i_0}{2} \cos \phi$$

$$= \frac{e_0}{\sqrt{2}} \cdot \frac{i_0}{\sqrt{2}} \cos \phi$$

$$= e_{rms} i_{rms} \cos \phi = e_{rms} i_{rms} (RZ), \text{ where the impedance } Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$(b) P_{av} = e_{rms} i_{rms} \cos \phi$$

The factor $\cos \phi$ is called as power factor. For circuits used for transporting electric power, a low power factor means the power available on transportation is much less than $e_{rms} i_{rms}$. It means there is significant loss of power during transportation.

Question 7.

A device Y is connected across an AC source of emf $e = e_0 \sin \omega t$. The current through Y is given as $i = i_0 \sin(\omega t + \pi/2)$

a) Identify the device Y and write the expression for its reactance.

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b) Draw graphs showing variation of emf and current with time over one cycle of AC for Y.

c) How does the reactance of the device Y vary with the frequency of the AC ? Show graphically

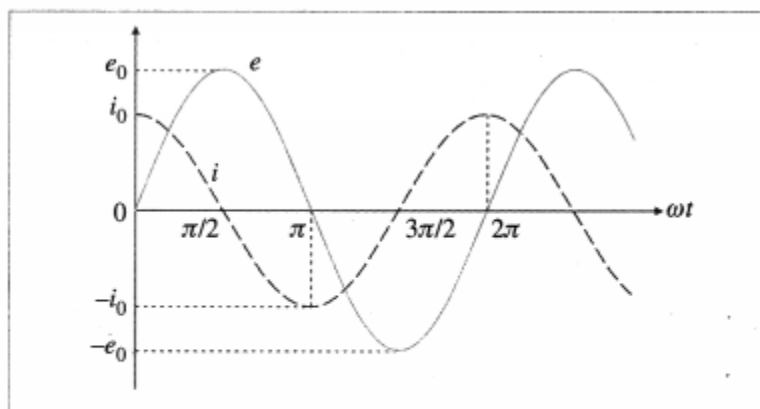
d) Draw the phasor diagram for the device Y.

Answer:

(a) The device Y is a capacitor. Its reactance is $X_C = 1/\omega C$,

where ω is the angular frequency of the applied emf and C is the capacitance of the capacitor.

(b)



Graphs of e and i versus ωt for a purely capacitive AC circuit ■

(c) $X_C = 1/\omega C = 1/(2\pi f C)$. Thus $X_C \propto 1/f$, where f is the frequency of AC. Suppose $C = (1000/2\pi)$ pF

For $f = 100$ Hz, $X_C = 1 \times 10^7 \Omega = 10 \text{ M}\Omega$;

for $f = 200$ Hz, $X_C = 5 \text{ M}\Omega$;

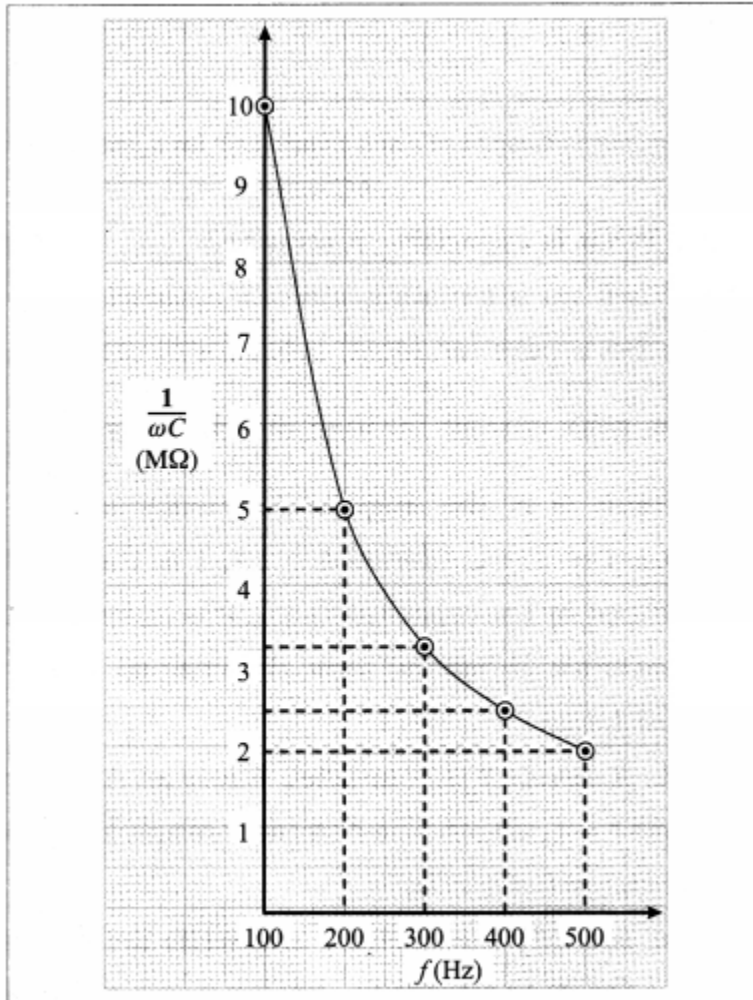
for $f = 300$ Hz, $X_C = 103 \text{ M}\Omega$;

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for $f = 400 \text{ Hz}$, $X_C = 2.5 \text{ M}\Omega$

for $f = 500 \text{ Hz}$, $X_C = 2 \text{ M}\Omega$ and so on

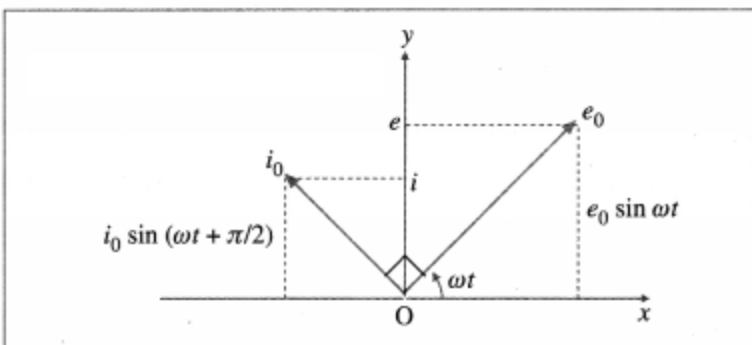
($1 \text{ M}\Omega = 10^6 \Omega$).



Variation of $\frac{1}{\omega C}$ with f .

(d)

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Phasor diagram for a purely capacitive circuit

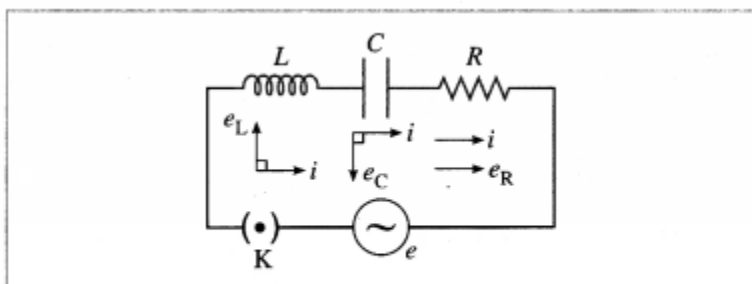
The phasor representing the peak emf (e_0) makes an angle (ωt) in an anticlockwise direction with respect to the horizontal axis. As the current leads the voltage by 90° , the phasor representing the peak current (i_0) is turned 90° anticlockwise with respect to the phasor representing emf e_0 . The projections of these phasors on the vertical axis give instantaneous values of e and i .

Question 8.

Derive an expression for the impedance of an LCR circuit connected to an AC power supply.

Answer:

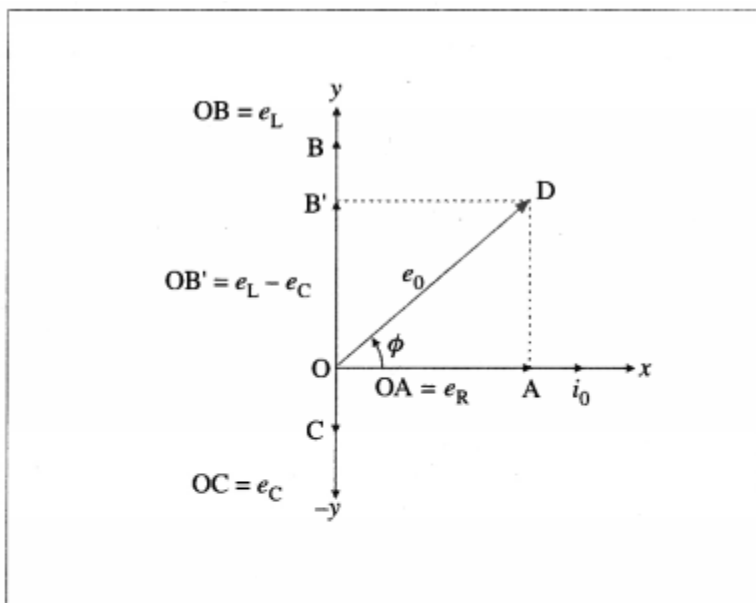
Figure shows an inductor of inductance L , capacitor of capacitance C , resistor of resistance R , key K and source (power supply) of alternating emf (e) connected to form a closed series circuit.



LCR Series circuit

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We assume the inductor, capacitor and resistor to be ideal. As these are connected in series, at any instant, they carry the same current $i = i_0 \sin \omega t$. The voltage across the resistor, $e_R = Ri$, is in phase with the current. The voltage across the inductor, $e_L = X_L i$, leads the current by $\pi/2$ rad and that across the capacitor, $e_C = X_C i$, lags behind the current by $\pi/2$ rad. This is shown in the phasor diagram.



Phasor diagram for an LCR series circuit

$$\begin{aligned} \text{From this figure, } e_0^2 &= e_R^2 + (e_L - e_C)^2 \\ &= R^2 i_0^2 + (X_L i_0 - X_C i_0)^2 = i_0^2 [R^2 + (X_L - X_C)^2] \\ \therefore e_0 &= i_0 \sqrt{R^2 + (X_L - X_C)^2} = i_0 Z, \text{ where} \\ Z &= \frac{e_0}{i_0} = \sqrt{R^2 + (X_L - X_C)^2} \end{aligned}$$

is the effective resistance of the circuit. It is called the impedance.

Question 9.

Compare resistance and reactance.

Answer:

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(1) Resistance is opposition to flow of charges (current) and appears in a DC circuit as well as in an AC circuit.

The term reactance appears only in an AC circuit. It occurs when an inductor and/or a capacitor is used.

(2) In a purely resistive circuit, current and voltage are always in phase.

When reactance is not zero, there is nonzero phase difference between current and voltage.

(3) Resistance does not depend on the frequency of AC.

Reactance depends on the frequency of AC. In case of an inductor, reactance increases linearly with frequency. In case of a capacitor, reactance decreases as frequency of AC increases; it is inversely proportional to frequency.

(4) Resistance gives rise to production of Joule heat in a component.

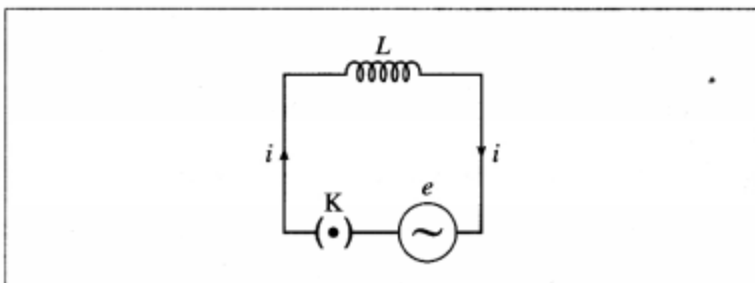
In a circuit with pure reactance, there is no production of heat.

Question 10.

Show that in an AC circuit containing a pure inductor, the voltage is ahead of current by $\pi/2$ in phase.

Answer:

Figure 13.8 shows an AC source, generating a voltage $e = e_0 \sin \omega t$, connected to a key K and a pure inductor of inductance L to form a closed circuit.



An AC source connected to an inductor

On closing the key K, an emf is induced in the inductor as the magnetic flux linked with it changes with time. This emf opposes the applied emf and according to the laws of electromagnetic induction by Faraday and Lenz, we have,

$$e' = -L \frac{di}{dt} \dots\dots\dots (1)$$

where e' is the induced emf and i is the current through the inductor. To maintain the current; e and e' must be equal in magnitude and opposite in direction.

According to Kirchhoff's voltage law, as the resistance of the inductor is assumed to be zero, we

$$\text{have, } e = -e' = L \frac{di}{dt} \dots\dots\dots (2)$$

$$\therefore \frac{di}{dt} = \frac{e}{L} = \frac{e_0 \sin \omega t}{L}$$

$$\therefore \int di = \int \frac{e_0 \sin \omega t}{L} dt$$

$$\therefore i = -\frac{e_0}{\omega L} \cos \omega t + C$$

where C is the constant of integration. C must be time independent and have the dimension of current. As e oscillates about zero, i also oscillates about zero and hence there cannot be any time independent component of current.

$$\therefore C = 0. \therefore i = -e_0 \omega L \cos \omega t = -e_0 \omega L \sin(\pi/2 - \omega t)$$

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$$\therefore i = e_0 \omega L \sin(\omega t - \pi/2) \dots\dots\dots (3)$$

as $\sin(-\theta) = -\sin \theta$

From Eq. (3), $i_{\text{peak}} = i_0 = e_0 \omega L$

$$\therefore i = i_0 \sin(\omega t - \pi/2) \dots\dots\dots (4)$$

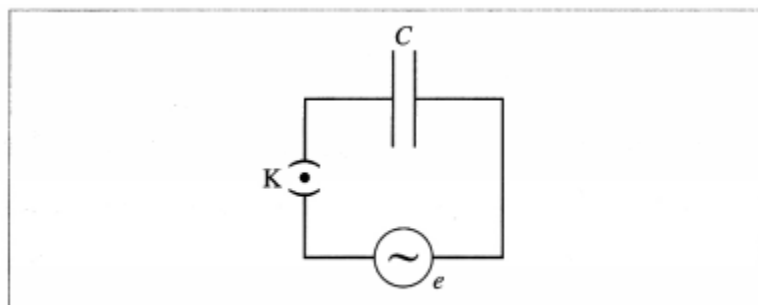
Comparison of this equation with $e = e_0 \sin \omega t$ shows that e leads i by $\pi/2$ rad, i.e., the voltage is ahead of current by $\pi/2$ rad in phase.

Question 11.

An AC source generating a voltage $e = e_0 \sin \omega t$ is connected to a capacitor of capacitance C . Find the expression for the current i flowing through it. Plot a graph of e and i versus ωt .

Answer:

Figure 13.12 shows an AC source, generating a voltage $e = e_0 \sin \omega t$, connected to a capacitor of capacitance C . The plates of the capacitor get charged due to the applied voltage. As the alternating voltage is reversed in each half cycle, the



An AC source connected to a capacitor

capacitor is alternately charged and discharged. If q is the charge on the capacitor, the corresponding potential difference across the plates of the capacitor is $V = q/C$. $\therefore q = CV$. q and V are functions of time, with $V = e = e_0 \sin \omega t$. The instantaneous current in the circuit is $i = dq/dt = d(CV)/dt = C dv/dt = C d(e_0 \sin \omega t)/dt = \omega C e_0 \cos \omega t$

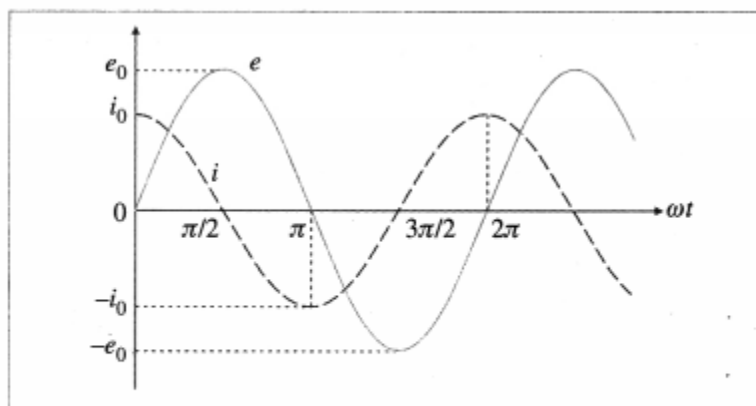
$$\therefore i = e_0 (1/\omega C) \sin(\omega t + \pi/2) = i_0 \sin(\omega t + \pi/2)$$

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where $i_0 = e_0(1/\omega C)$ is the peak value of the current.

ωt (rad)	$\omega t + \pi/2$ (rad)	$e = e_0 \sin \omega t$	$i = i_0 \sin \left(\omega t + \frac{\pi}{2} \right)$
0	$\frac{\pi}{2}$	0	i_0
$\frac{\pi}{2}$	π	e_0	0
π	$\frac{3\pi}{2}$	0	$-i_0$
$\frac{3\pi}{2}$	2π	$-e_0$	0
2π	$2\pi + \frac{\pi}{2}$	0	i_0

Table gives the values of e and i for different values of ωt and Fig shows graphs of e and i versus ωt . i leads e by phase angle of $\pi/2$ rad.



Graphs of e and i versus ωt for a purely capacitive
AC circuit

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Question 12.

If the effective current in a 50 cycle AC circuit is 5 A, what is the peak value of current? What is the current 1/600 sec. after it was zero ?

Answer:

Data : $f = 50$ Hz, $i_{\text{rms}} = 5$ A, $t = 1600$ s

The peak value of the current,

$$i_0 = i_{\text{rms}} \sqrt{2} = (5)(1.414) = 7.07 \text{ A}$$

$$= i_0 \sin (2\pi ft)$$

$$= 7.07 \sin [2\pi(50)(1600)]$$

$$= 7.07 \sin (\pi/6) = (7.07)(0.5)$$

$$= 3.535 \text{ A}$$

This is the required current.

Question 13.

A light bulb is rated 100W for 220 V AC supply of 50 Hz. Calculate (a) resistance of the bulb. (b) the rms current through the bulb.

Answer:

Data: Power ($V_{\text{rms}} i_{\text{rms}}$) = 100 W, $V_{\text{rms}} = 220$ V,

$f = 50$ Hz

The rms current through the bulb,

$$i_{\text{rms}} = \frac{\text{power}}{V_{\text{rms}}} = \frac{100}{220} = 0.4545 \text{ A}$$

The resistance of the bulb,

$$R = \frac{V_{\text{rms}}}{i_{\text{rms}}} = \frac{220}{(100/220)} = (22)(22) = 484 \Omega$$

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Question 14.

A 15.0 μF capacitor is connected to a 220 V, 50 Hz source. Find the capacitive reactance and the current (rms and peak)

in the circuit. If the frequency is doubled, what will happen to the capacitive reactance and the current.

Answer:

Data : $C = 15 \mu\text{F} = 15 \times 10^{-6} \text{ F}$, $V_{\text{rms}} = 220\text{V}$, $f = 50 \text{ Hz}$,

The capacitive reactance = $12\pi fC$

$$= \frac{1}{2(3.142)(50)(15 \times 10^{-6})} = \frac{100 \times 100}{(3.142)(15)}$$
$$= 212.2 \Omega$$

$$i_{\text{rms}} = \frac{V_{\text{rms}}}{\text{capacitive reactance}} = \frac{220}{212.2}$$
$$= 1.037 \text{ A}$$

$$i_{\text{peak}} = i_{\text{rms}} \sqrt{2} = (1.037)(1.414) = 1.466 \text{ A}$$

If the frequency is doubled, the capacitive reactance will be halved and the current will be doubled.

Question 15.

An AC circuit consists of only an inductor of inductance 2 H. If the current is represented by a sine wave of amplitude 0.25 A and frequency 60 Hz, calculate the effective potential difference across the inductor ($\pi = 3.142$)

Answer:

Data : $L = 2\text{H}$, $i_0 = 0.25 \text{ A}$, $f = 60 \text{ Hz}$, $\pi = 3.142$

$$\omega L = 2\pi fL = 2(3.142)(60)(2) = 754.1 \Omega$$

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The effective potential difference across the inductor = $\omega L i_{\text{rms}} = \omega L i_0 2\sqrt{}$
 $= (754.1)(0.25)1.414 = 133.3 \text{ V}$

Question 16.

Alternating emf of $e = 220 \sin 100 \pi t$ is applied to a circuit containing an inductance of $(1/\pi)$ henry. Write an equation for instantaneous current through the circuit. What will be the reading of the AC galvanometer connected in the circuit?

Answer:

Data: $e = 220 \sin 100 \pi t$, $L = (1/\pi) \text{ H}$

Comparing $e = 220 \sin 100 \pi t$ with

$e = e_0 \sin \omega t$, we get

$\omega = 100 \pi \therefore \omega L = (100 \pi) (1/\pi) = 100 \Omega$

$\therefore$ The instantaneous current through the circuit

$= i = e_0 \omega L \sin(100 \pi t - \pi/2)$

$= 220 \cdot 100 \sin(100 \pi t - \pi/2) = 2.2 \sin(100 \pi t - \pi/2)$ in ampere [assuming that e is in volt.]

$i_{\text{rms}} = i_0 2\sqrt{}/2 = 2.21.414 = 1.556 \text{ A}$ is the reading of the AC galvanometer connected in the circuit.

Question 17.

A $25 \mu\text{F}$ capacitor, a 0.10 H inductor and a 25Ω resistor are connected in series with an AC source whose emf is given by $e = 310 \sin 314 t$ (volt). What is the frequency, reactance, impedance, current and phase angle of the circuit?

Answer:

Data: $C = 25 \mu\text{F} = 25 \times 10^{-6} \text{ F}$, $L = 0.10 \text{ H}$, $R = 25 \Omega$,

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$$e = 310 \sin (314 t) \text{ [volt]}$$

Comparing $e = 310 \sin (314 t)$ with

$$e = e_0 \sin (2\pi ft), \text{ we get,}$$

the frequency of the alternating emf as

$$f = \frac{314}{2\pi} = \frac{314}{2(3.14)} = 50 \text{ Hz}$$

$$\begin{aligned} \text{Reactance} &= \left| \omega L - \frac{1}{\omega C} \right| = \left| 2\pi fL - \frac{1}{2\pi fC} \right| \\ &= \left| 2(3.14)(50)(0.10) - \frac{1}{2(3.14)(50)(25 \times 10^{-6})} \right| \\ &= \left| 31.4 - \frac{100 \times 10^2}{(3.14)(25)} \right| = |31.4 - 127.4| \\ &= 96 \Omega \end{aligned}$$

$$Z^2 = R^2 + \left(\omega L - \frac{1}{\omega C} \right)^2 = (25)^2 + (96)^2 = 9841 \Omega^2$$

$$\therefore \text{ Impedance, } Z = \sqrt{9841} \Omega = 99.2 \Omega$$

$$\text{Peak current, } i_0 = \frac{e_0}{Z} = \frac{310}{99.2} \text{ A}$$

$$\therefore i_{\text{rms}} = \frac{i_0}{\sqrt{2}} = \frac{310}{(1.414)(99.2)} \text{ A} = 2.21 \text{ A}$$

$$\cos \Phi = R/Z = 25/99.2 = 0.2520$$

$$\therefore \text{ The phase angle, } \Phi = \cos^{-1}(0.2520) = 75.40^\circ = 1.316 \text{ rad}$$

Question 18.

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A capacitor of 100 μF , a coil of resistance 50 Ω and an inductance 0.5 H are connected in series with a 110 V-50Hz source. Calculate the rms value of current in the circuit.

Answer:

Data : $C = 100 \mu\text{F} = 100 \times 10^{-6} \text{ F} = 10^{-4} \text{ F}$,

$R = 50 \Omega$, $L = 0.5\text{H}$, $f = 50 \text{ Hz}$, $V_{\text{rms}} = 110 \text{ V}$

$\therefore \omega L = 2\pi fL = 2 (3.142)(50)(0.5) = 157.1 \Omega$

$$\text{and } \frac{1}{\omega C} = \frac{1}{2\pi fC} = \frac{1}{2 (3.142)(50)(10^{-4})}$$

$$= \frac{100}{3.142} = 31.83 \Omega$$

$$Z^2 = R^2 + \left(\omega L - \frac{1}{\omega C} \right)^2 = (50)^2 + (157.1 - 31.83)^2$$

$$2500 + 15700 = 18200 \Omega^2$$

$\therefore$ Impedance, $Z = 18200 \text{-----} \sqrt{\Omega} = 134.9 \Omega$

The rms value of the current in the circuit,

$$i_{\text{rms}} = \frac{V_{\text{rms}}}{Z} = \frac{110}{134.9} \text{ A}$$

$$= 0.8154 \text{ A}$$

Question 19.

Find the capacity of a capacitor which when put in series with a 10 Ω resistor makes the power factor equal to 0.5. Assume an 80V-100Hz AC supply.

Answer:

Data : $R = 10 \Omega$, power factor = 0.5, $f = 100 \text{ Hz}$

$$\text{Power factor} = \frac{R}{Z} = \cos \phi = \frac{R}{\sqrt{R^2 + X_C^2}}$$

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$$\therefore 0.5 = 12(3.142)(100)C(10)$$

$$\therefore C = 13.142 \times 10^3$$

$$= 10 \times 10^{-4} 3.142$$

$$= 3.182 \times 10^{-4} \text{ F}$$

This is the capacity of the capacitor.

Question 20.

Find the time required for a 50 Hz alternating current to change its value from zero to the rms value.

Answer:

$$\text{Data : } f = 50 \text{ Hz, } i = i_0 2\sqrt{2} \therefore i_0 = 12\sqrt{2}$$

$$i = i_0 \sin \omega t$$

$$\therefore \sin \omega t = i_0 = 12\sqrt{2}$$

$$\therefore \omega t = \pi/4 \text{ rad}$$

$$\therefore 2\pi f t = \pi/4$$

$$\therefore t = 1/8f = 1/8(50) = 1400$$

$$= 1000 \times 10^{-3} 1400 = 2.5 \times 10^{-3} \text{ s}$$

This is the required time.

Question 21.

Calculate the value of capacitance in picofarad, which will make 101.4 micro henry inductance to oscillate with frequency of one megahertz.

Answer:

$$\text{Data : } f_r = 10^6 \text{ Hz, } L = 101.4 \times 10^{-6} \text{ H}$$

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$$f_r = \frac{1}{2\pi\sqrt{LC}} \quad \therefore f_r^2 = \frac{1}{4\pi^2 LC}$$
$$\therefore C = \frac{1}{4\pi^2 f_r^2 L} = \frac{1}{4(3.142)^2 (10^6)^2 (101.4 \times 10^{-6})}$$

$$= 10000 \times 10^{-104} (3.142)^2 (101.4) = 2.497 \times 10^{-10} \text{ F}$$

$$= 249.7 \times 10^{-12} \text{ F} = 249.7 \text{ picofarad}$$

This is the value of the capacity.

Question 22.

A 10 μF capacitor is charged to a 25 volt of potential. The battery is disconnected and a pure 100 m H coil is connected across the capacitor so that LC oscillations are set up. Calculate the maximum current in the coil.

Answer:

$$\text{Data: } C = 10 \mu\text{F} = 10 \times 10^{-6} \text{ F} = 10^{-5} \text{ F},$$

$$L = 100 \text{ mH} = 100 \times 10^{-3} \text{ H} = 10^{-1} \text{ H}, V = 25 \text{ V}$$

For reference, see the solved example (8) above.

$$12CV^2 = 12Li^2$$

$$\therefore i^2 = \frac{CLV^2}{L} = 10^{-5} 10^{-1} (25)^2$$

$$\therefore i = 25 \times 10^{-2} \text{ A} = 0.25 \text{ A}$$

This is the maximum current in the coil.

Question 23.

A 100 μF capacitor is charged with a 50 V source supply. Then source supply is removed and the capacitor is connected across an inductance, as a result of

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which 5A current flows through the inductance. Calculate the value of the inductance.

Answer:

Data: $C = 100 \mu\text{F} = 100 \times 10^{-6} \text{ F} = 10^{-4} \text{ F}$,

$V = 50\text{V}$, $i = 5\text{A}$

The energy stored in the electric field in the capacitor

$$= \frac{1}{2} CV^2$$

The energy stored in the magnetic field in the inductor = $\frac{1}{2} Li^2$

Here, $\frac{1}{2} CV^2 = \frac{1}{2} Li^2$

$$\therefore L = \frac{CV^2}{i^2}$$

$$\therefore L = \frac{C(V)^2}{(i)^2} = \frac{10^{-4} (50)^2}{(5)^2}$$

$$= 10^{-2} \text{H}$$

This is the value of the inductance.



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- Chapter 6- Superposition of Waves
- Chapter 7- Wave Optics
- Chapter 8- Electrostatics
- Chapter 9- Current Electricity
- Chapter 10- Magnetic Fields due to Electric Current
- Chapter 11- Magnetic Materials
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