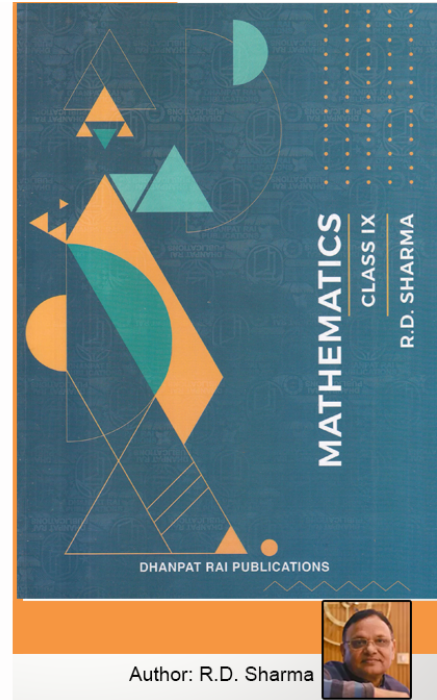


# Class 9 - Chapter 8 Lines and Angles



## RD Sharma Solutions for Class 9 Maths Chapter 8–Lines and Angles

Class 9: Maths Chapter 8 solutions. Complete Class 9 Maths Chapter 8 Notes.

### RD Sharma Solutions for Class 9 Maths Chapter 8–Lines and Angles

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**Exercise 8.1**

**Question 1: Write the complement of each of the following angles:**

(i)  $20^\circ$

(ii)  $35^\circ$

(iii)  $90^\circ$

(iv)  $77^\circ$

(v)  $30^\circ$

**Solution:**

(i) The sum of an angle and its complement =  $90^\circ$

Therefore, the complement of  $20^\circ = 90^\circ - 20^\circ = 70^\circ$

(ii) The sum of an angle and its complement =  $90^\circ$

Therefore, the complement of  $35^\circ = 90^\circ - 35^\circ = 55^\circ$

(iii) The sum of an angle and its complement =  $90^\circ$

Therefore, the complement of  $90^\circ = 90^\circ - 90^\circ = 0^\circ$

(iv) The sum of an angle and its complement =  $90^\circ$

Therefore, the complement of  $77^\circ = 90^\circ - 77^\circ = 13^\circ$

(v) The sum of an angle and its complement =  $90^\circ$

Therefore, the complement of  $30^\circ = 90^\circ - 30^\circ = 60^\circ$

**Question 2 : Write the supplement of each of the following angles:**

(i)  $54^\circ$

(ii)  $132^\circ$

(iii)  $138^\circ$

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**Solution:**

(i) The sum of an angle and its supplement =  $180^\circ$ .

Therefore supplement of angle  $54^\circ = 180^\circ - 54^\circ = 126^\circ$

(ii) The sum of an angle and its supplement =  $180^\circ$ .

Therefore supplement of angle  $132^\circ = 180^\circ - 132^\circ = 48^\circ$

(iii) The sum of an angle and its supplement =  $180^\circ$ .

Therefore supplement of angle  $138^\circ = 180^\circ - 138^\circ = 42^\circ$

**Question 3: If an angle is  $28^\circ$  less than its complement, find its measure?**

**Solution:**

Let the measure of any angle is ' a ' degrees

Thus, its complement will be  $(90 - a)^\circ$

So, the required angle = Complement of a – 28

$$a = (90 - a) - 28$$

$$2a = 62$$

$$a = 31$$

Hence, the angle measured is  $31^\circ$ .

**Question 4 : If an angle is  $30^\circ$  more than one half of its complement, find the measure of the angle?**

**Solution:**

Let an angle measured by ' a ' in degrees

Thus, its complement will be  $(90 - a)^\circ$

Required Angle =  $30^\circ + \text{complement}/2$

$$a = 30^\circ + (90 - a)^\circ / 2$$

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$$a + a/2 = 30^\circ + 45^\circ$$

$$3a/2 = 75^\circ$$

$$a = 50^\circ$$

Therefore, the measure of required angle is  $50^\circ$ .

**Question 5 : Two supplementary angles are in the ratio 4:5. Find the angles?**

**Solution:**

Two supplementary angles are in the ratio 4:5.

Let us say, the angles are  $4a$  and  $5a$  (in degrees)

Since angles are supplementary angles;

$$\text{Which implies, } 4a + 5a = 180^\circ$$

$$9a = 180^\circ$$

$$a = 20^\circ$$

Therefore,  $4a = 4(20) = 80^\circ$  and

$$5(a) = 5(20) = 100^\circ$$

Hence, required angles are  $80^\circ$  and  $100^\circ$ .

**Question 6 : Two supplementary angles differ by  $48^\circ$ . Find the angles?**

**Solution:** Given: Two supplementary angles differ by  $48^\circ$ .

Consider  $a^\circ$  be one angle then its supplementary angle will be equal to  $(180 - a)^\circ$

According to the question;

$$(180 - a) - a = 48$$

$$(180 - 48) = 2a$$

$$132 = 2a$$

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$$132/2 = a$$

$$\text{Or } a = 66^\circ$$

$$\text{Therefore, } 180 - a = 114^\circ$$

Hence, the two angles are  $66^\circ$  and  $114^\circ$ .

**Question 7: An angle is equal to 8 times its complement. Determine its measure?**

**Solution:** Given: Required angle = 8 times of its complement

Consider  $a^\circ$  be one angle then its complementary angle will be equal to  $(90 - a)^\circ$

According to the question;

$a = 8$  times of its complement

$$a = 8 ( 90 - a )$$

$$a = 720 - 8a$$

$$a + 8a = 720$$

$$9a = 720$$

$$a = 80$$

Therefore, the required angle is  $80^\circ$ .

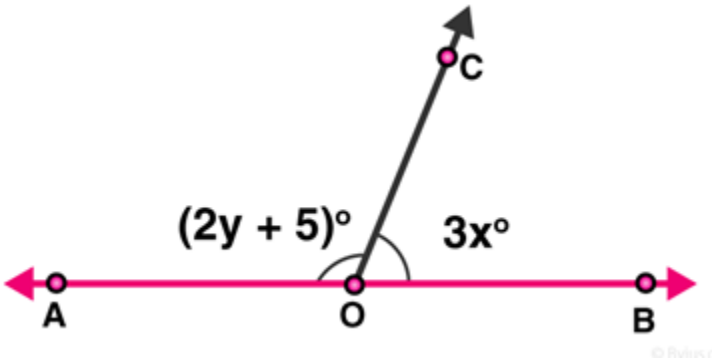
### **Exercise 8.2**

**Question 1: In the below Fig. OA and OB are opposite rays:**

(i) If  $x = 25^\circ$ , what is the value of  $y$ ?

(ii) If  $y = 35^\circ$ , what is the value of  $x$ ?

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**Solution:**

(i) Given:  $x = 25$

From figure:  $\angle AOC$  and  $\angle BOC$  form a linear pair

Which implies,  $\angle AOC + \angle BOC = 180^\circ$

From the figure,  $\angle AOC = 2y + 5$  and  $\angle BOC = 3x$

$$\angle AOC + \angle BOC = 180^\circ$$

$$(2y + 5) + 3x = 180$$

$$(2y + 5) + 3(25) = 180$$

$$2y + 5 + 75 = 180$$

$$2y + 80 = 180$$

$$2y = 100$$

$$y = 100/2 = 50$$

Therefore,  $y = 50^\circ$

(ii) Given:  $y = 35^\circ$

From figure:  $\angle AOC + \angle BOC = 180^\circ$  (Linear pair angles)

$$(2y + 5) + 3x = 180$$

$$(2(35) + 5) + 3x = 180$$

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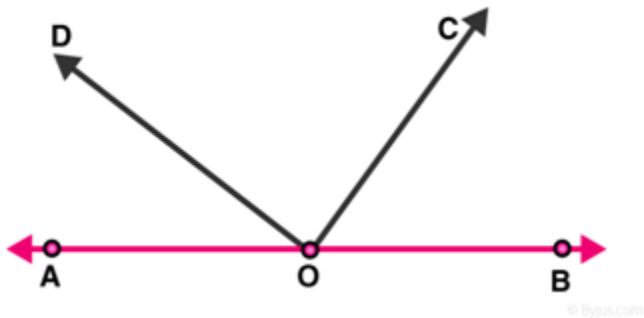
$$75 + 3x = 180$$

$$3x = 105$$

$$x = 35$$

Therefore,  $x = 35^\circ$

**Question 2:** In the below figure, write all pairs of adjacent angles and all the linear pairs.

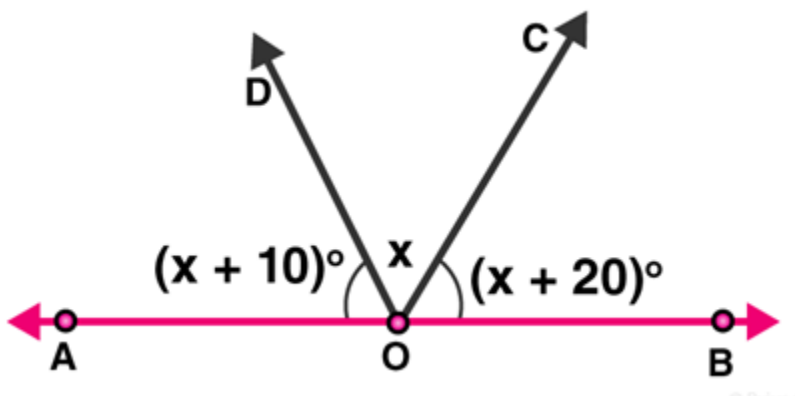


**Solution:** From figure, pairs of adjacent angles are :

$(\angle AOC, \angle COB)$ ;  $(\angle AOD, \angle BOD)$ ;  $(\angle AOD, \angle COD)$ ;  $(\angle BOC, \angle COD)$

And Linear pair of angles are  $(\angle AOD, \angle BOD)$  and  $(\angle AOC, \angle BOC)$ . [As  $\angle AOD + \angle BOD = 180^\circ$  and  $\angle AOC + \angle BOC = 180^\circ$ .]

**Question 3 :** In the given figure, find  $x$ . Further find  $\angle BOC$ ,  $\angle COD$  and  $\angle AOD$ .



**Solution:**

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From figure,  $\angle AOD$  and  $\angle BOD$  form a linear pair,

Therefore,  $\angle AOD + \angle BOD = 180^\circ$

Also,  $\angle AOD + \angle BOC + \angle COD = 180^\circ$

Given:  $\angle AOD = (x+10)^\circ$ ,  $\angle COD = x^\circ$  and  $\angle BOC = (x + 20)^\circ$

$$(x + 10) + x + (x + 20) = 180$$

$$3x + 30 = 180$$

$$3x = 180 - 30$$

$$x = 150/3$$

$$x = 50^\circ$$

Now,

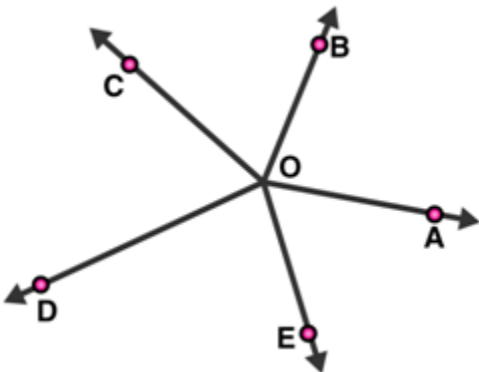
$$\angle AOD = (x+10) = 50 + 10 = 60$$

$$\angle COD = x = 50$$

$$\angle BOC = (x+20) = 50 + 20 = 70$$

Hence,  $\angle AOD = 60^\circ$ ,  $\angle COD = 50^\circ$  and  $\angle BOC = 70^\circ$

**Question 4:** In figure, rays OA, OB, OC, OD and OE have the common end point O. Show that  $\angle AOB + \angle BOC + \angle COD + \angle DOE + \angle EOA = 360^\circ$ .



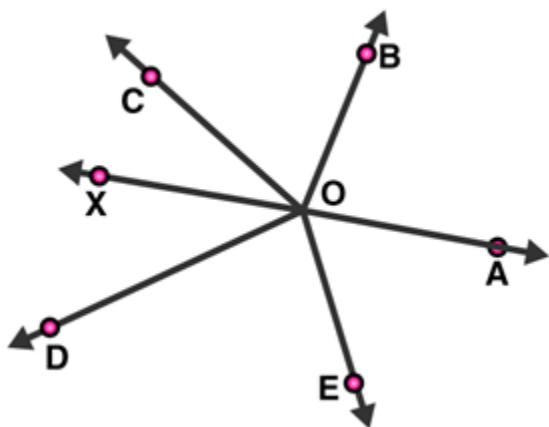
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**Solution:**

Given: Rays OA, OB, OC, OD and OE have the common endpoint O.

Draw an opposite ray OX to ray OA, which make a straight line AX.



From figure:

$\angle AOB$  and  $\angle BOX$  are linear pair angles, therefore,

$$\angle AOB + \angle BOX = 180^\circ$$

$$\text{Or, } \angle AOB + \angle BOC + \angle COX = 180^\circ \text{ ——(1)}$$

Also,

$\angle AOE$  and  $\angle EOX$  are linear pair angles, therefore,

$$\angle AOE + \angle EOX = 180^\circ$$

$$\text{Or, } \angle AOE + \angle DOE + \angle DOX = 180^\circ \text{ ——(2)}$$

By adding equations, (1) and (2), we get;

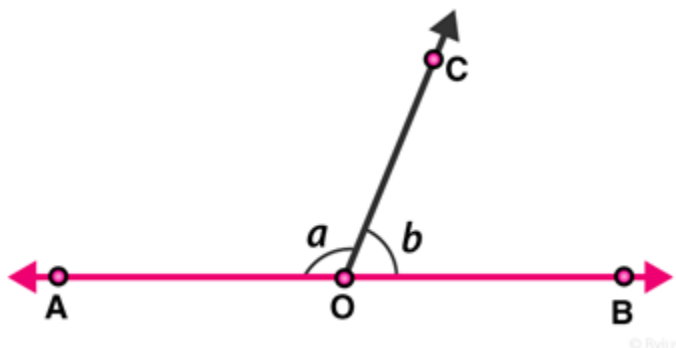
$$\angle AOB + \angle BOC + \angle COX + \angle AOE + \angle DOE + \angle DOX = 180^\circ + 180^\circ$$

$$\angle AOB + \angle BOC + \angle COD + \angle DOE + \angle EOA = 360^\circ$$

Hence Proved.

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**Question 5 :** In figure,  $\angle AOC$  and  $\angle BOC$  form a linear pair. If  $a - 2b = 30^\circ$ , find  $a$  and  $b$ ?



**Solution:**

Given :  $\angle AOC$  and  $\angle BOC$  form a linear pair.

$$\Rightarrow a + b = 180^\circ \dots(1)$$

$$a - 2b = 30^\circ \dots(2) \text{ (given)}$$

On subtracting equation (2) from (1), we get

$$a + b - a + 2b = 180 - 30$$

$$3b = 150$$

$$b = 150/3$$

$$b = 50^\circ$$

Since,  $a - 2b = 30^\circ$

$$a - 2(50) = 30$$

$$a = 30 + 100$$

$$a = 130^\circ$$

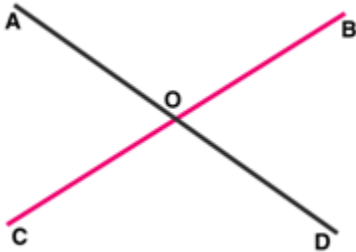
Therefore, the values of  $a$  and  $b$  are  $130^\circ$  and  $50^\circ$  respectively.

**Question 6:** How many pairs of adjacent angles are formed when two lines intersect at a point?

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**Solution:** Four pairs of adjacent angles are formed when two lines intersect each other at a single point.

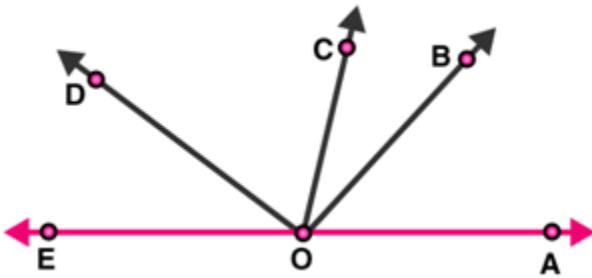
For example, Let two lines AB and CD intersect at point O.



The 4 pair of adjacent angles are :

( $\angle AOD, \angle DOB$ ), ( $\angle DOB, \angle BOC$ ), ( $\angle COA, \angle AOD$ ) and ( $\angle BOC, \angle COA$ ).

**Question 7:** How many pairs of adjacent angles, in all, can you name in figure given?



**Solution:** Number of Pairs of adjacent angles, from the figure, are :

$\angle EOC$  and  $\angle DOC$

$\angle EOD$  and  $\angle DOB$

$\angle DOC$  and  $\angle COB$

$\angle EOD$  and  $\angle DOA$

$\angle DOC$  and  $\angle COA$

$\angle BOC$  and  $\angle BOA$

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$\angle BOA$  and  $\angle BOD$

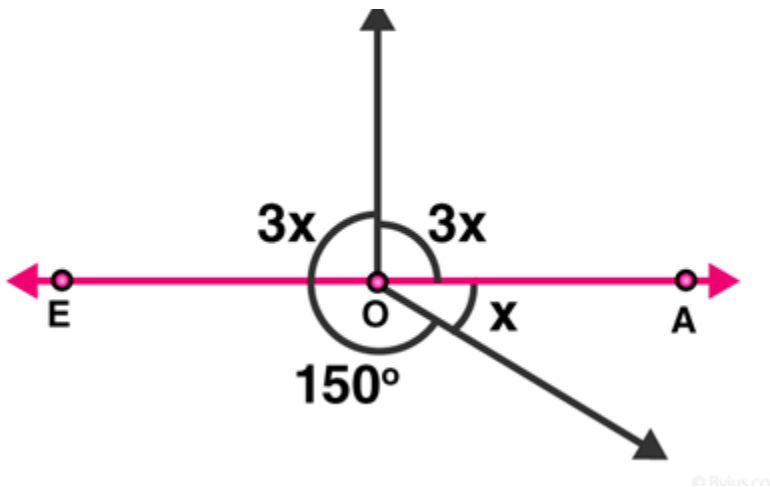
$\angle BOA$  and  $\angle BOE$

$\angle EOC$  and  $\angle COA$

$\angle EOC$  and  $\angle COB$

Hence, there are 10 pairs of adjacent angles.

**Question 8:** In figure, determine the value of  $x$ .



**Solution:**

The sum of all the angles around a point O is equal to  $360^\circ$ .

Therefore,

$$3x + 3x + 150 + x = 360^\circ$$

$$7x = 360^\circ - 150^\circ$$

$$7x = 210^\circ$$

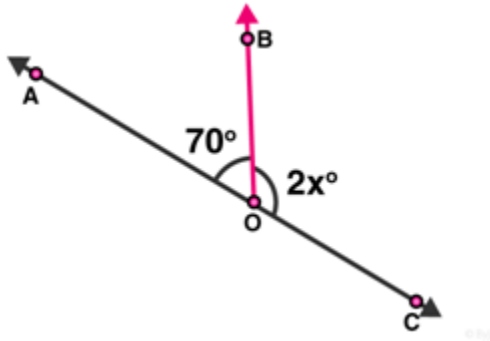
$$x = 210/7$$

$$x = 30^\circ$$

Hence, the value of  $x$  is  $30^\circ$ .

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**Question 9:** In figure, AOC is a line, find x.



**Solution:**

From the figure,  $\angle AOB$  and  $\angle BOC$  are linear pairs,

$$\angle AOB + \angle BOC = 180^\circ$$

$$70 + 2x = 180$$

$$2x = 180 - 70$$

$$2x = 110$$

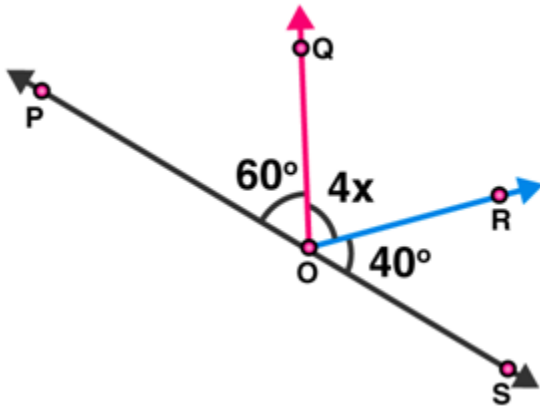
$$x = 110/2$$

$$x = 55$$

Therefore, the value of x is  $55^\circ$ .

**Question 10:** In figure, POS is a line, find x.

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**Solution:**

From figure,  $\angle POQ$  and  $\angle QOS$  are linear pairs.

Therefore,

$$\angle POQ + \angle QOS = 180^\circ$$

$$\angle POQ + \angle QOR + \angle ROS = 180^\circ$$

$$60^\circ + 4x + 40^\circ = 180^\circ$$

$$4x = 180^\circ - 100^\circ$$

$$4x = 80^\circ$$

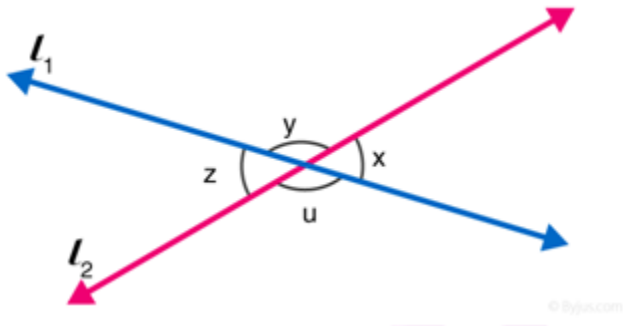
$$x = 20^\circ$$

Hence, the value of  $x$  is  $20^\circ$ .

**Exercise 8.3**

**Question 1:** In figure, lines  $l_1$  and  $l_2$  intersect at  $O$ , forming angles as shown in the figure. If  $x = 45$ . Find the values of  $y$ ,  $z$  and  $u$ .

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**Solution:**

Given:  $x = 45^\circ$

Since vertically opposite angles are equal, therefore  $z = x = 45^\circ$

$z$  and  $u$  are angles that are a linear pair, therefore,  $z + u = 180^\circ$

Solve,  $z + u = 180^\circ$ , for  $u$

$$u = 180^\circ - z$$

$$u = 180^\circ - 45$$

$$u = 135^\circ$$

Again,  $x$  and  $y$  angles are a linear pair.

$$x + y = 180^\circ$$

$$y = 180^\circ - x$$

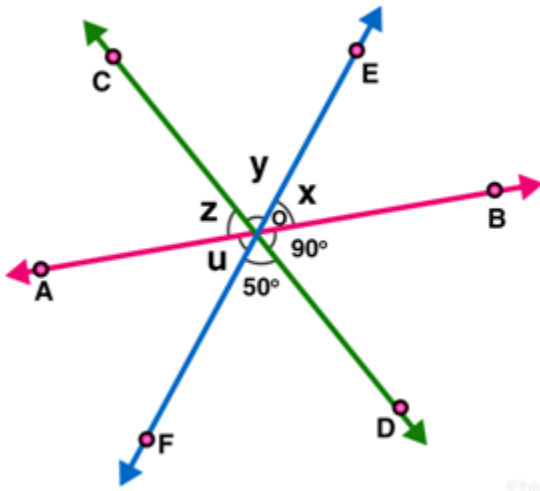
$$y = 180^\circ - 45^\circ$$

$$y = 135^\circ$$

Hence, remaining angles are  $y = 135^\circ$ ,  $u = 135^\circ$  and  $z = 45^\circ$ .

**Question 2 :** In figure, three coplanar lines intersect at a point O, forming angles as shown in the figure. Find the values of  $x$ ,  $y$ ,  $z$  and  $u$ .

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**Solution:**

( $\angle BOD, z$ ); ( $\angle DOF, y$ ) are pair of vertically opposite angles.

So,  $\angle BOD = z = 90^\circ$

$\angle DOF = y = 50^\circ$  [Vertically opposite angles are equal.]

Now,  $x + y + z = 180$  [Linear pair] [AB is a straight line]

$$x + y + z = 180$$

$$x + 50 + 90 = 180$$

$$x = 180 - 140$$

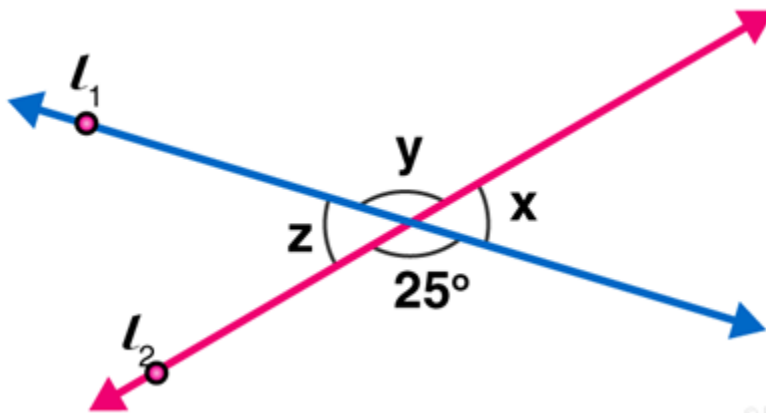
$$x = 40$$

Hence values of  $x, y, z$  and  $u$  are  $40^\circ, 50^\circ, 90^\circ$  and  $40^\circ$  respectively.

**Question 3 :** In figure, find the values of  $x, y$  and  $z$ .

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**Solution:**

From figure,

$$y = 25^\circ \text{ [Vertically opposite angles are equal]}$$

$$\text{Now } \angle x + \angle y = 180^\circ \text{ [Linear pair of angles]}$$

$$x = 180 - 25$$

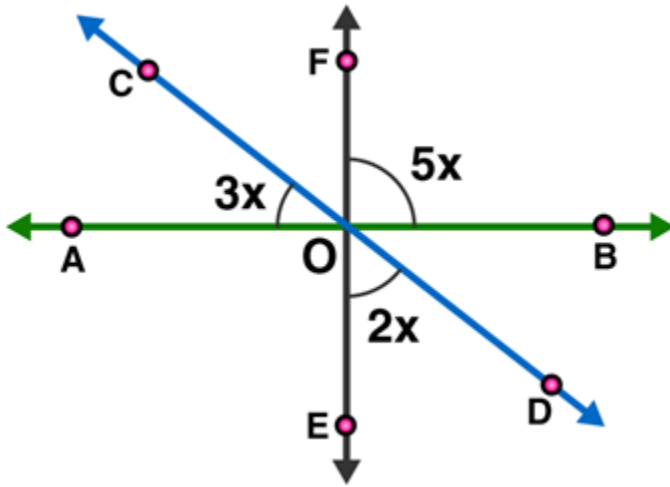
$$x = 155$$

$$\text{Also, } z = x = 155 \text{ [Vertically opposite angles]}$$

$$\text{Answer: } y = 25^\circ \text{ and } z = 155^\circ$$

**Question 4 : In figure, find the value of x.**

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**Solution:**

$\angle AOE = \angle BOF = 5x$  [Vertically opposite angles]

$\angle COA + \angle AOE + \angle EOD = 180^\circ$  [Linear pair]

$$3x + 5x + 2x = 180$$

$$10x = 180$$

$$x = 180/10$$

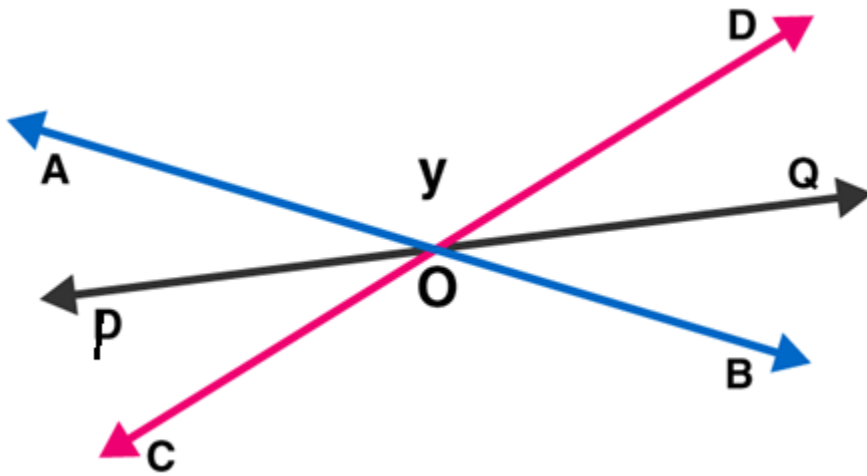
$$x = 18$$

The value of  $x = 18^\circ$

**Question 5 : Prove that bisectors of a pair of vertically opposite angles are in the same straight line.**

**Solution:**

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Lines AB and CD intersect at point O, such that

$$\angle AOC = \angle BOD \text{ (vertically angles) } \dots(1)$$

Also OP is the bisector of AOC and OQ is the bisector of BOD

To Prove: POQ is a straight line.

OP is the bisector of  $\angle AOC$ :

$$\angle AOP = \angle COP \dots(2)$$

OQ is the bisector of  $\angle BOD$ :

$$\angle BOQ = \angle QOD \dots(3)$$

Now,

Sum of the angles around a point is  $360^\circ$ .

$$\angle AOC + \angle BOD + \angle AOP + \angle COP + \angle BOQ + \angle QOD = 360^\circ$$

$$\angle BOQ + \angle QOD + \angle DOA + \angle AOP + \angle POC + \angle COB = 360^\circ$$

$$2\angle QOD + 2\angle DOA + 2\angle AOP = 360^\circ \text{ (Using (1), (2) and (3))}$$

$$\angle QOD + \angle DOA + \angle AOP = 180^\circ$$

$$\angle POQ = 180^\circ$$

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Which shows that, the bisectors of pair of vertically opposite angles are on the same straight line.

Hence Proved.

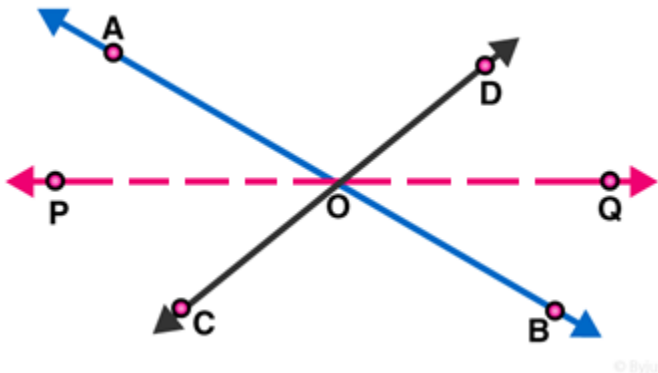
**Question 6 :** If two straight lines intersect each other, prove that the ray opposite to the bisector of one of the angles thus formed bisects the vertically opposite angle.

**Solution:** Given AB and CD are straight lines which intersect at O.

OP is the bisector of  $\angle AOC$ .

To Prove : OQ is the bisector of  $\angle BOD$

Proof :



AB, CD and PQ are straight lines which intersect in O.

Vertically opposite angles:  $\angle AOP = \angle BOQ$

Vertically opposite angles:  $\angle COP = \angle DOQ$

OP is the bisector of  $\angle AOC$  :  $\angle AOP = \angle COP$

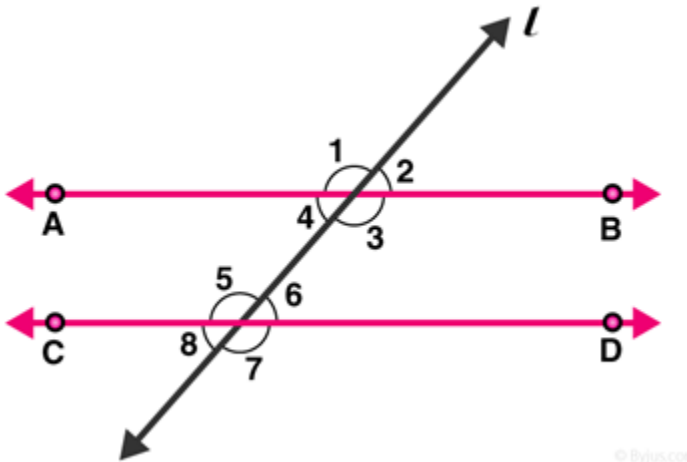
Therefore,  $\angle BOQ = \angle DOQ$

Hence, OQ is the bisector of  $\angle BOD$ .

#### **Exercise 8.4**

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**Question 1:** In figure, AB, CD and  $\angle 1$  and  $\angle 2$  are in the ratio 3 : 2. Determine all angles from 1 to 8.



**Solution:**

Let  $\angle 1 = 3x$  and  $\angle 2 = 2x$

From figure:  $\angle 1$  and  $\angle 2$  are linear pair of angles

Therefore,  $\angle 1 + \angle 2 = 180$

$$3x + 2x = 180$$

$$5x = 180$$

$$x = 180 / 5$$

$$\Rightarrow x = 36$$

So,  $\angle 1 = 3x = 108^\circ$  and  $\angle 2 = 2x = 72^\circ$

As we know, vertically opposite angles are equal.

Pairs of vertically opposite angles are:

$(\angle 1 = \angle 3)$ ;  $(\angle 2 = \angle 4)$  ;  $(\angle 5, \angle 7)$  and  $(\angle 6 , \angle 8)$

$$\angle 1 = \angle 3 = 108^\circ$$

$$\angle 2 = \angle 4 = 72^\circ$$

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$$\angle 5 = \angle 7$$

$$\angle 6 = \angle 8$$

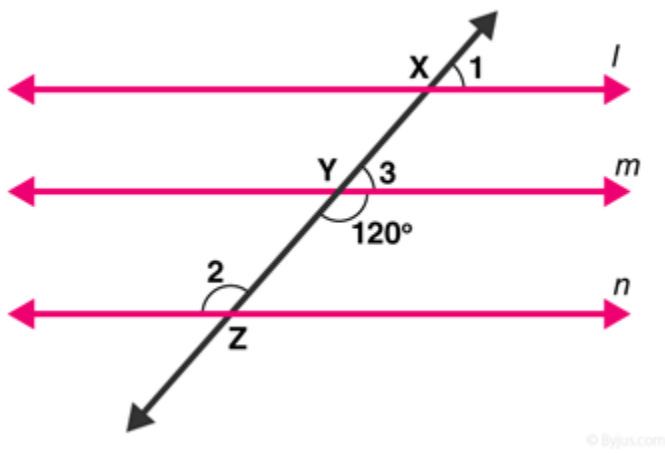
We also know, if a transversal intersects any parallel lines, then the corresponding angles are equal

$$\angle 1 = \angle 5 = \angle 7 = 108^\circ$$

$$\angle 2 = \angle 6 = \angle 8 = 72^\circ$$

Answer:  $\angle 1 = 108^\circ$ ,  $\angle 2 = 72^\circ$ ,  $\angle 3 = 108^\circ$ ,  $\angle 4 = 72^\circ$ ,  $\angle 5 = 108^\circ$ ,  $\angle 6 = 72^\circ$ ,  $\angle 7 = 108^\circ$  and  $\angle 8 = 72^\circ$

**Question 2:** In figure,  $l$ ,  $m$  and  $n$  are parallel lines intersected by transversal  $p$  at  $X$ ,  $Y$  and  $Z$  respectively. Find  $\angle 1$ ,  $\angle 2$  and  $\angle 3$ .



**Solution:** From figure:

$$\angle Y = 120^\circ \text{ [Vertical opposite angles]}$$

$$\angle 3 + \angle Y = 180^\circ \text{ [Linear pair angles theorem]}$$

$$\Rightarrow \angle 3 = 180 - 120$$

$$\Rightarrow \angle 3 = 60^\circ$$

Line  $l$  is parallel to line  $m$ ,

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$\angle 1 = \angle 3$  [Corresponding angles]

$\angle 1 = 60^\circ$

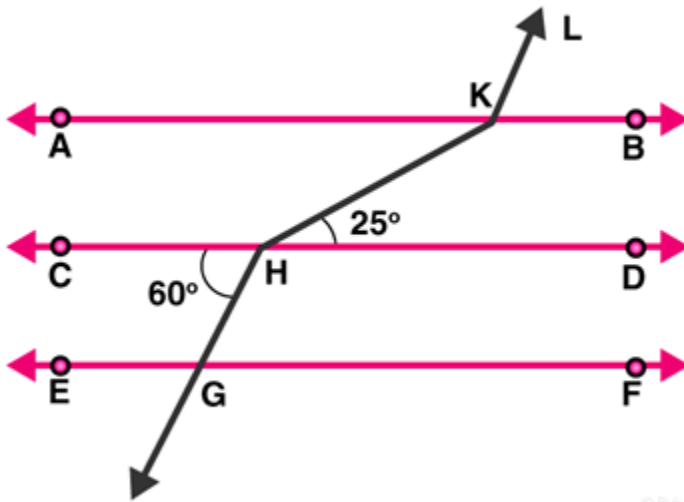
Also, line  $m$  is parallel to line  $n$ ,

$\angle 2 = \angle Y$  [Alternate interior angles are equal]

$\angle 2 = 120^\circ$

Answer:  $\angle 1 = 60^\circ$ ,  $\angle 2 = 120^\circ$  and  $\angle 3 = 60^\circ$ .

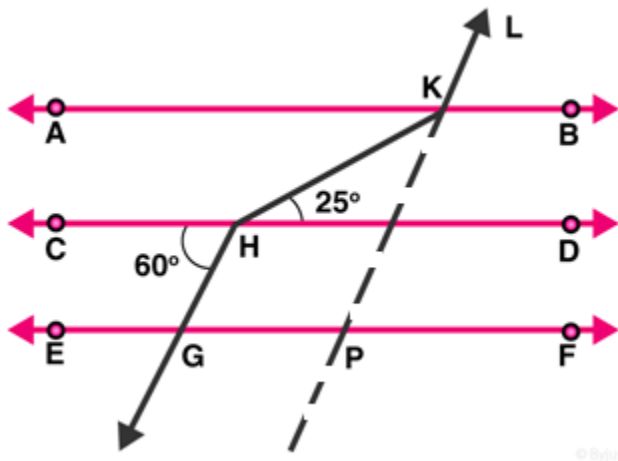
**Question 3:** In figure,  $AB \parallel CD \parallel EF$  and  $GH \parallel KL$ . Find  $\angle HKL$ .



**Solution:**

Extend  $LK$  to meet line  $GF$  at point  $P$ .

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From figure,  $CD \parallel GF$ , so, alternate angles are equal.

$$\angle CHG = \angle HGP = 60^\circ$$

$$\angle HGP = \angle KPF = 60^\circ \text{ [Corresponding angles of parallel lines are equal]}$$

$$\text{Hence, } \angle KPG = 180 - 60 = 120^\circ$$

$$\Rightarrow \angle GPK = \angle AKL = 120^\circ \text{ [Corresponding angles of parallel lines are equal]}$$

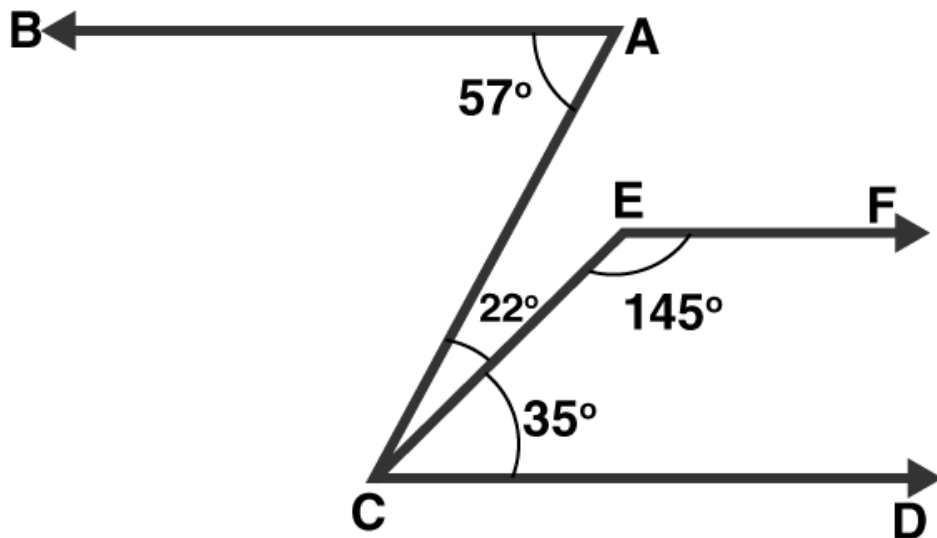
$$\angle AKH = \angle KHD = 25^\circ \text{ [alternate angles of parallel lines]}$$

$$\text{Therefore, } \angle HKL = \angle AKH + \angle AKL = 25 + 120 = 145^\circ$$

**Question 4: In figure, show that  $AB \parallel EF$ .**

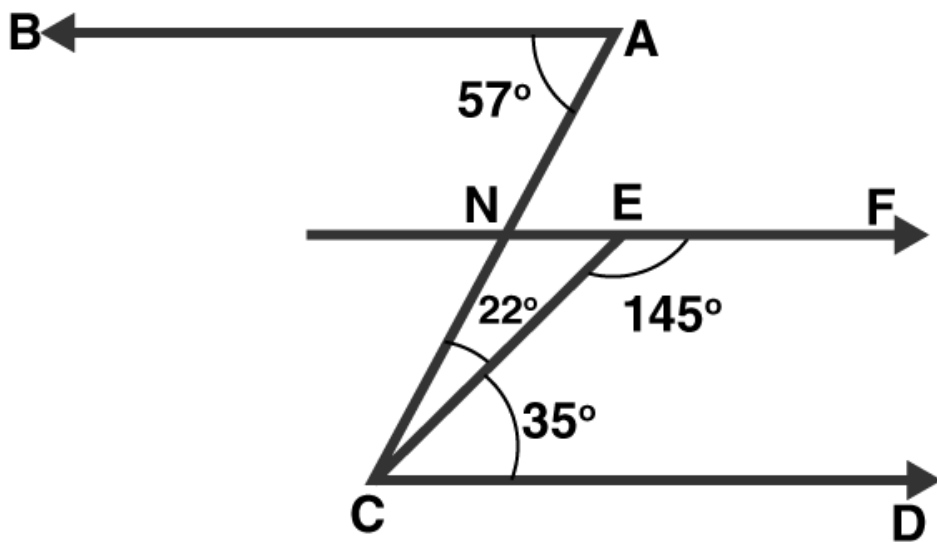
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**Solution:** Produce  $EF$  to intersect  $AC$  at point  $N$ .



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From figure,  $\angle BAC = 57^\circ$  and

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$$\angle ACD = 22^\circ + 35^\circ = 57^\circ$$

Alternative angles of parallel lines are equal

$$\Rightarrow BA \parallel EF \dots(1)$$

Sum of Co-interior angles of parallel lines is  $180^\circ$

$$EF \parallel CD$$

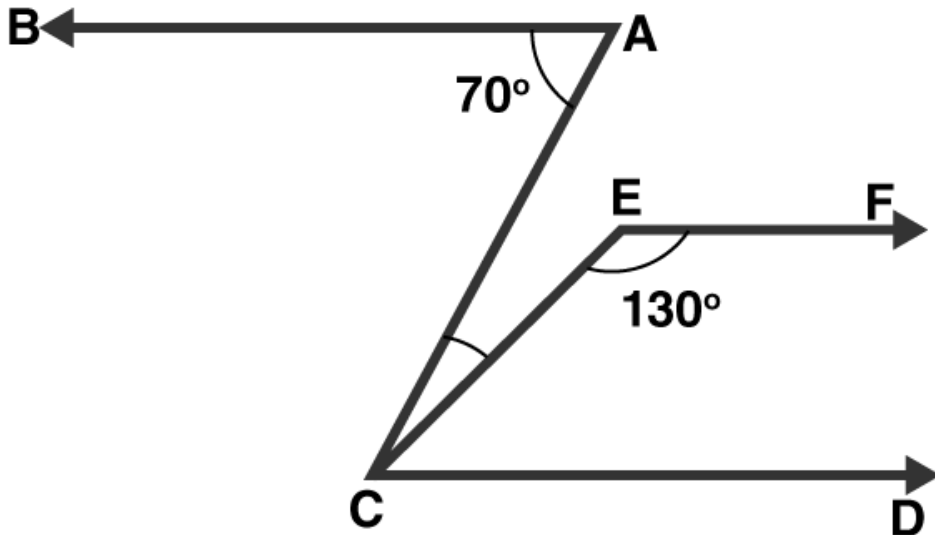
$$\angle DCE + \angle CEF = 35 + 145 = 180^\circ \dots(2)$$

From (1) and (2)

$AB \parallel EF$  [Since, Lines parallel to the same line are parallel to each other]

Hence Proved.

**Question 5 :** In figure, if  $AB \parallel CD$  and  $CD \parallel EF$ , find  $\angle ACE$ .



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**Solution:**

Given:  $CD \parallel EF$

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$\angle FEC + \angle ECD = 180^\circ$  [Sum of co-interior angles is supplementary to each other]

$$\Rightarrow \angle ECD = 180^\circ - 130^\circ = 50^\circ$$

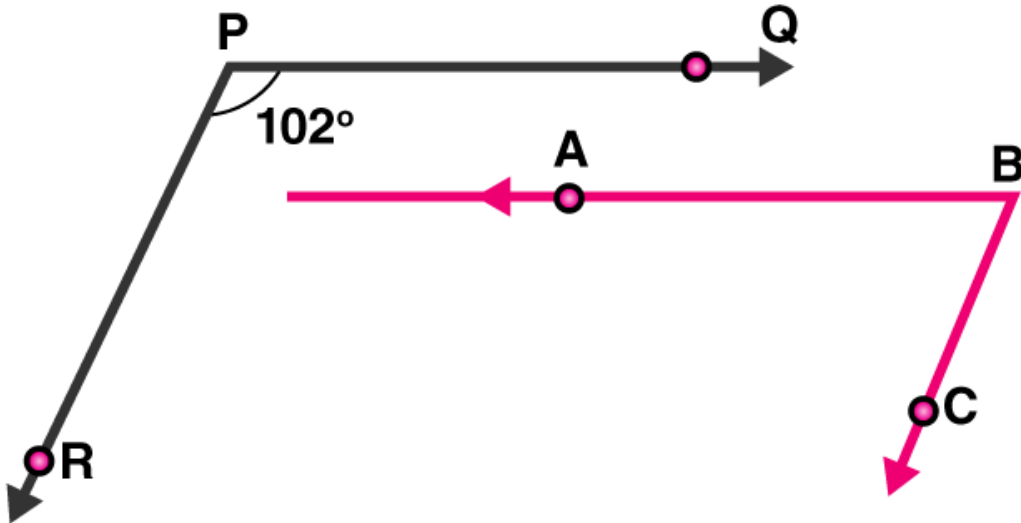
Also,  $BA \parallel CD$

$$\Rightarrow \angle BAC = \angle ACD = 70^\circ$$
 [Alternative angles of parallel lines are equal]

But,  $\angle ACE + \angle ECD = 70^\circ$

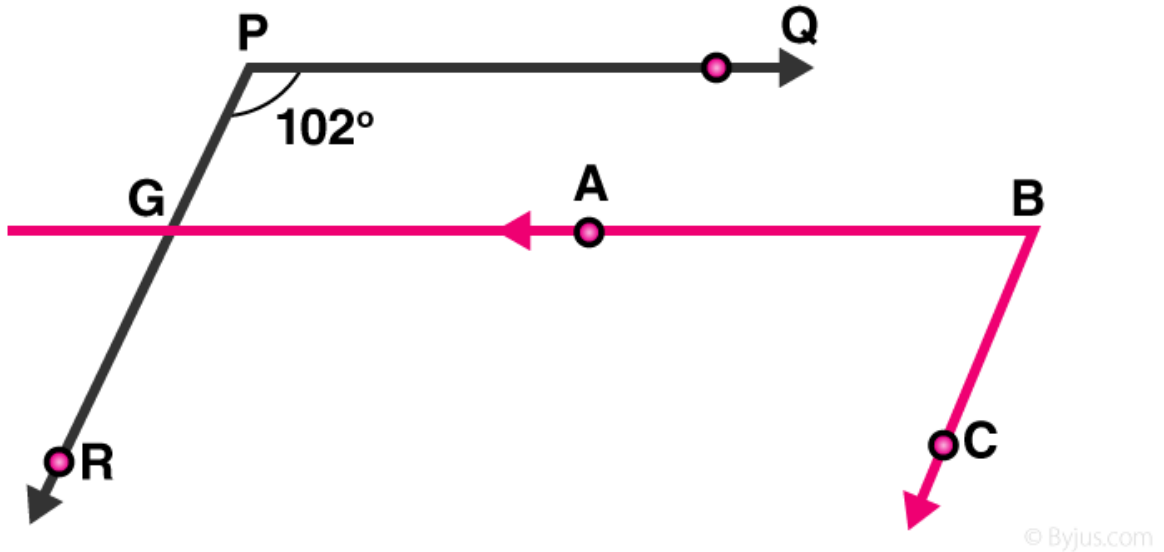
$$\Rightarrow \angle ACE = 70^\circ - 50^\circ = 20^\circ$$

**Question 6:** In figure,  $PQ \parallel AB$  and  $PR \parallel BC$ . If  $\angle QPR = 102^\circ$ , determine  $\angle ABC$ . Give reasons.



**Solution:** Extend line AB to meet line PR at point G.

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Given:  $PQ \parallel AB$ ,

$\angle QPR = \angle BGR = 102^\circ$  [Corresponding angles of parallel lines are equal]

And  $PR \parallel BC$ ,

$\angle RGB + \angle CBG = 180^\circ$  [Corresponding angles are supplementary]

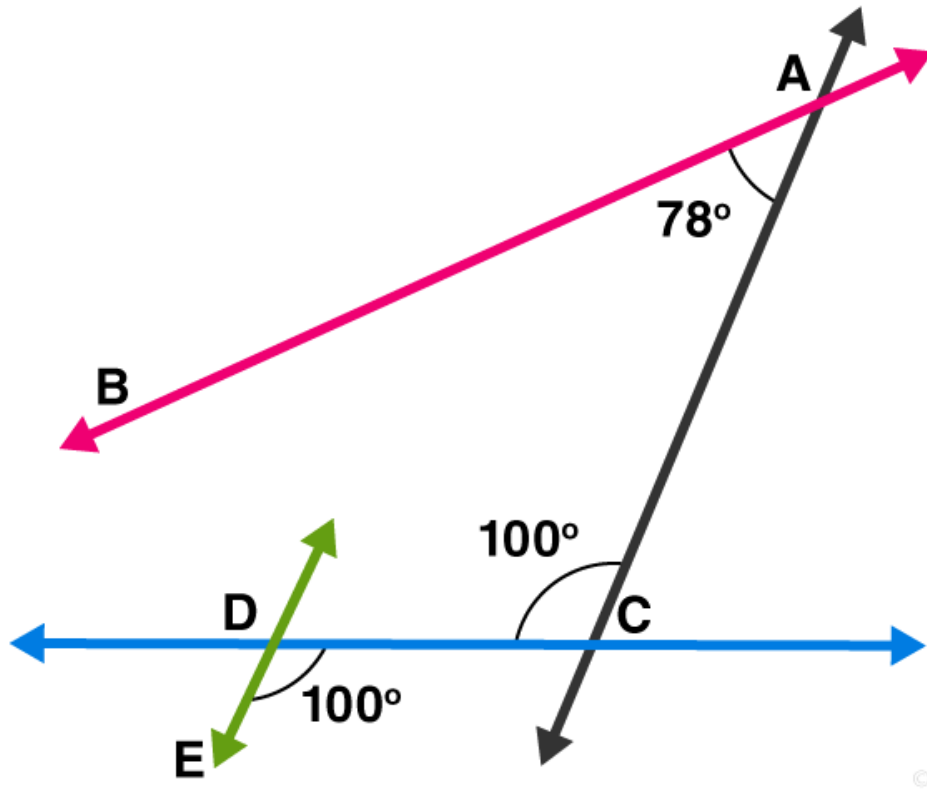
$\angle CBG = 180^\circ - 102^\circ = 78^\circ$

Since,  $\angle CBG = \angle ABC$

$\Rightarrow \angle ABC = 78^\circ$

**Question 7 : In figure, state which lines are parallel and why?**

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**Solution:**

We know, If a transversal intersects two lines such that a pair of alternate interior angles are equal, then the two lines are parallel

From figure:

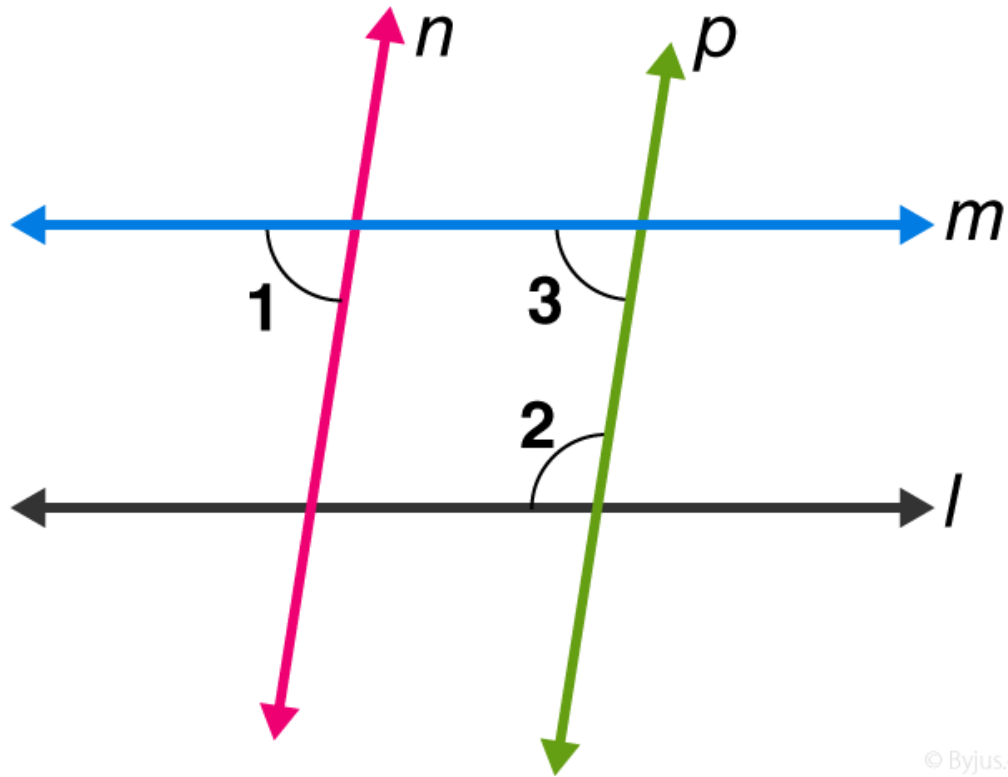
$$\Rightarrow \angle EDC = \angle DCA = 100^\circ$$

Lines DE and AC are intersected by a transversal DC such that the pair of alternate angles are equal.

So,  $DE \parallel AC$

**Question 8:** In figure, if  $l \parallel m$ ,  $n \parallel p$  and  $\angle 1 = 85^\circ$ , find  $\angle 2$ .

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**Solution:**

Given:  $\angle 1 = 85^\circ$

As we know, when a line cuts the parallel lines, the pair of alternate interior angles are equal.

$$\Rightarrow \angle 1 = \angle 3 = 85^\circ$$

Again, co-interior angles are supplementary, so

$$\angle 2 + \angle 3 = 180^\circ$$

$$\angle 2 + 85^\circ = 180^\circ$$

$$\angle 2 = 180^\circ - 85^\circ$$

$$\angle 2 = 95^\circ$$

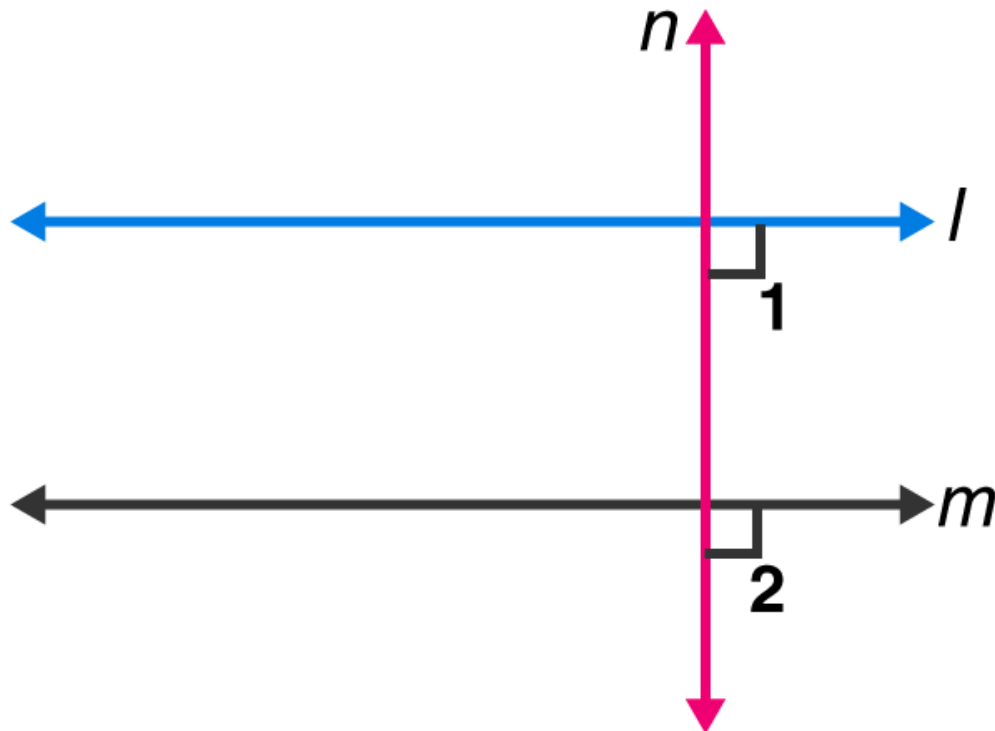
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**Question 9 :** If two straight lines are perpendicular to the same line, prove that they are parallel to each other.

**Solution:**

Let lines  $l$  and  $m$  are perpendicular to  $n$ , then

$$\angle 1 = \angle 2 = 90^\circ$$



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Since, lines  $l$  and  $m$  cut by a transversal line  $n$  and the corresponding angles are equal, which shows that, line  $l$  is parallel to line  $m$ .

**Question 10:** Prove that if the two arms of an angle are perpendicular to the two arms of another angle, then the angles are either equal or supplementary.

**Solution:** Let the angles be  $\angle ACB$  and  $\angle ABD$

Let  $AC$  perpendicular to  $AB$ , and  $CD$  is perpendicular to  $BD$ .

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To Prove :  $\angle ACD = \angle ABD$  OR  $\angle ACD + \angle ABD = 180^\circ$

Proof :

In a quadrilateral,

$\angle A + \angle C + \angle D + \angle B = 360^\circ$  [ Sum of angles of quadrilateral is  $360^\circ$  ]

$\Rightarrow 180^\circ + \angle C + \angle B = 360^\circ$

$\Rightarrow \angle C + \angle B = 360^\circ - 180^\circ$

Therefore,  $\angle ACD + \angle ABD = 180^\circ$

And  $\angle ABD = \angle ACD = 90^\circ$

Hence, angles are equal as well as supplementary.

### **Exercise VSAQs**

**Question 1: Define complementary angles.**

**Solution:** When the sum of two angles is 90 degrees, then the angles are known as complementary angles.

**Question 2: Define supplementary angles.**

**Solution:** When the sum of two angles is  $180^\circ$ , then the angles are known as supplementary angles.

**Question 3: Define adjacent angles.**

**Solution:** Two angles are Adjacent when they have a common side and a common vertex.

**Question 4: The complement of an acute angle is \_\_\_\_\_.**

**Solution:** An acute angle

**Question 5: The supplement of an acute angle is \_\_\_\_\_.**

**Solution:** An obtuse angle

**Question 6: The supplement of a right angle is \_\_\_\_\_.**

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**Solution:** A right angle



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- Chapter 2–Exponents of Real Numbers
- Chapter 3–Rationalisation
- Chapter 4–Algebraic Identities
- Chapter 5–Factorization of Algebraic Expressions
- Chapter 6–Factorization Of Polynomials
- Chapter 7–Introduction to Euclid’s Geometry
- Chapter 8–Lines and Angles
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- Chapter 15–Area of Parallelograms and Triangles
- Chapter 16–Circles
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- Chapter 19–Surface Area and Volume of A Right Circular Cylinder
- Chapter 20–Surface Area and Volume of A Right Circular Cone
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- Chapter 24–Measure of Central Tendency
- Chapter 25–Probability

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# About RD Sharma

*RD Sharma isn't the kind of author you'd bump into at lit fests. But his bestselling books have helped many CBSE students lose their dread of maths. Sunday Times profiles the tutor turned internet star*

He dreams of algorithms that would give most people nightmares. And, spends every waking hour thinking of ways to explain concepts like 'series solution of linear differential equations'. Meet Dr Ravi Dutt Sharma — mathematics teacher and author of 25 reference books — whose name evokes as much awe as the subject he teaches. And though students have used his thick tomes for the last 31 years to ace the dreaded maths exam, it's only recently that a spoof video turned the tutor into a YouTube star.

R D Sharma had a good laugh but said he shared little with his on-screen persona except for the love for maths. "I like to spend all my time thinking and writing about maths problems. I find it relaxing," he says. When he is not writing books explaining mathematical concepts for classes 6 to 12 and engineering students, Sharma is busy dispensing his duty as vice-principal and head of department of science and humanities at Delhi government's Guru Nanak Dev Institute of Technology.

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