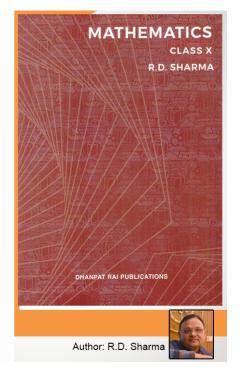
Class 10 -Chapter 4 Triangles





RD Sharma Solutions for Class 10 Maths Chapter 4–Triangles

Class 10: Maths Chapter 4 solutions. Complete Class 10 Maths Chapter 4 Notes.

RD Sharma Solutions for Class 10 Maths Chapter 4–Triangles

RD Sharma 10th Maths Chapter 4, Class 10 Maths Chapter 4 solutions

Exercise 4.1 Page No: 4.3

1. Fill in the blanks using the correct word given in brackets:





(i) All circles are (congruent, similar).							
(ii) All squares are (similar, congruent).							
(iii) All triangles are similar (isosceles, equilaterals).							
(iv) Two triangles are similar, if their corresponding angles are (proportional, equal)							
(v) Two triangles are similar, if their corresponding sides are (proportional, equal)							
(vi) Two polygons of the same number of sides are similar, if (a)their corresponding angles are and their corresponding sides are (b) (equal, proportional).							
Solutions:							
(i) All circles are similar.							
(ii) All squares are similar.							
(iii) All equilateral triangles are similar.							
(iv) Two triangles are similar, if their corresponding angles are equal.							
(v) Two triangles are similar, if their corresponding sides are proportional.							
(vi) Two polygons of the same number of sides are similar, if (a) equal their corresponding angles are and their corresponding sides are (b) proportional.							
Exercise 4.2 Page No: 4.19							
1. In a Δ ABC, D and E are points on the sides AB and AC respectively such that DE $\mid\mid$ BC.							
i) If AD = 6 cm, DB = 9 cm and AE = 8 cm, Find AC.							
Solution:							
Given: \triangle ABC, DE $\#$ BC, AD = 6 cm, DB = 9 cm and AE = 8 cm.							

https://www.indcareer.com/schools/rd-sharma-solutions-for-class-10-maths-chapter-4-triangles/



Required to find AC.



By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

Let CE = x.

So then.

6/9 = 8/x

6x = 72 cm

x = 72/6 cm

x = 12 cm

 \therefore AC = AE + CE = 12 + 8 = 20.

ii) If AD/DB = 3/4 and AC = 15 cm, Find AE.

Solution:

Given: AD/BD = 3/4 and AC = 15 cm [As $DE \parallel BC$]

Required to find AE.

By using Thales Theorem, [As DE # BC]

AD/BD = AE/CE

Let, AE = x, then CE = 15-x.

 \Rightarrow 3/4 = x/ (15–x)

45 - 3x = 4x

-3x - 4x = -45

7x = 45

x = 45/7

x = 6.43 cm

∴ AE= 6.43cm





iii) If AD/DB = 2/3 and AC = 18 cm, Find AE.

Solution:

Given: AD/BD = 2/3 and AC = 18 cm

Required to find AE.

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

Let, AE = x and CE = 18 - x

 \Rightarrow 23 = x/ (18–x)

3x = 36 - 2x

5x = 36 cm

x = 36/5 cm

x = 7.2 cm

 \therefore AE = 7.2 cm

iv) If AD = 4 cm, AE = 8 cm, DB = x - 4 cm and EC = 3x - 19, find x.

Solution:

Given: AD = 4 cm, AE = 8 cm, DB = x - 4 and EC = 3x - 19

Required to find x.

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

Then, 4/(x-4) = 8/(3x-19)

4(3x - 19) = 8(x - 4)

12x - 76 = 8(x - 4)

12x - 8x = -32 + 76





4x = 44 cm

x = 11 cm

v) If AD = 8 cm, AB = 12 cm and AE = 12 cm, find CE.

Solution:

Given: AD = 8 cm, AB = 12 cm, and AE = 12 cm.

Required to find CE,

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

8/4 = 12/CE

 $8 \times CE = 4 \times 12 \text{ cm}$

 $CE = (4 \times 12)/8 \text{ cm}$

CE = 48/8 cm

∴ CE = 6 cm

vi) If AD = 4 cm, DB = 4.5 cm and AE = 8 cm, find AC.

Solution:

Given: AD = 4 cm, DB = 4.5 cm, AE = 8 cm

Required to find AC.

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

4/4.5 = 8/AC

 $AC = (4.5 \times 8)/4 \text{ cm}$

∴AC = 9 cm

vii) If AD = 2 cm, AB = 6 cm and AC = 9 cm, find AE.





Solution:

Given: AD = 2 cm, AB = 6 cm and AC = 9 cm

Required to find AE.

DB = AB - AD = 6 - 2 = 4 cm

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

2/4 = x/(9-x)

4x = 18 - 2x

6x = 18

x = 3 cm

∴ AE= 3cm

viii) If AD/BD = 4/5 and EC = 2.5 cm, Find AE.

Solution:

Given: AD/BD = 4/5 and EC = 2.5 cm

Required to find AE.

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

Then, 4/5 = AE/2.5

 \therefore AE = 4 × 2.55 = 2 cm

ix) If AD = x cm, DB = x - 2 cm, AE = x + 2 cm, and EC = x - 1 cm, find the value of x.

Solution:

Given: AD = x, DB = x - 2, AE = x + 2 and EC = x - 1

Required to find the value of x.





By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

So,
$$x/(x-2) = (x+2)/(x-1)$$

$$x(x-1) = (x-2)(x+2)$$

$$x^2 - x - x^2 + 4 = 0$$

x = 4

x) If AD = 8x - 7 cm, DB = 5x - 3 cm, AE = 4x - 3 cm, and EC = (3x - 1) cm, Find the value of x.

Solution:

Given: AD = 8x - 7, DB = 5x - 3, AER = 4x - 3 and EC = 3x - 1

Required to find x.

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

$$(8x-7)/(5x-3) = (4x-3)/(3x-1)$$

$$(8x-7)(3x-1) = (5x-3)(4x-3)$$

$$24x^2 - 29x + 7 = 20x^2 - 27x + 9$$

$$4x^2 - 2x - 2 = 0$$

$$2(2x^2 - x - 1) = 0$$

$$2x^2 - x - 1 = 0$$

$$2x^2 - 2x + x - 1 = 0$$

$$2x(x-1) + 1(x-1) = 0$$

$$(x-1)(2x+1)=0$$

$$\Rightarrow$$
 x = 1 or x = -1/2





We know that the side of triangle can never be negative. Therefore, we take the positive value.

$$\therefore x = 1$$
.

xi) If AD =
$$4x - 3$$
, AE = $8x - 7$, BD = $3x - 1$, and CE = $5x - 3$, find the value of x.

Solution:

Given:
$$AD = 4x - 3$$
, $BD = 3x - 1$, $AE = 8x - 7$ and $EC = 5x - 3$

Required to find x.

By using Thales Theorem, [As DE // BC]

$$AD/BD = AE/CE$$

So,
$$(4x-3)/(3x-1) = (8x-7)/(5x-3)$$

$$(4x-3)(5x-3) = (3x-1)(8x-7)$$

$$4x(5x-3)-3(5x-3) = 3x(8x-7)-1(8x-7)$$

$$20x^2 - 12x - 15x + 9 = 24x^2 - 29x + 7$$

$$20x^2 - 27x + 9 = 24^2 - 29x + 7$$

$$\Rightarrow$$
 -4x² + 2x + 2 = 0

$$4x^2 - 2x - 2 = 0$$

$$4x^2 - 4x + 2x - 2 = 0$$

$$4x(x-1) + 2(x-1) = 0$$

$$(4x + 2)(x - 1) = 0$$

$$\Rightarrow$$
 x = 1 or x = -2/4

We know that the side of triangle can never be negative. Therefore, we take the positive value.

$$\therefore x = 1$$

xii) If AD = 2.5 cm, BD = 3.0 cm, and AE = 3.75 cm, find the length of AC.

Solution:





Given: AD = 2.5 cm, AE = 3.75 cm and BD = 3 cm

Required to find AC.

By using Thales Theorem, [As DE // BC]

AD/BD = AE/CE

2.5/3 = 3.75/CE

 $2.5 \times CE = 3.75 \times 3$

 $CE = 3.75 \times 32.5$

CE = 11.252.5

CE = 4.5

Now, AC = 3.75 + 4.5

 \therefore AC = 8.25 cm.

2. In a \triangle ABC, D and E are points on the sides AB and AC respectively. For each of the following cases show that DE # BC:

i) AB = 12 cm, AD = 8 cm, AE = 12 cm, and AC = 18 cm.

Solution:

Required to prove DE // BC.

We have,

AB = 12 cm, AD = 8 cm, AE = 12 cm, and AC = 18 cm. (Given)

So,

BD = AB - AD = 12 - 8 = 4 cm

And,

CE = AC - AE = 18 - 12 = 6 cm

It's seen that,





AD/BD = 8/4 = 1/2

AE/CE = 12/6 = 1/2

Thus,

AD/BD = AE/CE

So, by the converse of Thale's Theorem

We have,

DE // BC.

Hence Proved.

ii) AB = 5.6 cm, AD = 1.4 cm, AC = 7.2 cm, and AE = 1.8 cm.

Solution:

Required to prove DE // BC.

We have,

AB = 5.6 cm, AD = 1.4 cm, AC = 7.2 cm, and AE = 1.8 cm. (Given)

So,

BD = AB - AD = 5.6 - 1.4 = 4.2 cm

And,

CE = AC - AE = 7.2 - 1.8 = 5.4 cm

It's seen that,

AD/BD = 1.4/4.2 = 1/3

AE/CE = 1.8/5.4 = 1/3

Thus,

AD/BD = AE/CE

So, by the converse of Thale's Theorem





We have,

DE // BC.

Hence Proved.

iii) AB = 10.8 cm, BD = 4.5 cm, AC = 4.8 cm, and AE = 2.8 cm.

Solution:

Required to prove DE // BC.

We have

AB = 10.8 cm, BD = 4.5 cm, AC = 4.8 cm, and AE = 2.8 cm.

So,

$$AD = AB - DB = 10.8 - 4.5 = 6.3$$

And,

$$CE = AC - AE = 4.8 - 2.8 = 2$$

It's seen that,

$$AD/BD = 6.3/4.5 = 2.8/2.0 = AE/CE = 7/5$$

So, by the converse of Thale's Theorem

We have,

DE // BC.

Hence Proved.

iv) AD = 5.7 cm, BD = 9.5 cm, AE = 3.3 cm, and EC = 5.5 cm.

Solution:

Required to prove DE // BC.

We have

AD = 5.7 cm, BD = 9.5 cm, AE = 3.3 cm, and EC = 5.5 cm





Now,

AD/BD = 5.7/9.5 = 3/5

And,

AE/CE = 3.3/5.5 = 3/5

Thus,

AD/BD = AE/CE

So, by the converse of Thale's Theorem

We have,

DE // BC.

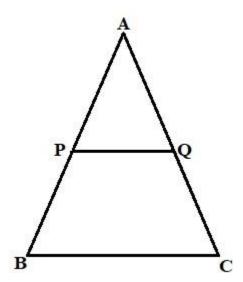
Hence Proved.

3. In a \triangle ABC, P and Q are the points on sides AB and AC respectively, such that PQ # BC. If AP = 2.4 cm, AQ = 2 cm, QC = 3 cm and BC = 6 cm. Find AB and PQ.

Solution:

Given: \triangle ABC, AP = 2.4 cm, AQ = 2 cm, QC = 3 cm, and BC = 6 cm. Also, PQ // BC.

Required to find: AB and PQ.







By using Thales Theorem, we have [As it's given that PQ // BC]

AP/PB = AQ/QC

2.4/PB = 2/3

 $2 \times PB = 2.4 \times 3$

 $PB = (2.4 \times 3)/2 \text{ cm}$

 \Rightarrow PB = 3.6 cm

Now finding, AB = AP + PB

AB = 2.4 + 3.6

 \Rightarrow AB = 6 cm

Now, considering \triangle APQ and \triangle ABC

We have,

 $\angle A = \angle A$

 \angle APQ = \angle ABC (Corresponding angles are equal, PQ||BC and AB being a transversal)

Thus, \triangle APQ and \triangle ABC are similar to each other by AA criteria.

Now, we know that

Corresponding parts of similar triangles are propositional.

 \Rightarrow AP/AB = PQ/BC

 \Rightarrow PQ = (AP/AB) x BC

 $= (2.4/6) \times 6 = 2.4$

∴ PQ = 2.4 cm.

4. In a \triangle ABC, D and E are points on AB and AC respectively, such that DE # BC. If AD = 2.4 cm, AE = 3.2 cm, DE = 2 cm and BC = 5 cm. Find BD and CE.

Solution:





Given: \triangle ABC such that AD = 2.4 cm, AE = 3.2 cm, DE = 2 cm and BE = 5 cm. Also DE # BC.

Required to find: BD and CE.

As DE // BC, AB is transversal,

 $\angle APQ = \angle ABC$ (corresponding angles)

As DE // BC, AC is transversal,

 \angle AED = \angle ACB (corresponding angles)

In \triangle ADE and \triangle ABC,

∠ADE=∠ABC

∠AED=∠ACB

 $\therefore \triangle$ ADE = \triangle ABC (AA similarity criteria)

Now, we know that

Corresponding parts of similar triangles are propositional.

 \Rightarrow AD/AB = AE/AC = DE/BC

AD/AB = DE/BC

2.4/(2.4 + DB) = 2/5 [Since, AB = AD + DB]

2.4 + DB = 6

DB = 6 - 2.4

DB = 3.6 cm

In the same way,

⇒ AE/AC = DE/BC

3.2/(3.2 + EC) = 2/5 [Since AC = AE + EC]

3.2 + EC = 8

EC = 8 - 3.2





EC = 4.8 cm

∴ BD = 3.6 cm and CE = 4.8 cm.

Exercise 4.3 Page No: 4.31

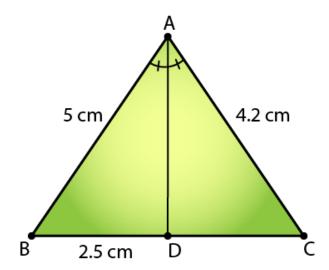
1. In a \triangle ABC, AD is the bisector of \angle A, meeting side BC at D.

(i) if BD = 2.5 cm, AB = 5 cm, and AC = 4.2 cm, find DC.

Solution:

Given: \triangle ABC and AD bisects \angle A, meeting side BC at D. And BD = 2.5 cm, AB = 5 cm, and AC = 4.2 cm.

Required to find: DC



Since, AD is the bisector of \angle A meeting side BC at D in \triangle ABC

 \Rightarrow AB/ AC = BD/ DC

5/4.2 = 2.5/ DC

 $5DC = 2.5 \times 4.2$





 \therefore DC = 2.1 cm

(ii) if BD = 2 cm, AB = 5 cm, and DC = 3 cm, find AC.

Solution:

Given: \triangle ABC and AD bisects \angle A, meeting side BC at D. And BD = 2 cm, AB = 5 cm, and DC = 3 cm

Required to find: AC

Since, AD is the bisector of \angle A meeting side BC at D in \triangle ABC

 \Rightarrow AB/ AC = BD/ DC

5/AC = 2/3

 $2AC = 5 \times 3$

 \therefore AC = 7.5 cm

(iii) if AB = 3.5 cm, AC = 4.2 cm, and DC = 2.8 cm, find BD.

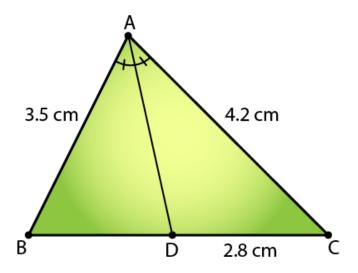
Solution:

Given: \triangle ABC and AD bisects \angle A, meeting side BC at D. And AB = 3.5 cm, AC = 4.2 cm, and DC = 2.8 cm.

Required to find: BD







 \Rightarrow AB/ AC = BD/ DC

3.5/4.2 = BD/2.8

 $4.2 \times BD = 3.5 \times 2.8$

BD = 7/3

∴ BD = 2.3 cm

(iv) if AB = 10 cm, AC = 14 cm, and BC = 6 cm, find BD and DC.

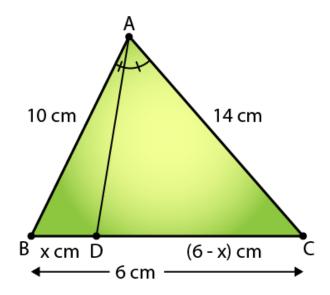
Solution:

Given: In \triangle ABC, AD is the bisector of \angle A meeting side BC at D. And, AB = 10 cm, AC = 14 cm, and BC = 6 cm

Required to find: BD and DC.







Since, AD is bisector of $\angle A$

We have,

AB/AC = BD/DC (AD is bisector of \angle A and side BC)

Then, 10/14 = x/(6 - x)

14x = 60 - 6x

20x = 60

x = 60/20

∴ BD = 3 cm and DC = (6 - 3) = 3 cm.

(v) if AC = 4.2 cm, DC = 6 cm, and BC = 10 cm, find AB.

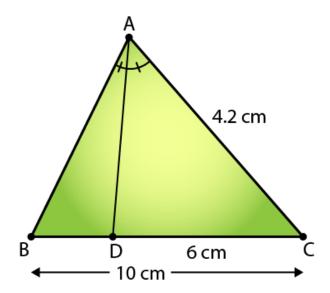
Solution:

Given: \triangle ABC and AD bisects \angle A, meeting side BC at D. And AC = 4.2 cm, DC = 6 cm, and BC = 10 cm.

Required to find: AB







$$\Rightarrow$$
 AB/ AC = BD/ DC

AB/ 4.2 = BD/ 6

We know that,

$$BD = BC - DC = 10 - 6 = 4 \text{ cm}$$

$$\Rightarrow$$
 AB/ 4.2 = 4/6

$$AB = (2 \times 4.2)/3$$

(vi) if AB = 5.6 cm, AC = 6 cm, and DC = 3 cm, find BC.

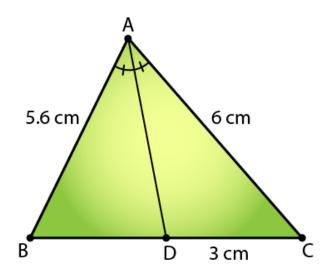
Solution:

Given: \triangle ABC and AD bisects \angle A, meeting side BC at D. And AB = 5.6 cm, AC = 6 cm, and DC = 3 cm.

Required to find: BC







 \Rightarrow AB/ AC = BD/ DC

5.6/6 = BD/3

BD = 5.6/2 = 2.8cm

And, we know that,

BD = BC - DC

2.8 = BC - 3

∴ BC = 5.8 cm

(vii) if AB = 5.6 cm, BC = 6 cm, and BD = 3.2 cm, find AC.

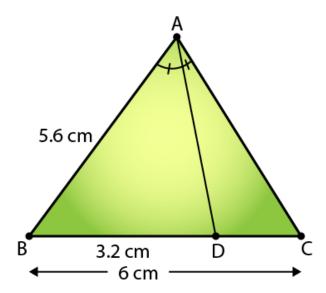
Solution:

Given: \triangle ABC and AD bisects \angle A, meeting side BC at D. And AB = 5.6 cm, BC = 6 cm, and BD = 3.2 cm.

Required to find: AC







⇒ AB/ AC = BD/ DC

5.6/AC = 3.2/DC

And, we know that

BD = BC - DC

3.2 = 6 - DC

∴ DC = 2.8 cm

 \Rightarrow 5.6/ AC = 3.2/ 2.8

 $AC = (5.6 \times 2.8)/3.2$

∴ AC = 4.9 cm

(viii) if AB = 10 cm, AC = 6 cm, and BC = 12 cm, find BD and DC.

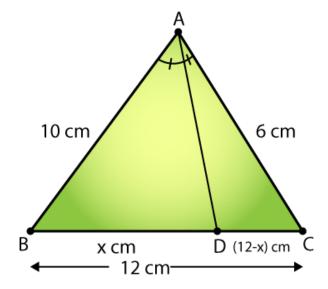
Solution:

Given: \triangle ABC and AD bisects \angle A, meeting side BC at D. AB = 10 cm, AC = 6 cm, and BC = 12 cm.





Required to find: DC



Since, AD is the bisector of \angle A meeting side BC at D in \triangle ABC

$$\Rightarrow$$
 AB/AC = BD/DC

$$10/6 = BD/DC(i)$$

And, we know that

$$BD = BC - DC = 12 - DC$$

Let BD = x,

$$\Rightarrow$$
 DC = 12 - x

Thus (i) becomes,

$$10/6 = x/(12 - x)$$

$$5(12-x)=3x$$

$$60 - 5x = 3x$$

$$\therefore$$
 x = 60/8 = 7.5

Hence, DC = 12 - 7.5 = 4.5cm and BD = 7.5 cm



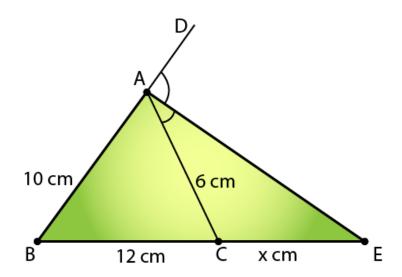


2. In figure 4.57, AE is the bisector of the exterior \angle CAD meeting BC produced in E. If AB = 10 cm, AC = 6 cm, and BC = 12 cm, find CE.

Solution:

Given: AE is the bisector of the exterior \angle CAD and AB = 10 cm, AC = 6 cm, and BC = 12 cm.

Required to find: CE



Since AE is the bisector of the exterior $\angle CAD$.

BE / CE = AB / AC

Let's take CE as x.

So, we have

BE/ CE = AB/ AC

(12+x)/x = 10/6

6x + 72 = 10x

10x - 6x = 72

4x = 72





$$x = 18$$

Therefore, CE = 18 cm.

3. In fig. 4.58, \triangle ABC is a triangle such that AB/AC = BD/DC, \angle B=70°, \angle C = 50°, find \angle BAD.

Solution:

Given: \triangle ABC such that AB/AC = BD/DC, \angle B = 70° and \angle C = 50°

Required to find: ∠BAD

We know that,

In ΔABC,

 $\angle A = 180 - (70 + 50)$ [Angle sum property of a triangle]

= 180 - 120

 $= 60^{\circ}$

Since,

AB/AC = BD/DC,

AD is the angle bisector of angle $\angle A$.

Thus,

 $\angle BAD = \angle A/2 = 60/2 = 30^{\circ}$

Exercise 4.4 Page No: 4.37

1. (i) In fig. 4.70, if AB # CD, find the value of x.

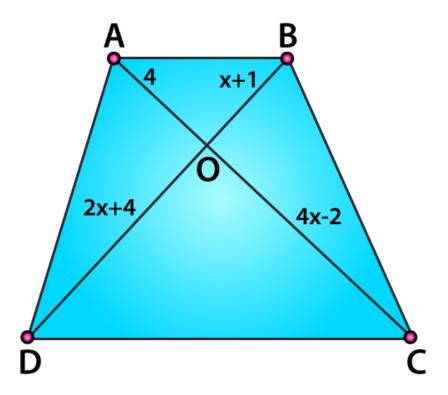
Solution:

It's given that AB // CD.

Required to find the value of x.







We know that,

Diagonals of a parallelogram bisect each other.

So,

$$\Rightarrow$$
 4/ (4x - 2) = (x +1)/ (2x + 4)

$$4(2x + 4) = (4x - 2)(x + 1)$$

$$8x + 16 = x(4x - 2) + 1(4x - 2)$$

$$8x + 16 = 4x^2 - 2x + 4x - 2$$

$$-4x^2 + 8x + 16 + 2 - 2x = 0$$

$$-4x^2 + 6x + 8 = 0$$





$$4x^2 - 6x - 18 = 0$$

$$4x^2 - 12x + 6x - 18 = 0$$

$$4x(x-3) + 6(x-3) = 0$$

$$(4x + 6)(x - 3) = 0$$

$$\therefore x = -6/4 \text{ or } x = 3$$

(ii) In fig. 4.71, if AB $/\!\!/$ CD, find the value of x.

Solution:

It's given that AB // CD.

Required to find the value of x.

We know that,

Diagonals of a parallelogram bisect each other

So,

$$\Rightarrow$$
 (6x - 5)/ (2x + 1) = (5x - 3)/ (3x - 1)

$$(6x-5)(3x-1) = (2x+1)(5x-3)$$

$$3x(6x-5) - 1(6x-5) = 2x(5x-3) + 1(5x-3)$$

$$18x^2 - 10x^2 - 21x + 5 + x + 3 = 0$$

$$8x^2 - 16x - 4x + 8 = 0$$

$$8x(x-2)-4(x-2)=0$$

$$(8x-4)(x-2)=0$$

$$x = 4/8 = 1/2 \text{ or } x = -2$$

(iii) In fig. 4.72, if AB // CD. If OA = 3x - 19, OB = x - 4, OC = x - 3 and OD = 4, find x.

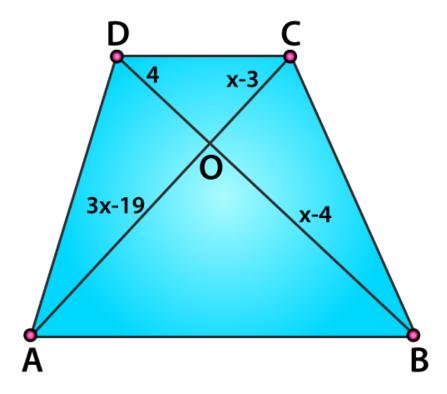




Solution:

It's given that AB // CD.

Required to find the value of x.



We know that,

Diagonals of a parallelogram bisect each other

So,

AO/CO = BO/DO

$$(3x-19)/(x-3) = (x-4)/4$$

$$4(3x-19) = (x-3)(x-4)$$

$$12x - 76 = x(x - 4) - 3(x - 4)$$





$$12x - 76 = x^2 - 4x - 3x + 12$$

$$-x^2 + 7x - 12 + 12x - 76 = 0$$

$$-x^2 + 19x - 88 = 0$$

$$x^2 - 19x + 88 = 0$$

$$x^2 - 11x - 8x + 88 = 0$$

$$x(x-11) - 8(x-11) = 0$$

$$\therefore$$
 x = 11 or x = 8

Exercise 4.5 Page No: 4.37

1. In fig. 4.136, \triangle ACB ~ \triangle APQ. If BC = 8 cm, PQ = 4 cm, BA = 6.5 cm and AP = 2.8 cm, find CA and AQ.

Solution:

Given,

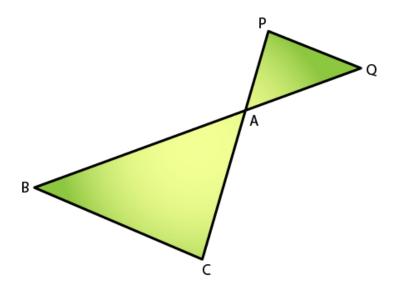
ΔACB ~ ΔAPQ

BC = 8 cm, PQ = 4 cm, BA = 6.5 cm and AP = 2.8 cm

Required to find: CA and AQ







We know that,

ΔACB ~ ΔAPQ [given]

BA/ AQ = CA/ AP = BC/ PQ [Corresponding Parts of Similar Triangles]

So,

6.5/AQ = 8/4

 $AQ = (6.5 \times 4)/8$

AQ = 3.25 cm

Similarly, as

CA/AP = BC/PQ

CA/2.8 = 8/4

 $CA = 2.8 \times 2$

CA = 5.6 cm

Hence, CA = 5.6 cm and AQ = 3.25 cm.

2. In fig.4.137, AB // QR, find the length of PB.





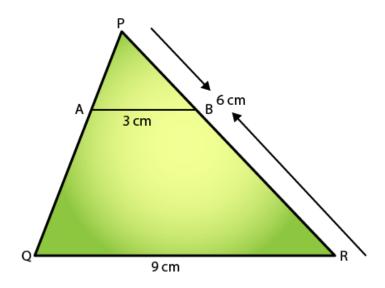
Solution:

Given,

ΔPQR, AB // QR and

AB = 3 cm, QR = 9 cm and PR = 6 cm

Required to find: PB



In $\triangle PAB$ and $\triangle PQR$

We have,

 $\angle P = \angle P$ [Common]

 \angle PAB = \angle PQR [Corresponding angles as AB||QR with PQ as the transversal]

⇒ ΔPAB ~ ΔPQR [By AA similarity criteria]

Hence,

AB/ QR = PB/ PR [Corresponding Parts of Similar Triangles are propositional]

 \Rightarrow 3/9 = PB/6

PB = 6/3





Therefore, PB = 2 cm

3. In fig. 4.138 given, XY // BC. Find the length of XY.

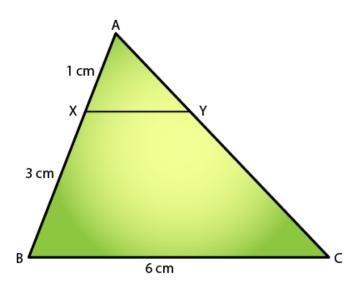
Solution:

Given,

XY // BC

AX = 1 cm, XB = 3 cm and BC = 6 cm

Required to find: XY



In ΔAXY and ΔABC

We have.

 $\angle A = \angle A$ [Common]

 \angle AXY = \angle ABC [Corresponding angles as AB||QR with PQ as the transversal]

⇒ ΔAXY ~ ΔABC [By AA similarity criteria]

Hence,

XY/ BC = AX/ AB [Corresponding Parts of Similar Triangles are propositional]





We know that,

$$(AB = AX + XB = 1 + 3 = 4)$$

$$XY/6 = 1/4$$

$$XY/1 = 6/4$$

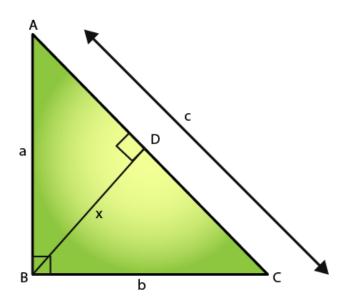
Therefore, XY = 1.5 cm

4. In a right-angled triangle with sides a and b and hypotenuse c, the altitude drawn on the hypotenuse is x. Prove that ab = cx.

Solution:

Consider \triangle ABC to be a right angle triangle having sides a and b and hypotenuse c. Let BD be the altitude drawn on the hypotenuse AC.

Required to prove: ab = cx



We know that,

In ΔACB and ΔCDB

$$\angle B = \angle B$$
 [Common]

$$\angle$$
ACB = \angle CDB = 90°





⇒ ΔACB ~ ΔCDB [By AA similarity criteria]

Hence,

AB/ BD = AC/ BC [Corresponding Parts of Similar Triangles are propositional]

a/x = c/b

 \Rightarrow xc = ab

Therefore, ab = cx

5. In fig. 4.139, \angle ABC = 90 and BD \perp AC. If BD = 8 cm, and AD = 4 cm, find CD.

Solution:

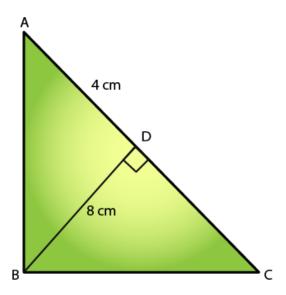
Given,

 \angle ABC = 90° and BD \perp AC

BD = 8 cm

AD = 4 cm

Required to find: CD.



We know that,





ABC is	a riaht	angled	triangle	and	RD I	ΔC
ADC IS	a nyni	angleu	ulaliqie	anu	DDT	AC.

Then, ΔDBA~ΔDCB [By AA similarity]

BD/CD = AD/BD

 $BD^2 = AD \times DC$

 $(8)^2 = 4 \times DC$

DC = 64/4 = 16 cm

Therefore, CD = 16 cm

6. In fig.4.140, \angle ABC = 90° and BD \perp AC. If AC = 5.7 cm, BD = 3.8 cm and CD = 5.4 cm, Find BC.

Solution:

Given:

 $BD \perp AC$

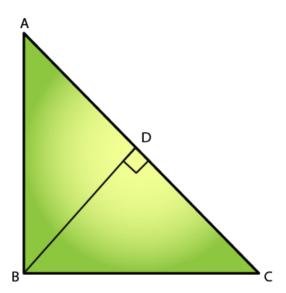
AC = 5.7 cm, BD = 3.8 cm and CD = 5.4 cm

∠ABC = 90°

Required to find: BC



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We know that,

ΔABC ~ ΔBDC [By AA similarity]

 \angle BCA = \angle DCA = 90°

 $\angle AXY = \angle ABC$ [Common]

Thus,

AB/ BD = BC/ CD [Corresponding Parts of Similar Triangles are propositional]

5.7/3.8 = BC/5.4

 $BC = (5.7 \times 5.4)/3.8 = 8.1$

Therefore, BC = 8.1 cm

7. In the fig.4.141 given, DE # BC such that AE = (1/4)AC. If AB = 6 cm, find AD.

Solution:

Given:

DE // BC

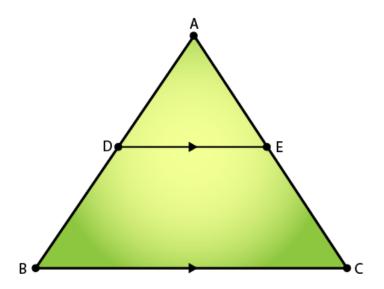
AE = (1/4)AC





AB = 6 cm.

Required to find: AD.



In ΔADE and ΔABC

We have,

 $\angle A = \angle A$ [Common]

 \angle ADE = \angle ABC [Corresponding angles as AB||QR with PQ as the transversal]

⇒ ΔADE ~ ΔABC [By AA similarity criteria]

Then,

AD/AB = AE/ AC [Corresponding Parts of Similar Triangles are propositional]

AD/6 = 1/4

 $4 \times AD = 6$

AD = 6/4

Therefore, AD = 1.5 cm

8. In the fig.4.142 given, if AB \perp BC, DC \perp BC, and DE \perp AC, prove that Δ CED $^{\sim}$ Δ ABC





Solution:

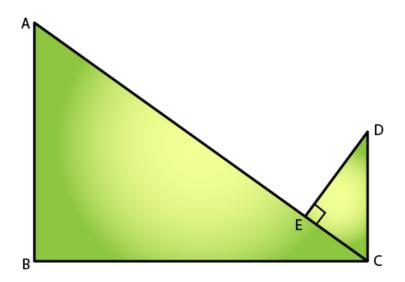
Given:

 $AB \perp BC$,

 $DC \perp BC$

DE \perp AC

Required to prove: ΔCED~ΔABC



We know that,

From ΔABC and ΔCED

 $\angle B = \angle E = 90^{\circ}$ [given]

 \angle BAC = \angle ECD [alternate angles since, AB || CD with BC as transversal]

Therefore, $\triangle CED^-\triangle ABC$ [AA similarity]

9. Diagonals AC and BD of a trapezium ABCD with AB # DC intersect each other at the point O. Using similarity criterion for two triangles, show that OA/ OC = OB/ OD

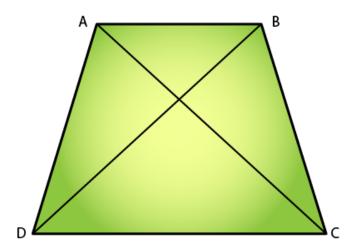
Solution:





Given: OC is the point of intersection of AC and BD in the trapezium ABCD, with AB // DC.

Required to prove: OA/ OC = OB/ OD



We know that,

In ΔAOB and ΔCOD

∠AOB = ∠COD [Vertically Opposite Angles]

 $\angle OAB = \angle OCD$ [Alternate angles]

Then, ΔAOB ~ ΔCOD

Therefore, OA/ OC = OB/ OD [Corresponding sides are proportional]

10. If \triangle ABC and \triangle AMP are two right triangles, right angled at B and M, respectively such that \angle MAP = \angle BAC. Prove that

- (i) ΔΑΒC ~ ΔΑΜΡ
- (ii) CA/PA = BC/MP

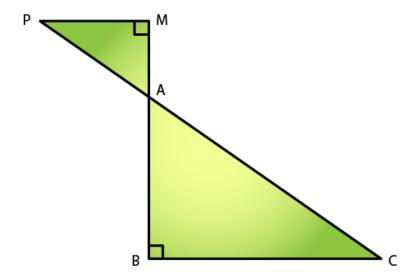
Solution:

(i) Given:





 \triangle ABC and \triangle AMP are the two right triangles.



We know that,

 $\angle AMP = \angle B = 90^{\circ}$

 \angle MAP = \angle BAC [Vertically Opposite Angles]

 $\Rightarrow \triangle ABC^{-}\triangle AMP$ [AA similarity]

(ii) Since, ΔABC~ΔAMP

CA/ PA = BC/ MP [Corresponding sides are proportional]

Hence proved.

11. A vertical stick 10 cm long casts a shadow 8 cm long. At the same time, a tower casts a shadow 30 m long. Determine the height of the tower.

Solution:

Given:

Length of stick = 10cm

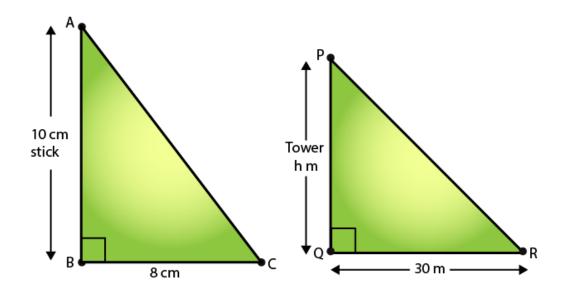
Length of the stick's shadow = 8cm





Length of the tower's shadow = 30m = 3000cm

Required to find: the height of the tower = PQ.



In ΔABC ~ ΔPQR

 \angle ABC = \angle PQR = 90°

 \angle ACB = \angle PRQ [Angular Elevation of Sun is same for a particular instant of time]

 \Rightarrow \triangle ABC ~ \triangle PQR [By AA similarity]

So, we have

AB/BC = PQ/QR [Corresponding sides are proportional]

10/8 = PQ/ 3000

 $PQ = (3000 \times 10)/8$

PQ = 30000/8

PQ = 3750/100

Therefore, PQ = 37.5 m

12. In fig.4.143, $\angle A = \angle CED$, prove that $\triangle CAB \sim \triangle CED$. Also find the value of x.



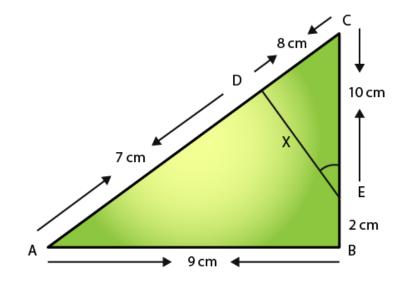


Solution:

Given:

 $\angle A = \angle CED$

Required to prove: ΔCAB ~ ΔCED



In ΔCAB ~ ΔCED

 $\angle C = \angle C$ [Common]

 $\angle A = \angle CED$ [Given]

 \Rightarrow \triangle CAB ~ \triangle CED [By AA similarity]

Hence, we have

CA/ CE = AB/ ED [Corresponding sides are proportional]

15/10 = 9/x

 $x = (9 \times 10)/15$

Therefore, x = 6 cm





Exercise 4.6 Page No: 4.94

- 1. Triangles ABC and DEF are similar.
- (i) If area of (\triangle ABC) = 16 cm², area (\triangle DEF) = 25 cm² and BC = 2.3 cm, find EF.
- (ii) If area (\triangle ABC) = 9 cm², area (\triangle DEF) = 64 cm² and DE = 5.1 cm, find AB.
- (iii) If AC = 19 cm and DF = 8 cm, find the ratio of the area of two triangles.
- (iv) If area of (\triangle ABC) = 36 cm², area (\triangle DEF) = 64 cm² and DE = 6.2 cm, find AB.
- (v) If AB = 1.2 cm and DE = 1.4 cm, find the ratio of the area of two triangles.

Solutions:

As we know that, the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we get

$$\frac{ar\Delta ABC}{ar\Delta DEF} = (\frac{BC}{EF})^2 \frac{16}{25} = (\frac{2.3}{EF})^2 \frac{4}{5} = \frac{2.3}{EF}$$

Therefore, EF = 2.875 cm

$$\frac{ar\Delta ABC}{ar\Delta DEF}=(\frac{AB}{DE})^2\,\frac{9}{64}=(\frac{AB}{DE})^2\,\frac{3}{8}=\frac{AB}{5.1}$$

Therefore, AB = 1.9125 cm

$$\frac{ar\Delta ABC}{ar\Delta DEF} = (\frac{AC}{DF})^2 \frac{ar\Delta ABC}{ar\Delta DEF} = (\frac{19}{8})^2 \frac{ar\Delta ABC}{ar\Delta DEF} = (\frac{361}{64})$$

Therefore, the ratio of the areas of the two triangles are 361: 64

$$\frac{ar\Delta ABC}{ar\Delta DEF} = \left(\frac{AB}{DE}\right)^2 \frac{36}{64} = \left(\frac{AB}{DE}\right)^2 \frac{6}{8} = \frac{AB}{6.2}$$

Therefore, AB = 4.65 cm

$$\frac{ar\Delta ABC}{ar\Delta DEF} = \left(\frac{AB}{DE}\right)^2 \frac{ar\Delta ABC}{ar\Delta DEF} = \left(\frac{1.2}{1.4}\right)^2 \frac{ar\Delta ABC}{ar\Delta DEF} = \left(\frac{36}{49}\right)$$

Therefore, the ratio of the areas of the two triangles are 36: 49





2. In the fig 4.178, \triangle ACB ~ \triangle APQ. If BC = 10 cm, PQ = 5 cm, BA = 6.5 cm, AP = 2.8 cm, find CA and AQ. Also, find the area (\triangle ACB): area (\triangle APQ).

Solution:

Given:

ΔACB is similar to ΔAPQ

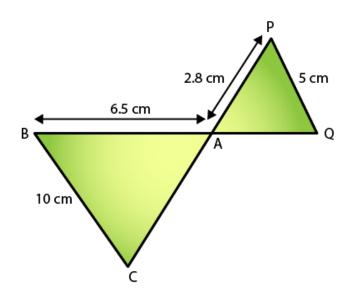
BC = 10 cm

PQ = 5 cm

BA = 6.5 cm

AP = 2.8 cm

Required to Find: CA, AQ and that the area (\triangle ACB): area (\triangle APQ).



Since, $\triangle ACB \sim \triangle APQ$

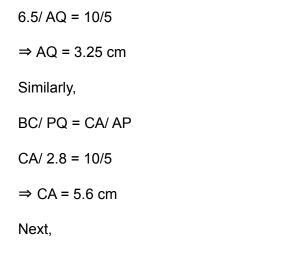
We know that,

AB/ AQ = BC/ PQ = AC/ AP [Corresponding Parts of Similar Triangles]

AB/AQ = BC/PQ







Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have,

 $ar(\Delta ACQ)$: $ar(\Delta APQ) = (BC/PQ)2$

= (10/5)2

= (2/1)2

= 4/1

Therefore, the ratio is 4:1.

3. The areas of two similar triangles are 81 cm² and 49 cm² respectively. Find the ration of their corresponding heights. What is the ratio of their corresponding medians?

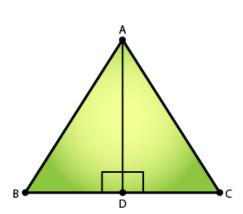
Solution:

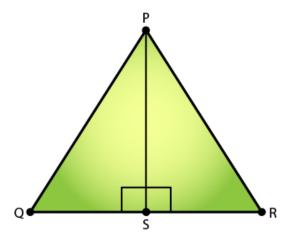
Given: The areas of two similar triangles are 81cm² and 49cm².

Required to find: The ratio of their corresponding heights and the ratio of their corresponding medians.



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Let's consider the two similar triangles as \triangle ABC and \triangle PQR, AD and PS be the altitudes of \triangle ABC and \triangle PQR respectively.

So.

By area of similar triangle theorem, we have

 $ar(\Delta ABC)/ar(\Delta PQR) = AB^2/PQ^2$

 \Rightarrow 81/49 = AB²/PQ²

 \Rightarrow 9/7 = AB/PQ

In ΔABD and ΔPQS

 $\angle B = \angle Q$ [Since $\triangle ABC \sim \triangle PQR$]

∠ABD **=** ∠PSQ = 90°

⇒ ΔABD ~ ΔPQS [By AA similarity]

Hence, as the corresponding parts of similar triangles are proportional, we have

AB/PQ = AD/PS

Therefore,





AD/PS = 9/7 (Ratio of altitudes)

Similarly,

The ratio of two similar triangles is equal to the ratio of the squares of their corresponding medians also.

Thus, ratio of altitudes = Ratio of medians = 9/7

4. The areas of two similar triangles are 169 cm² and 121 cm² respectively. If the longest side of the larger triangle is 26 cm, find the longest side of the smaller triangle.

Solution:

Given:

The area of two similar triangles is 169cm² and 121cm².

The longest side of the larger triangle is 26cm.

Required to find: the longest side of the smaller triangle

Let the longer side of the smaller triangle = x

We know that, the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have

ar(larger triangle)/ ar(smaller triangle) = (side of the larger triangle/ side of the smaller triangle)²

= 169/121

Taking square roots of LHS and RHS, we get

= 13/ 11

Since, sides of similar triangles are propositional, we can say

3/ 11 = (longer side of the larger triangle)/ (longer side of the smaller triangle)

 \Rightarrow 13/11 = 26/x

x = 22

Therefore, the longest side of the smaller triangle is 22 cm.





5. The area of two similar triangles are 25 cm² and 36cm² respectively. If the altitude of the first triangle is 2.4 cm, find the corresponding altitude of the other.

Solution:

Given: The area of two similar triangles are 25 cm² and 36cm² respectively, the altitude of the first triangle is 2.4 cm

Required to find: the altitude of the second triangle

We know that the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding altitudes, we have

 \Rightarrow ar(triangle1)/ar(triangle2) = (altitude1/ altitude2)²

 \Rightarrow 25/ 36 = (2.4)²/ (altitude2)²

Taking square roots of LHS and RHS, we get

5/6 = 2.4/ altitude2

 \Rightarrow altitude2 = (2.4 x 6)/5 = 2.88cm

Therefore, the altitude of the second triangle is 2.88cm.

6. The corresponding altitudes of two similar triangles are 6 cm and 9 cm respectively. Find the ratio of their areas.

Solution:

Given:

The corresponding altitudes of two similar triangles are 6 cm and 9 cm.

Required to find: Ratio of areas of the two similar triangles

We know that the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding altitudes, we have

 $ar(triangle1)/ar(triangle2) = (altitude1/ altitude2)^2 = (6/9)^2$

= 36/81

= 4/9





Therefore, the ratio of the areas of two triangles = 4: 9.

7. ABC is a triangle in which \angle A = 90°, AN \perp BC, BC = 12 cm and AC = 5 cm. Find the ratio of the areas of \triangle ANC and \triangle ABC.

Solution:

Given:

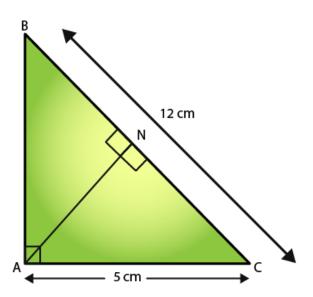
Given,

 \triangle ABC, \angle A = 90°, AN \perp BC

BC= 12 cm

AC = 5 cm.

Required to find: $ar(\Delta ANC)/ar(\Delta ABC)$.



We have,

In \triangle ANC and \triangle ABC,

 $\angle ACN = \angle ACB$ [Common]

 $\angle A = \angle ANC$ [each 90°]





 $\Rightarrow \Delta ANC \sim \Delta ABC$ [AA similarity]

Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we get have

 $ar(\Delta ANC)/ar(\Delta ABC) = (AC/BC)^2 = (5/12)^2 = 25/144$

Therefore, $ar(\Delta ANC)/ar(\Delta ABC) = 25:144$

8. In Fig 4.179, DE || BC

(i) If DE = 4m, BC = 6 cm and Area (\triangle ADE) = 16cm², find the area of \triangle ABC.

(ii) If DE = 4cm, BC = 8 cm and Area (\triangle ADE) = 25cm², find the area of \triangle ABC.

(iii) If DE: BC = 3: 5. Calculate the ratio of the areas of \triangle ADE and the trapezium BCED.

Solution:

Given,

DE // BC.

In ΔADE and ΔABC

We know that,

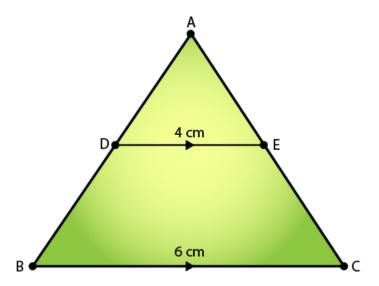
 $\angle ADE = \angle B$ [Corresponding angles]

 $\angle DAE = \angle BAC$ [Common]

Hence, \triangle ADE ~ \triangle ABC (AA Similarity)



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(i) Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have,

 $Ar(\Delta ADE)/Ar(\Delta ABC) = DE^2/BC^2$

$$16/Ar(\Delta ABC) = 4^2/6^2$$

$$\Rightarrow$$
 Ar(\triangle ABC) = (6² × 16)/ 4²

$$\Rightarrow$$
 Ar(\triangle ABC) = 36 cm²

(ii) Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have,

 $Ar(\Delta ADE)/Ar(\Delta ABC) = DE^2/BC^2$

$$25/Ar(\Delta ABC) = 4^2/8^2$$

$$\Rightarrow$$
 Ar(\triangle ABC) = (8² × 25)/4²

$$\Rightarrow$$
 Ar(\triangle ABC) = 100 cm²

(iii) According to the question,

$$Ar(\Delta ADE)/Ar(\Delta ABC) = DE^2/BC^2$$

$$Ar(\Delta ADE)/Ar(\Delta ABC) = 3^2/5^2$$





Ar(\triangle ADE)/ Ar(\triangle ABC) = 9/25 Assume that the area of \triangle ADE = 9x sq units And, area of \triangle ABC = 25x sq units So, Area of trapezium BCED = Area of \triangle ABC – Area of \triangle ADE = 25x – 9x = 16x

 $Ar(\Delta ADE)/Ar(trapBCED) = 9/16$

Now, $Ar(\Delta ADE)/Ar(trap BCED) = 9x/16x$

9. In \triangle ABC, D and E are the mid-points of AB and AC respectively. Find the ratio of the areas \triangle ADE and \triangle ABC.

Solution:

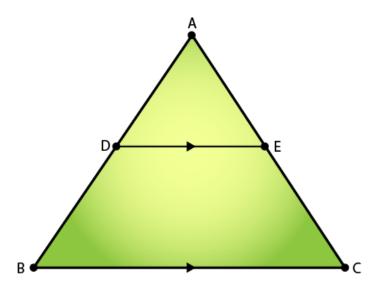
Given:

In ΔABC, D and E are the midpoints of AB and AC respectively.

Required to find: Ratio of the areas of \triangle ADE and \triangle ABC







Since, D and E are the midpoints of AB and AC respectively.

We can say,

DE || BC (By converse of mid-point theorem)

Also, DE = (1/2) BC

In \triangle ADE and \triangle ABC,

 \angle ADE = \angle B (Corresponding angles)

 $\angle DAE = \angle BAC$ (common)

Thus, $\triangle ADE \sim \triangle ABC$ (AA Similarity)

Now, we know that

The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides, so

 $Ar(\Delta ADE)/Ar(\Delta ABC) = AD^2/AB^2$

 $Ar(\Delta ADE)/Ar(\Delta ABC) = 1^2/2^2$

 $Ar(\Delta ADE)/Ar(\Delta ABC) = 1/4$





Therefore, the ratio of the areas \triangle ADE and \triangle ABC is 1:4

10. The areas of two similar triangles are 100 cm² and 49 cm² respectively. If the altitude of the bigger triangles is 5 cm, find the corresponding altitude of the other.

Solution:

Given: The area of the two similar triangles is 100cm² and 49cm². And the altitude of the bigger triangle is 5cm.

Required to find: The corresponding altitude of the other triangle

We know that,

The ratio of the areas of the two similar triangles is equal to the ratio of squares of their corresponding altitudes.

ar(bigger triangle)/ ar(smaller triangle) = (altitude of the bigger triangle/ altitude of the smaller triangle)²

 $(100/49) = (5/altitude of the smaller triangle)^2$

Taking square root on LHS and RHS, we get

(10/7) = (5/altitude of the smaller triangle) = 7/2

Therefore, altitude of the smaller triangle = 3.5cm

11. The areas of two similar triangles are 121 cm² and 64 cm² respectively. If the median of the first triangle is 12.1 cm, find the corresponding median of the other.

Solution:

Given: the area of the two triangles is 121cm² and 64cm² respectively and the median of the first triangle is 12.1cm

Required to find: the corresponding median of the other triangle

We know that,

The ratio of the areas of the two similar triangles are equal to the ratio of the squares of their medians.

ar(triangle1)/ ar(triangle2) = (median of triangle 1/median of triangle 2)²





 $121/64 = (12.1/ \text{ median of triangle } 2)^2$

Taking the square roots on both LHS and RHS, we have

11/8 = (12.1 / median of triangle 2) = (12.1 x 8) / 11

Therefore, Median of the other triangle = 8.8cm

Exercise 4.7 Page No: 4.119

1. If the sides of a triangle are 3 cm, 4 cm, and 6 cm long, determine whether the triangle is a right-angled triangle.

Solution:

We have,

Sides of triangle as

AB = 3 cm

BC = 4 cm

AC = 6 cm

On finding their squares, we get

$$AB^2 = 3^2 = 9$$

$$BC^2 = 4^2 = 16$$

$$AC^2 = 6^2 = 36$$

Since, $AB^2 + BC^2 \neq AC^2$

So, by converse of Pythagoras theorem the given sides cannot be the sides of a right triangle.

- 2. The sides of certain triangles are given below. Determine which of them are right triangles.
- (i) a = 7 cm, b = 24 cm and c = 25 cm
- (ii) a = 9 cm, b = 16 cm and c = 18 cm





(iii) a = 1.6 cm, b = 3.8 cm and c = 4 cm

(iv) a = 8 cm, b = 10 cm and c = 6 cm

Solutions:

(i) Given,

a = 7 cm, b = 24 cm and c = 25 cm

$$\therefore$$
 a² = 49. b² = 576 and c² = 625

Since,
$$a^2 + b^2 = 49 + 576 = 625 = c^2$$

Then, by converse of Pythagoras theorem

The given sides are of a right triangle.

(ii) Given,

a = 9 cm, b = 16 cm and c = 18 cm

$$\therefore$$
 a² = 81, b² = 256 and c² = 324

Since,
$$a^2 + b^2 = 81 + 256 = 337 \neq c^2$$

Then, by converse of Pythagoras theorem

The given sides cannot be of a right triangle.

(iii) Given,

a = 1.6 cm, b = 3.8 cm and C = 4 cm

$$\therefore$$
 a² = 2.56, b² = 14.44 and c² = 16

Since,
$$a^2 + b^2 = 2.56 + 14.44 = 17 \neq c^2$$

Then, by converse of Pythagoras theorem

The given sides cannot be of a right triangle.

(iv) Given,

$$a = 8 \text{ cm}, b = 10 \text{ cm} \text{ and } C = 6 \text{ cm}$$





$$\therefore$$
 a² = 64, b² = 100 and c² = 36

Since,
$$a^2 + c^2 = 64 + 36 = 100 = b^2$$

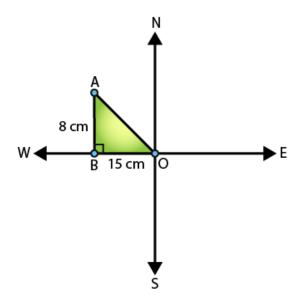
Then, by converse of Pythagoras theorem

The given sides are of a right triangle

3. A man goes 15 metres due west and then 8 metres due north. How far is he from the starting point?

Solution:

Let the starting point of the man be O and final point be A.



In ∆ABO,

by Pythagoras theorem $AO^2 = AB^2 + BO^2$

$$\Rightarrow$$
 AO² = 8² + 15²

$$\Rightarrow$$
 AO² = 64 + 225 = 289

$$\Rightarrow$$
 AO = $\sqrt{289}$ = 17m

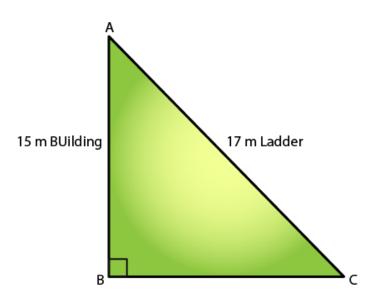
: the man is 17m far from the starting point.





4. A ladder 17 m long reaches a window of a building 15 m above the ground. Find the distance of the foot of the ladder from the building.

Solution:



In $\triangle ABC$, by Pythagoras theorem

$$AB^2 + BC^2 = AC^2$$

$$\Rightarrow$$
 15² + BC² = 17²

$$225 + BC^2 = 17^2$$

$$BC^2 = 289 - 225$$

$$BC^2 = 64$$

Therefore, the distance of the foot of the ladder from building = 8 m

5. Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between their feet is 12 m, find the distance between their tops.

Solution:

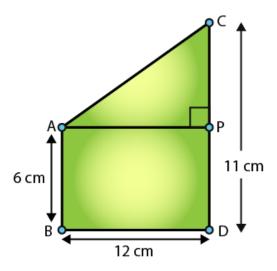
Let CD and AB be the poles of height 11m and 6m.





Then, its seen that CP = 11 - 6 = 5m.

From the figure, AP should be 12m (given)



In triangle APC, by applying Pythagoras theorem, we have

$$AP^2 + PC^2 = AC^2$$

$$12^2 + 5^2 = AC^2$$

$$AC^2 = 144 + 25 = 169$$

 \therefore AC = 13 (by taking sq. root on both sides)

Thus, the distance between their tops = 13 m.

6. In an isosceles triangle ABC, AB = AC = 25 cm, BC = 14 cm. Calculate the altitude from A on BC.

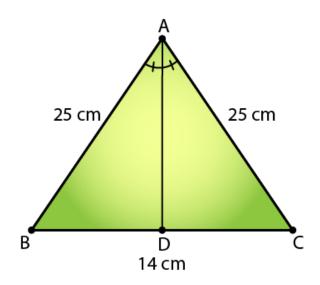
Solution:

Given,

 \triangle ABC, AB = AC = 25 cm and BC = 14.







In \triangle ABD and \triangle ACD, we see that

$$\angle ADB = \angle ADC$$
 [Each = 90°]

Then,
$$\triangle ABD \cong \triangle ACD$$
 [By RHS condition]

Finally,

In \triangle ADB, by Pythagoras theorem

$$AD^2 + BD^2 = AB^2$$

$$\Rightarrow$$
 AD² + 7² = 25²

$$AD^2 = 625 - 49 = 576$$

∴ AD =
$$\sqrt{576}$$
 = 24 cm

7. The foot of a ladder is 6 m away from a wall and its top reaches a window 8 m above the ground. If the ladder is shifted in such a way that its foot is 8 m away from the wall, to what height does its tip reach?





Solution:

Let's assume the length of ladder to be, AD = BE = x m

So, in \triangle ACD, by Pythagoras theorem

We have,

$$AD^2 = AC^2 + CD^2$$

$$\Rightarrow$$
 $x^2 = 8^2 + 6^2 ... (i)$

Also, in \triangle BCE, by Pythagoras theorem

$$BE^2 = BC^2 + CE^2$$

$$\Rightarrow$$
 $x^2 = BC^2 + 8^2 \dots (ii)$

Compare (i) and (ii)

$$BC^2 + 8^2 = 8^2 + 6^2$$

$$\Rightarrow$$
 BC² + 6²

$$\Rightarrow$$
 BC = 6 m

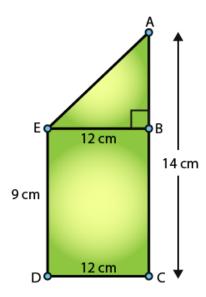
Therefore, the tip of the ladder reaches to a height od 6m.

8. Two poles of height 9 in and 14 m stand on a plane ground. If the distance between their feet is 12 m, find the distance between their tops.

Solution:







Comparing with the figure, it's given that

AC = 14 m, DC = 12m and ED = BC = 9 m

Construction: Draw EB ⊥ AC

Now,

It's seen that AB = AC - BC = (14 - 9) = 5 m

And, EB = DC = 12m [distance between their feet]

Thus,

In $\triangle ABE$, by Pythagoras theorem, we have

$$AE^2 = AB^2 + BE^2$$

$$AE^2 = 5^2 + 12^2$$

$$AE^2 = 25 + 144 = 169$$

$$\Rightarrow$$
 AE = $\sqrt{169}$ = 13 m

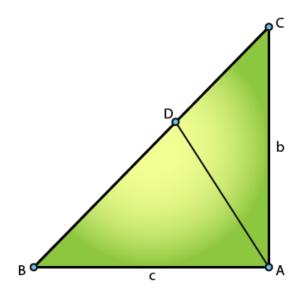
Therefore, the distance between their tops = 13 m





9. Using Pythagoras theorem determine the length of AD in terms of b and c shown in Fig. 4.219

Solution:



We have,

In \triangle BAC, by Pythagoras theorem, we have

$$BC^2 = AB^2 + AC^2$$

$$\Rightarrow$$
 BC² = c² + b²

$$\Rightarrow$$
 BC = $\sqrt{(c^2 + b^2)}$

In $\triangle ABD$ and $\triangle CBA$

$$\angle B = \angle B$$
 [Common]

$$\angle ADB = \angle BAC$$
 [Each 90°]

Then, $\triangle ABD \sim \triangle CBA$ [By AA similarity]

Thus,

AB/ CB = AD/ CA [Corresponding parts of similar triangles are proportional]





$$c/\sqrt{(c^2 + b^2)} = AD/b$$

$$\therefore AD = bc/\sqrt{(c^2 + b^2)}$$

10. A triangle has sides 5 cm, 12 cm and 13 cm. Find the length to one decimal place, of the perpendicular from the opposite vertex to the side whose length is 13 cm.

Solution:

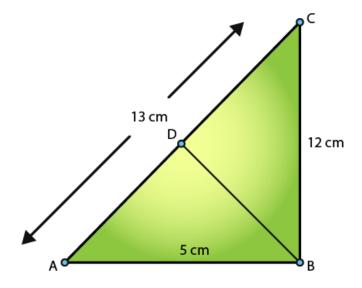
From the fig. AB = 5 cm, BC = 12 cm and AC = 13 cm.

Then,
$$AC^2 = AB^2 + BC^2$$
.

$$\Rightarrow$$
 (13)² = (5)² + (12)² = 25 + 144 = 169 = 13²

This proves that $\triangle ABC$ is a right triangle, right angled at B.

Let BD be the length of perpendicular from B on AC.



So, area of $\triangle ABC = (BC \times BA)/2$ [Taking BC as the altitude]

$$= (12 \times 5)/2$$

$$= 30 \text{ cm}^2$$

Also, area of $\triangle ABC = (AC \times BD)/2$ [Taking BD as the altitude]





$$= (13 \times BD)/2$$

$$\Rightarrow$$
 (13 x BD)/ 2 = 30

BD = 60/13 = 4.6 (to one decimal place)

11. ABCD is a square. F is the mid-point of AB. BE is one third of BC. If the area of \triangle FBE = 108cm², find the length of AC.

Solution:

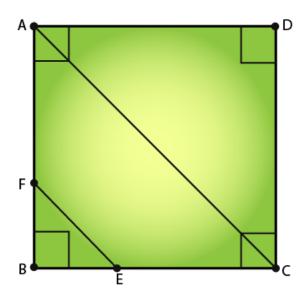
Given,

ABCD is a square. And, F is the mid-point of AB.

BE is one third of BC.

Area of \triangle FBE = 108cm²

Required to find: length of AC



Let's assume the sides of the square to be x.

$$\Rightarrow$$
 AB = BC = CD = DA = x cm

And, AF = FB = x/2 cm





So, BE = x/3 cm

Now, the area of \triangle FBE = 1/2 x BE x FB

$$\Rightarrow$$
 108 = (1/2) x (x/3) x (x/2)

$$\Rightarrow$$
 x² = 108 x 2 x 3 x 2 = 1296

 \Rightarrow x = $\sqrt{(1296)}$ [taking square roots of both the sides]

$$\therefore$$
 x = 36cm

Further in \triangle ABC, by Pythagoras theorem, we have

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow$$
 AC² = $x^2 + x^2 = 2x^2$

$$\Rightarrow$$
 AC² = 2 x (36)²

$$\Rightarrow$$
 AC = $36\sqrt{2}$ = 36×1.414 = 50.904 cm

Therefore, the length of AC is 50.904 cm.

12. In an isosceles triangle ABC, if AB = AC = 13cm and the altitude from A on BC is 5cm, find BC.

Solution:

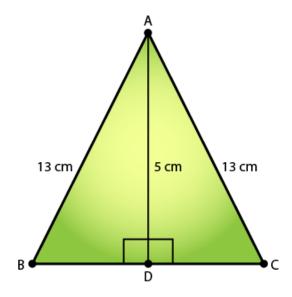
Given,

An isosceles triangle ABC, AB = AC = 13cm, AD = 5cm

Required to find: BC







In Δ ADB, by using Pythagoras theorem, we have

$$AD^2 + BD^2 = 13^2$$

$$5^2 + BD^2 = 169$$

$$BD^2 = 169 - 25 = 144$$

$$\Rightarrow$$
BD = $\sqrt{144}$ = 12 cm

Similarly, applying Pythagoras theorem is \triangle ADC we can have,

$$AC^2 = AD^2 + DC^2$$

$$13^2 = 5^2 + DC^2$$

$$\Rightarrow$$
 DC = $\sqrt{144}$ = 12 cm

Thus,
$$BC = BD + DC = 12 + 12 = 24 \text{ cm}$$

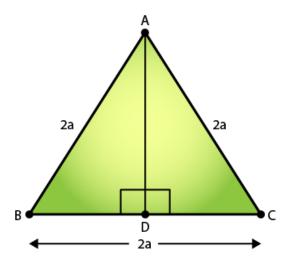
13. In a \triangle ABC, AB = BC = CA = 2a and AD \perp BC. Prove that

(i) AD =
$$a\sqrt{3}$$
 (ii) Area (\triangle ABC) = $\sqrt{3}$ a^2

Solution:



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(i) In \triangle ABD and \triangle ACD, we have

$$\angle ADB = \angle ADC = 90^{\circ}$$

AD = AD [Common]

So, $\triangle ABD \cong \triangle ACD$ [By RHS condition]

Hence, BD = CD = a [By C.P.C.T]

Now, in $\triangle ABD$, by Pythagoras theorem

$$AD^2 + BD^2 = AB^2$$

$$AD^2 + a^2 = 2a^2$$

$$AD^2 = 4a^2 - a^2 = 3a^2$$

$$AD = a\sqrt{3}$$

(ii) Area (
$$\triangle$$
ABC) = 1/2 x BC x AD

$$= 1/2 \times (2a) \times (a\sqrt{3})$$

$$= \sqrt{3} a^2$$



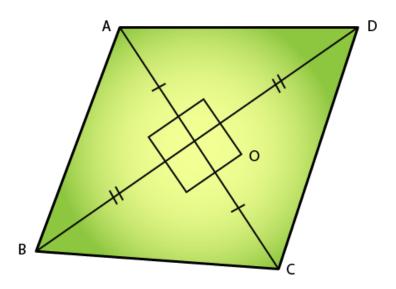


14. The lengths of the diagonals of a rhombus is 24cm and 10cm. Find each side of the rhombus.

Solution:

Let ABCD be a rhombus and AC and BD be the diagonals of ABCD.

So, AC = 24cm and BD = 10cm



We know that diagonals of a rhombus bisect each other at right angle. (Perpendicular to each other)

So,

$$AO = OC = 12cm$$
 and $BO = OD = 3cm$

In \triangle AOB, by Pythagoras theorem, we have

$$AB^2 = AO^2 + BO^2$$

$$= 12^2 + 5^2$$

$$= 144 + 25$$

$$\Rightarrow$$
 AB = $\sqrt{169}$ = 13cm





Since, the sides of rhombus are all equal.

Therefore, AB = BC = CD = AD = 13cm.







Chapterwise RD Sharma Solutions for Class 10 Maths:

- Chapter 1–Real Numbers
- Chapter 2-Polynomials
- Chapter 3-Pair of Linear Equations In Two Variables
- <u>Chapter 4–Triangles</u>
- <u>Chapter 5–Trigonometric Ratios</u>
- Chapter 6-Trigonometric Identities
- <u>Chapter 7–Statistics</u>
- Chapter 8-Quadratic Equations
- Chapter 9-Arithmetic Progressions
- Chapter 10-Circles
- <u>Chapter 11–Constructions</u>
- Chapter 12—Some Applications of Trigonometry
- Chapter 13-Probability
- <u>Chapter 14–Co-ordinate Geometry</u>
- <u>Chapter 15–Areas Related To Circles</u>
- Chapter 16-Surface Areas And Volumes





About RD Sharma

RD Sharma isn't the kind of author you'd bump into at lit fests. But his bestselling books have helped many CBSE students lose their dread of maths. Sunday Times profiles the tutor turned internet star

He dreams of algorithms that would give most people nightmares. And, spends every waking hour thinking of ways to explain concepts like 'series solution of linear differential equations'. Meet Dr Ravi Dutt Sharma — mathematics teacher and author of 25 reference books — whose name evokes as much awe as the subject he teaches. And though students have used his thick tomes for the last 31 years to ace the dreaded maths exam, it's only recently that a spoof video turned the tutor into a YouTube star.

R D Sharma had a good laugh but said he shared little with his on-screen persona except for the love for maths. "I like to spend all my time thinking and writing about maths problems. I find it relaxing," he says. When he is not writing books explaining mathematical concepts for classes 6 to 12 and engineering students, Sharma is busy dispensing his duty as vice-principal and head of department of science and humanities at Delhi government's Guru Nanak Dev Institute of Technology.

