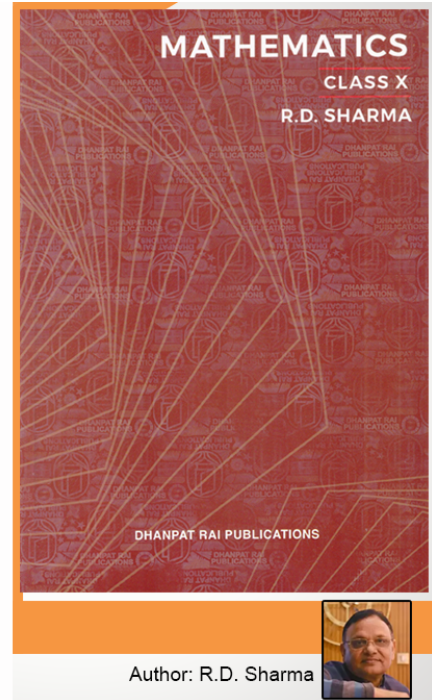


# Class 10 - Chapter 10 Circles



## RD Sharma Solutions for Class 10 Maths Chapter 10–Circles

Class 10: Maths Chapter 10 solutions. Complete Class 10 Maths Chapter 10 Notes.

### RD Sharma Solutions for Class 10 Maths Chapter 10–Circles

RD Sharma 10th Maths Chapter 10, Class 10 Maths Chapter 10 solutions

Exercise 10.1 Page No: 10.5

1. Fill in the blanks:

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- (i) The common point of tangent and the circle is called \_\_\_\_\_.
- (ii) A circle may have \_\_\_\_\_ parallel tangents.
- (iii) A tangent to a circle intersects it in \_\_\_\_\_ point.
- (iv) A line intersecting a circle in two points is called a \_\_\_\_\_
- (v) The angle between tangent at a point P on circle and radius through the point is \_\_\_\_\_

**Solution:**

- (i) The common point of tangent and the circle is called point of contact.
- (ii) A circle may have two parallel tangents.
- (iii) A tangent to a circle intersects it in one point.
- (iv) A line intersecting a circle in two points is called a secant.
- (v) The angle between tangent at a point P on circle and radius through the point is  $90^\circ$  .

**2. How many tangents can a circle have?**

**Solution:**

A tangent is defined as a line intersecting the circle in one point. Since, there are infinite number of points on the circle, a circle can have many (infinite) tangents.

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**Exercise 10.2 Page No: 10.33**

**1. If PT is a tangent at T to a circle whose centre is O and  $OP = 17$  cm,  $OT = 8$  cm. Find the length of the tangent segment PT.**

**Solution:**

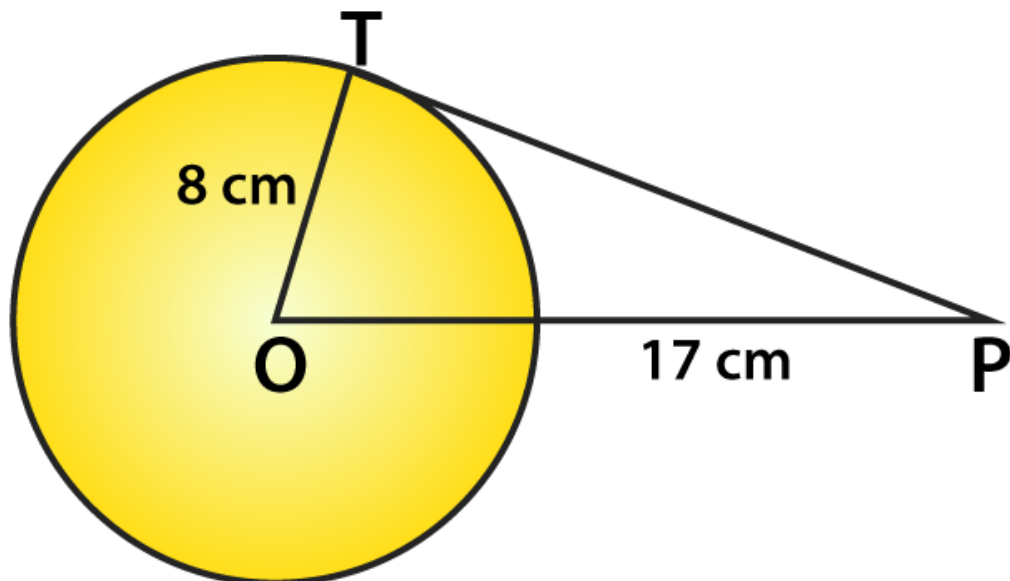
Given,

$OT = \text{radius} = 8$  cm

$OP = 17$  cm

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To find:  $PT = \text{length of tangent} = ?$



Clearly, T is point of contact. And, we know that at point of contact tangent and radius are perpendicular.

$\therefore$  OTP is right angled triangle  $\angle OTP = 90^\circ$ , from Pythagoras theorem  $OT^2 + PT^2 = OP^2$

$$8^2 + PT^2 = 17^2$$

$$8^2 + PT^2 = 17^2$$

$$PT = \sqrt{17^2 - 8^2}$$

$$= \sqrt{289 - 64}$$

$$= \sqrt{225}$$

$\therefore$   $PT = \text{length of tangent} = 15 \text{ cm.}$

**2. Find the length of a tangent drawn to a circle with radius 5cm, from a point 13 cm from the center of the circle.**

**Solution:**

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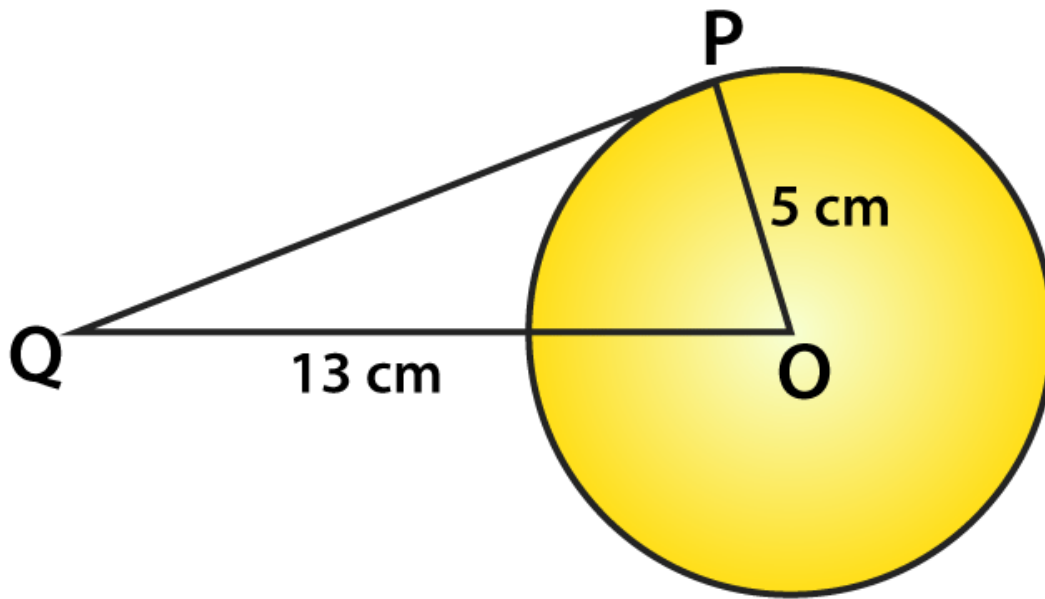
Consider a circle with centre O.

OP = radius = 5 cm. (given)

A tangent is drawn at point P, such that line through O intersects it at Q.

And, OQ = 13cm (given).

To find: Length of tangent PQ =?



We know that tangent and radius are perpendicular to each other.

$\triangle OPQ$  is right angled triangle with  $\angle OPQ = 90^\circ$

By Pythagoras theorem we have,

$$OQ^2 = OP^2 + PQ^2$$

$$\Rightarrow 13^2 = 5^2 + PQ^2$$

$$\Rightarrow PQ^2 = 169 - 25 = 144$$

$$\Rightarrow PQ = \sqrt{144}$$

$$= 12 \text{ cm}$$

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Therefore, the length of tangent = 12 cm

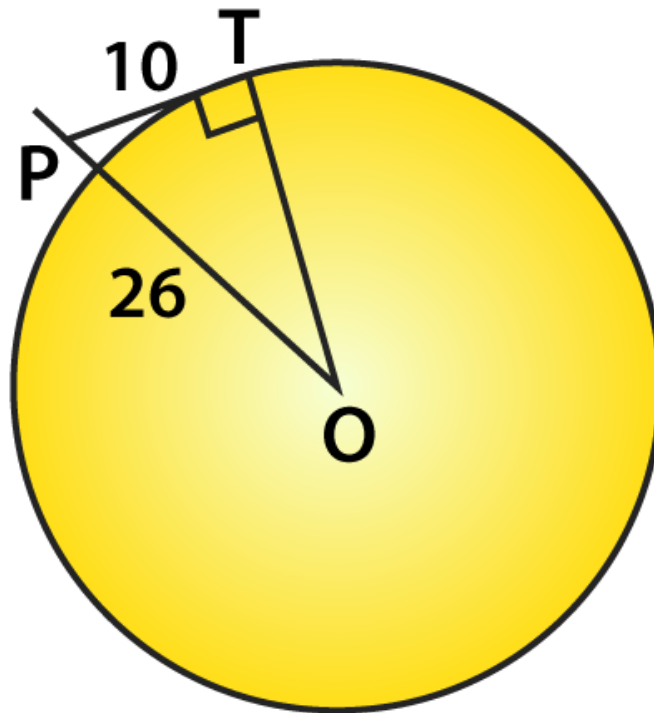
**3. A point P is 26 cm away from O of circle and the length PT of the tangent drawn from P to the circle is 10 cm. Find the radius of the circle.**

**Solution:**

Given,  $OP = 26$  cm

$PT =$  length of tangent = 10 cm

To find: radius =  $OT = ?$



We know that,

At point of contact, radius and tangent are perpendicular  $\angle OTP = 90^\circ$

So,  $\triangle OTP$  is right angled triangle.

Then by Pythagoras theorem, we have

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$$OP^2 = OT^2 + PT^2$$

$$26^2 = OT^2 + 10^2$$

$$OT^2 = 676 - 100$$

$$OT = \sqrt{576}$$

$$OT = 24 \text{ cm}$$

Thus,  $OT = \text{length of tangent} = 24 \text{ cm}$

**4. If from any point on the common chord of two intersecting circles, tangents be drawn to the circles, prove that they are equal.**

**Solution:**

Let the two circles intersect at points X and Y.

So, XY is the common chord.

Suppose 'A' is a point on the common chord and AM and AN be the tangents drawn from A to the circle

Then it's required to prove that  $AM = AN$ .

In order to prove the above relation, following property has to be used.

“Let PT be a tangent to the circle from an external point P and a secant to the circle through P intersecting the circle at points A and B, then  $PT^2 = PA \times PB$ ”

Now AM is the tangent and AXY is a secant

$$\therefore AM^2 = AX \times AY \dots (i)$$

Similarly, AN is a tangent and AXY is a secant

$$\therefore AN^2 = AX \times AY \dots (ii)$$

From (i) & (ii), we have  $AM^2 = AN^2$

$$\therefore AM = AN$$

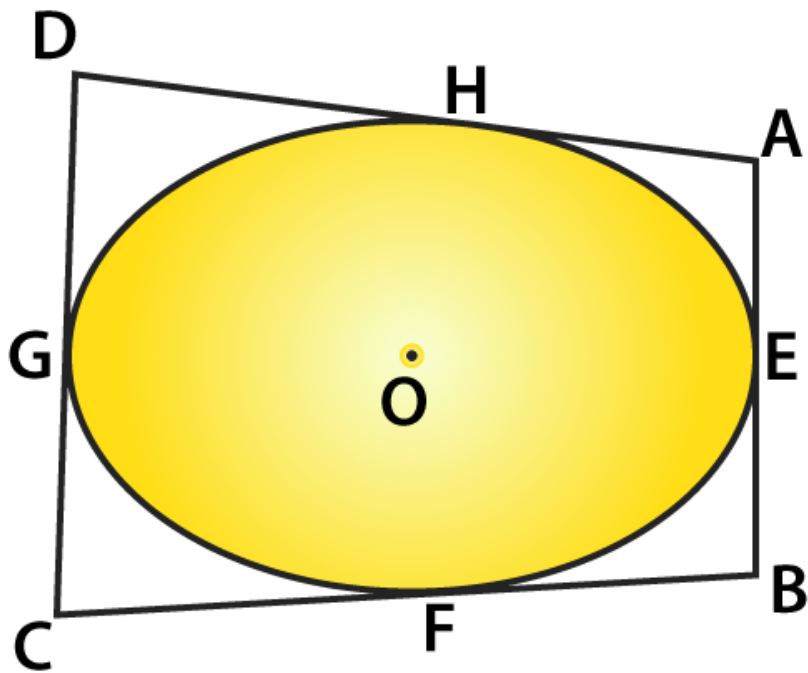
Therefore, tangents drawn from any point on the common chord of two intersecting circles are equal.

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Hence Proved

**5. If the quadrilateral sides touch the circle, prove that sum of pair of opposite sides is equal to the sum of other pair.**

**Solution:**



Consider a quadrilateral ABCD touching circle with centre O at points E, F, G and H as shown in figure.

We know that,

The tangents drawn from same external points to the circle are equal in length.

Consider tangents:

1. From point A [AH & AE]

$$AH = AE \dots (i)$$

2. From point B [EB & BF]

$$BF = EB \dots (ii)$$

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3. From point C [CF & GC]

$$FC = CG \dots \text{(iii)}$$

4. From point D [DG & DH]

$$DH = DG \dots \text{(iv)}$$

Adding (i), (ii), (iii), & (iv)

$$(AH + BF + FC + DH) = [(AE + EB) + (CG + DG)]$$

$$\Rightarrow (AH + DH) + (BF + FC) = (AE + EB) + (CG + DG)$$

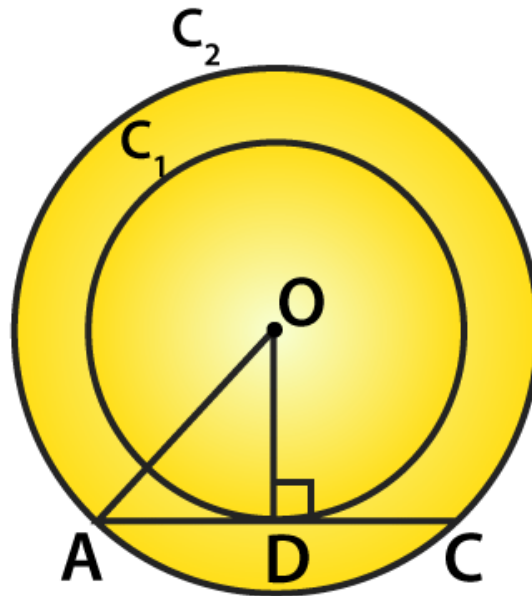
$$\Rightarrow AD + BC = AB + DC \text{ [from fig.]}$$

Therefore, the sum of one pair of opposite sides is equal to other.

Hence Proved

**6. Out of the two concentric circles, the radius of the outer circle is 5 cm and the chord AC of length 8 cm is a tangent to the inner circle. Find the radius of the inner circle.**

**Solution:**



Let  $C_1$  and  $C_2$  be the two circles having same center  $O$ .

And,  $AC$  is a chord which touches the  $C_1$  at point  $D$

let's join  $OD$ .

So,  $OD \perp AC$

$AD = DC = 4$  cm [perpendicular line  $OD$  bisects the chord]

Thus, in right angled  $\triangle AOD$ ,

$OA^2 = AD^2 + DO^2$  [By Pythagoras theorem]

$$DO^2 = 5^2 - 4^2 = 25 - 16 = 9$$

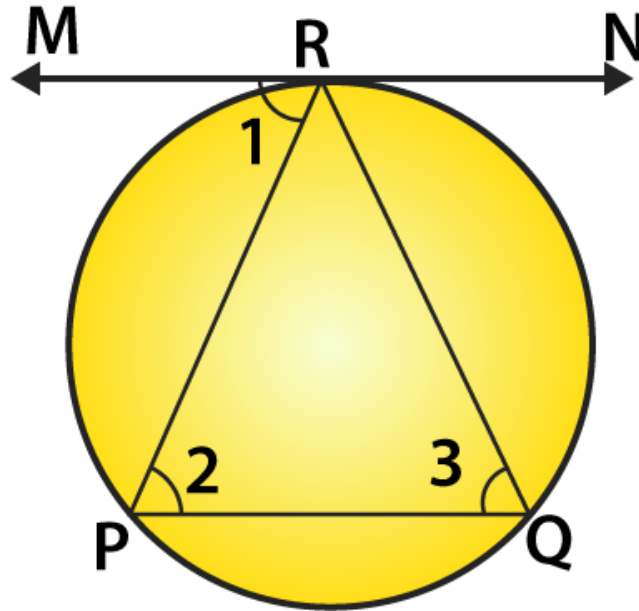
$$DO = 3 \text{ cm}$$

Therefore, the radius of the inner circle  $OD = 3$  cm.

**7. A chord  $PQ$  of a circle is parallel to the tangent drawn at a point  $R$  of the circle. Prove that  $R$  bisects the arc  $PRQ$ .**

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**Solution:**



Given: Chord PQ is parallel to tangent at R.

To prove: R bisects the arc PRQ.

Proof:

Since  $PQ \parallel$  tangent at R.

$\angle 1 = \angle 2$  [alternate interior angles]

$\angle 1 = \angle 3$  [angle between tangent and chord is equal to angle made by chord in alternate segment]

So,  $\angle 2 = \angle 3$

$\Rightarrow PR = QR$  [sides opposite to equal angles are equal]

Hence, clearly R bisects the arc PRQ.

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8. Prove that a diameter AB of a circle bisects all those chords which are parallel to the tangent at the point A.

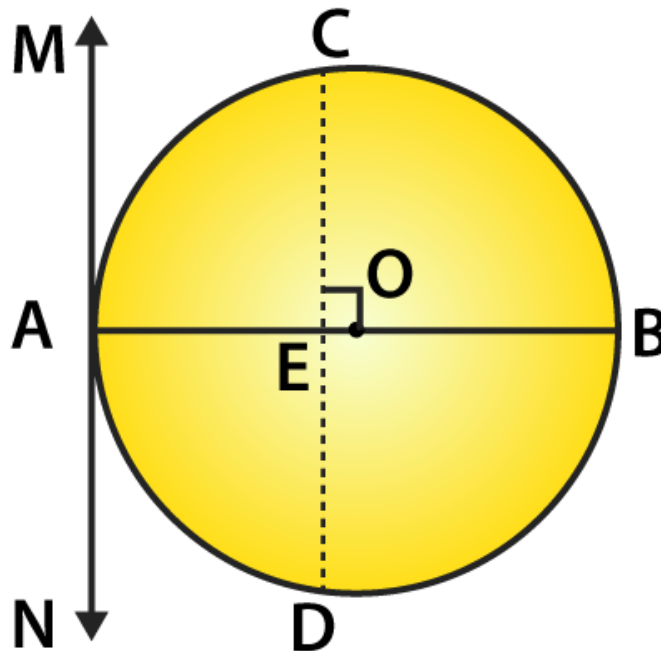
**Solution:**

Given,

AB is a diameter of the circle.

A tangent is drawn from point A.

Construction: Draw a chord CD parallel to the tangent MAN.



So now, CD is a chord of the circle and OA is a radius of the circle.

$\angle MAO = 90^\circ$  [Tangent at any point of a circle is perpendicular to the radius through the point of contact]

$\angle CEO = \angle MAO$  [corresponding angles]

$\angle CEO = 90^\circ$

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Therefore, OE bisects CD. [perpendicular from center of circle to chord bisects the chord]

Similarly, the diameter AB bisects all the chords which are parallel to the tangent at the point A.

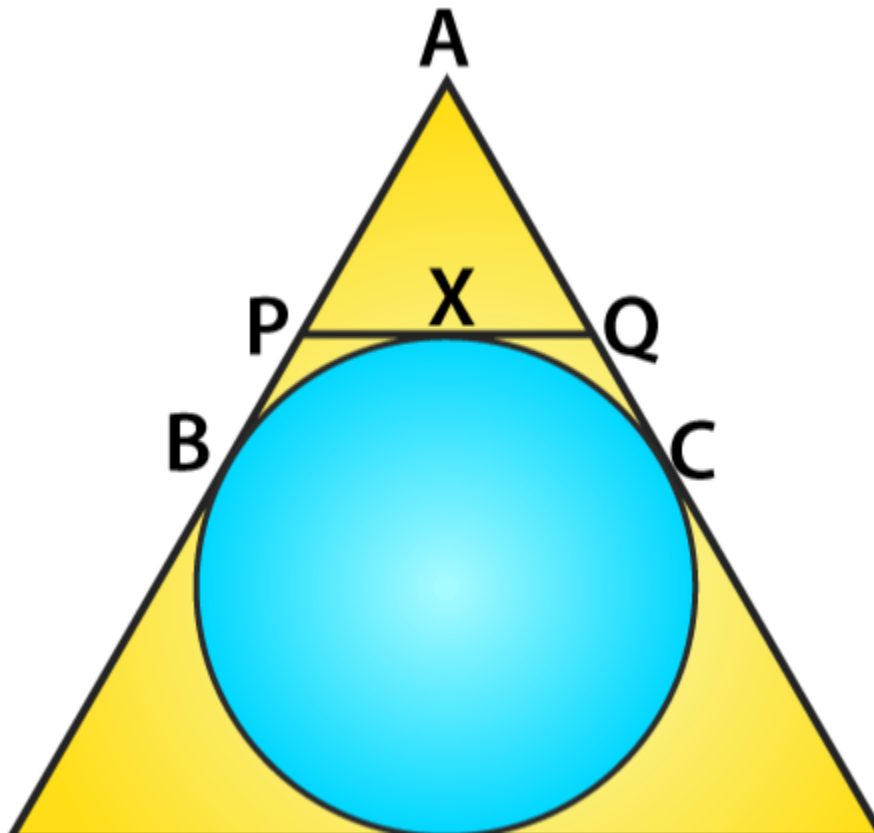
**9. If AB, AC, PQ are the tangents in the figure, and AB = 5 cm, find the perimeter of  $\triangle APQ$ .**

**Solution:**

Given,

AB, AC, PQ are tangents

And, AB = 5 cm



Perimeter of  $\triangle APQ$ ,

$$\text{Perimeter} = AP + AQ + PQ$$

$$= AP + AQ + (PX + QX)$$

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We know that,

The two tangents drawn from external point to the circle are equal in length from point A,

So,  $AB = AC = 5$  cm

From point P,  $PX = PB$  [Tangents from an external point to the circle are equal.]

From point Q,  $QX = QC$  [Tangents from an external point to the circle are equal.]

Thus,

Perimeter (P) =  $AP + AQ + (PB + QC)$

=  $(AP + PB) + (AQ + QC)$

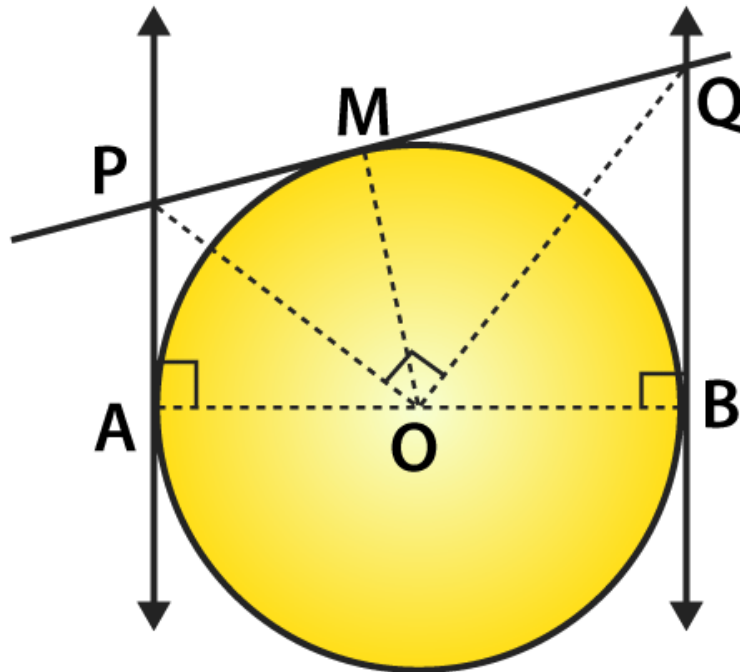
=  $AB + AC = 5 + 5$

= 10 cm.

**10. Prove that the intercept of a tangent between two parallel tangents to a circle subtends a right angle at centre.**

**Solution:**

Consider a circle with centre 'O' and has two parallel tangents through A & B at ends of diameter.



Let tangent through M intersect the parallel tangents at P and Q

Then, required to prove:  $\angle POQ = 90^\circ$ .

From fig. it is clear that ABQP is a quadrilateral

$$\angle A + \angle B = 90^\circ + 90^\circ = 180^\circ \text{ [At point of contact tangent \& radius are perpendicular]}$$

$$\angle A + \angle B + \angle P + \angle Q = 360^\circ \text{ [Angle sum property of a quadrilateral]}$$

So,

$$\angle P + \angle Q = 360^\circ - 180^\circ = 180^\circ \dots (i)$$

At P & Q

$$\angle APO = \angle OPQ = 1/2 \angle P \dots (ii)$$

$$\angle BQO = \angle PQO = 1/2 \angle Q \dots (iii)$$

Using (ii) and (iii) in (i)  $\Rightarrow$

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$$2\angle OPQ + 2\angle PQQ = 180^\circ$$

$$\angle OPQ + \angle PQQ = 90^\circ \dots \text{(iv)}$$

In  $\triangle OPQ$ ,

$$\angle OPQ + \angle PQQ + \angle POQ = 180^\circ \text{ [Angle sum property]}$$

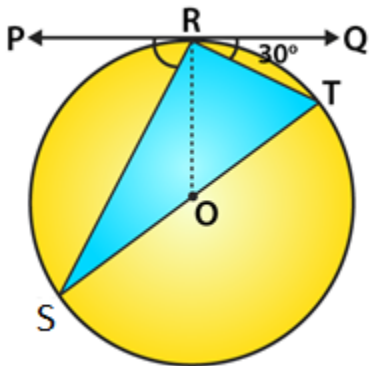
$$90^\circ + \angle POQ = 180^\circ \quad \text{[from (iv)]}$$

$$\angle POQ = 180^\circ - 90^\circ = 90^\circ$$

Hence,  $\angle POQ = 90^\circ$

**11. In Fig below, PQ is tangent at point R of the circle with center O. If  $\angle TRQ = 30^\circ$ , find  $\angle PRS$ .**

**Solution:**



Given,

$$\angle TRQ = 30^\circ.$$

At point R,  $OR \perp RQ$ .

$$\text{So, } \angle ORQ = 90^\circ$$

$$\Rightarrow \angle TRQ + \angle ORT = 90^\circ$$

$$\Rightarrow \angle ORT = 90^\circ - 30^\circ = 60^\circ$$

It's seen that, ST is diameter,

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So,  $\angle SRT = 90^\circ$  [  $\because$  Angle in semicircle =  $90^\circ$  ]

Then,

$$\angle ORT + \angle SRO = 90^\circ$$

$$\angle SRO + \angle PRS = 90^\circ$$

$$\therefore \angle PRS = 90^\circ - 30^\circ = 60^\circ$$

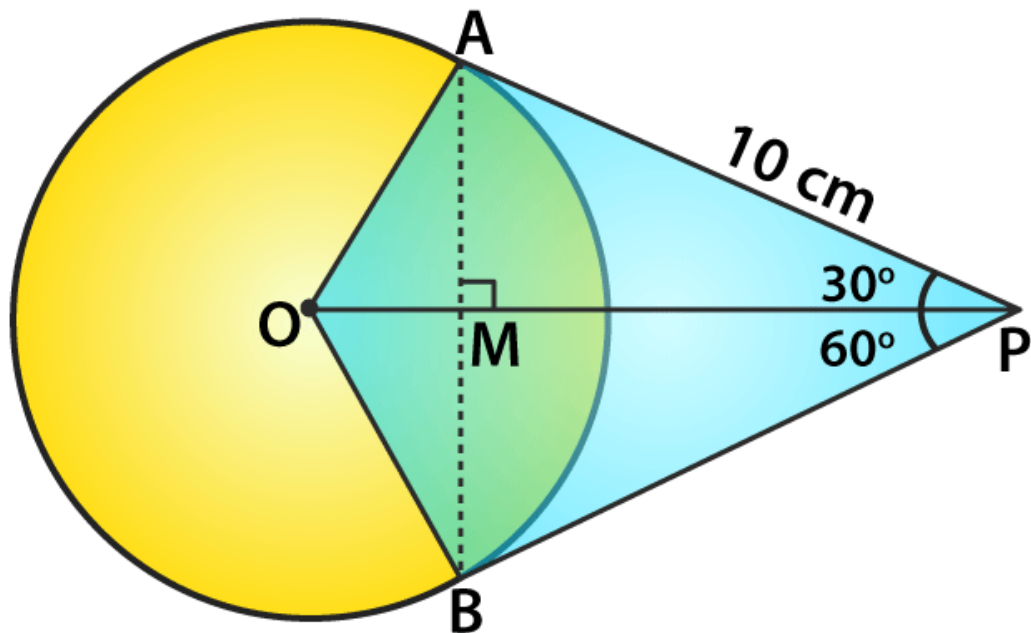
**12. If PA and PB are tangents from an outside point P. such that PA = 10 cm and  $\angle APB = 60^\circ$ . Find the length of chord AB.**

**Solution:**

Given,

$$AP = 10 \text{ cm and } \angle APB = 60^\circ$$

Represented in the figure



We know that,

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A line drawn from centre to point from where external tangents are drawn divides or bisects the angle made by tangents at that point

$$\text{So, } \angle APO = \angle OPB = 1/2 \times 60^\circ = 30^\circ$$

And, the chord AB will be bisected perpendicularly

$$\therefore AB = 2AM$$

In  $\triangle AMP$ ,

$$\sin 30^\circ = \frac{\text{opp. side}}{\text{hypotenuse}} = \frac{AM}{AP}$$

$$AM = AP \sin 30^\circ$$

$$AP/2 = 10/2 = 5\text{cm [As } AB = 2AM]$$

$$\text{So, } AP = 2 AM = 10 \text{ cm}$$

$$\text{And, } AB = 2 AM = 10\text{cm}$$

Alternate method:

$$\text{In } \triangle AMP, \angle AMP = 90^\circ, \angle APM = 30^\circ$$

$$\angle AMP + \angle APM + \angle MAP = 180^\circ$$

$$90^\circ + 30^\circ + \angle MAP = 180^\circ$$

$$\angle MAP = 60^\circ$$

$$\text{In } \triangle PAB, \angle MAP = \angle BAP = 60^\circ, \angle APB = 60^\circ$$

$$\text{We also get, } \angle PBA = 60^\circ$$

$\therefore \triangle PAB$  is equilateral triangle

$$AB = AP = 10 \text{ cm}$$

**13. In a right triangle ABC in which  $\angle B = 90^\circ$ , a circle is drawn with AB as diameter intersecting the hypotenuse AC at P. Prove that the tangent to the circle at P bisects BC.**

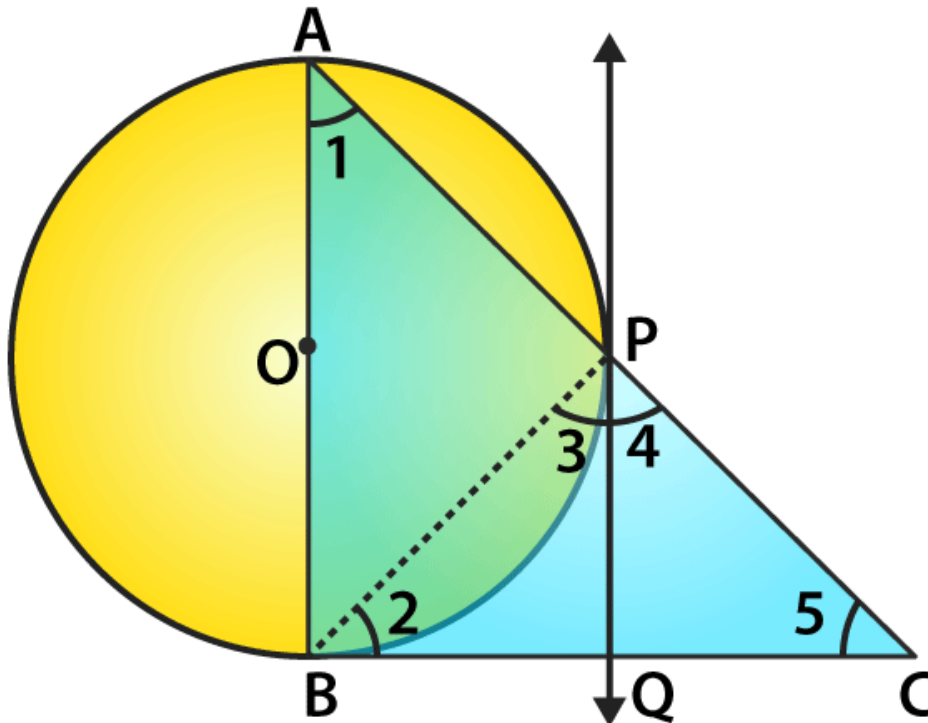
**Solution:**

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Let O be the center of the given circle. Suppose, the tangent at P meets BC at Q.

Then join BP.

Required to prove:  $BQ = QC$



Proof :

$\angle ABC = 90^\circ$  [tangent at any point of circle is perpendicular to radius through the point of contact]

In  $\triangle ABC$ ,  $\angle 1 + \angle 5 = 90^\circ$  [angle sum property,  $\angle ABC = 90^\circ$ ]

And,  $\angle 3 = \angle 1$  [angle between tangent and the chord equals angle made by the chord in alternate segment]

So,

$$\angle 3 + \angle 5 = 90^\circ \dots\dots(i)$$

Also,  $\angle APB = 90^\circ$  [angle in semi-circle]

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$$\angle 3 + \angle 4 = 90^\circ \dots\dots(ii) [\angle APB + \angle BPC = 180^\circ, \text{ linear pair}]$$

From (i) and (ii), we get

$$\angle 3 + \angle 5 = \angle 3 + \angle 4$$

$$\angle 5 = \angle 4$$

$\Rightarrow PQ = QC$  [sides opposite to equal angles are equal]

Also,  $QP = QB$  [tangents drawn from an internal point to a circle are equal]

$$\Rightarrow QB = QC$$

– Hence proved.

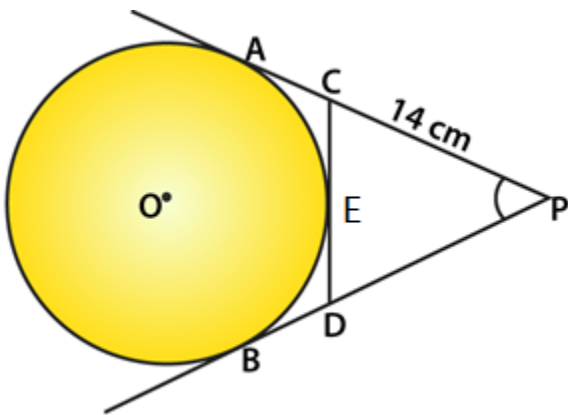
**14. From an external point P, tangents PA and PB are drawn to a circle with centre O. If CD is the tangent to the circle at a point E and PA = 14 cm, find the perimeter of  $\triangle PCD$ .**

**Solution:**

Given,

PA and PB are the tangents drawn from a point P outside the circle with centre O.

CD is another tangents to the circle at point E which intersects PA and PB at C and D respectively.



$$PA = 14 \text{ cm}$$

PA and PB are the tangents to the circle from P

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So,  $PA = PB = 14$  cm

Now,  $CA$  and  $CE$  are the tangents from  $C$  to the circle.

$$CA = CE \dots(i)$$

Similarly,  $DB$  and  $DE$  are the tangents from  $D$  to the circle.

$$DB = DE \dots(ii)$$

Now, perimeter of  $\triangle PCD$

$$= PC + PD + CD$$

$$= PC + PD + CE + DE$$

$$= PC + CE + PD + DE$$

$$= PC + CA + PD + DB \text{ \{From (i) and (ii)\}}$$

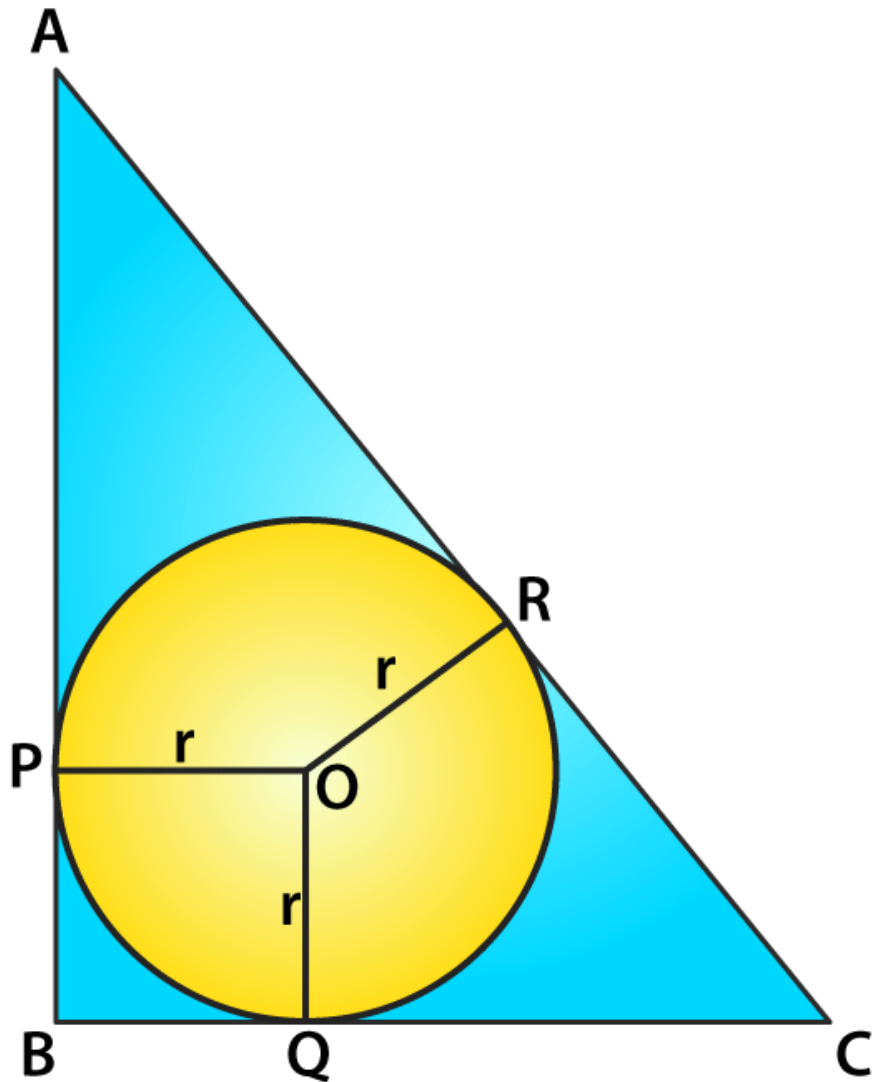
$$= PA + PB$$

$$= 14 + 14$$

$$= 28 \text{ cm}$$

**15. In the figure,  $ABC$  is a right triangle right-angled at  $B$  such that  $BC = 6$  cm and  $AB = 8$  cm. Find the radius of its incircle.**

**Solution:**



Given,

In right  $\triangle ABC$ ,  $\angle B = 90^\circ$

And,  $BC = 6$  cm,  $AB = 8$  cm

Let  $r$  be the radius of incircle whose centre is  $O$  and touches the sides  $AB$ ,  $BC$  and  $CA$  at  $P$ ,  $Q$  and  $R$  respectively.

Since,  $AP$  and  $AR$  are the tangents to the circle  $AP = AR$

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Similarly,  $CR = CQ$  and  $BQ = BP$

$OP$  and  $OQ$  are radii of the circle

$OP \perp AB$  and  $OQ \perp BC$  and  $\angle B = 90^\circ$  (given)

Hence,  $BPOQ$  is a square

Thus,  $BP = BQ = r$  (sides of a square are equal)

So,

$$AR = AP = AB - PB = 8 - r$$

$$\text{and } CR = CQ = BC - BQ = 6 - r$$

But  $AC^2 = AB^2 + BC^2$  (By Pythagoras Theorem)

$$= (8)^2 + (6)^2 = 64 + 36 = 100 = (10)^2$$

So,  $AC = 10$  cm

$$\Rightarrow AR + CR = 10$$

$$\Rightarrow 8 - r + 6 - r = 10$$

$$\Rightarrow 14 - 2r = 10$$

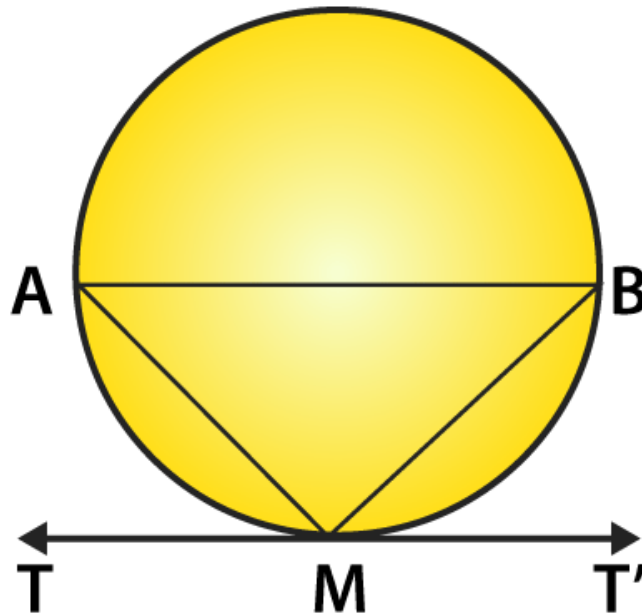
$$\Rightarrow 2r = 14 - 10 = 4$$

$$\Rightarrow r = 2$$

Therefore, the radius of the incircle = 2 cm

**16. Prove that the tangent drawn at the mid-point of an arc of a circle is parallel to the chord joining the end points of the arc. u**

**Solution:**



Let mid-point of an arc  $AMB$  be  $M$  and  $TMT'$  be the tangent to the circle.

Now, join  $AB$ ,  $AM$  and  $MB$ .

Since, arc  $AM =$  arc  $MB$

$\Rightarrow$  Chord  $AM =$  Chord  $MB$

In  $\triangle AMB$ ,  $AM = MB$

$\Rightarrow \angle MAB = \angle MBA \dots\dots(i)$  [equal sides corresponding to the equal angle]

Since,  $TMT'$  is a tangent line.

$\angle AMT = \angle MBA$  [angles in alternate segment are equal]

Thus,  $\angle AMT = \angle MAB$  [from Eq. (i)]

But  $\angle AMT$  and  $\angle MAB$  are alternate angles, which is possible only when  $AB \parallel TMT'$

Hence, the tangent drawn at the mid-point of an arc of a circle is parallel to the chord joining the end points of the arc.

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– Hence proved

**17. From a point P, two tangents PA and PB are drawn to a circle with centre O. If OP = diameter of the circle, show that  $\triangle APB$  is equilateral.**

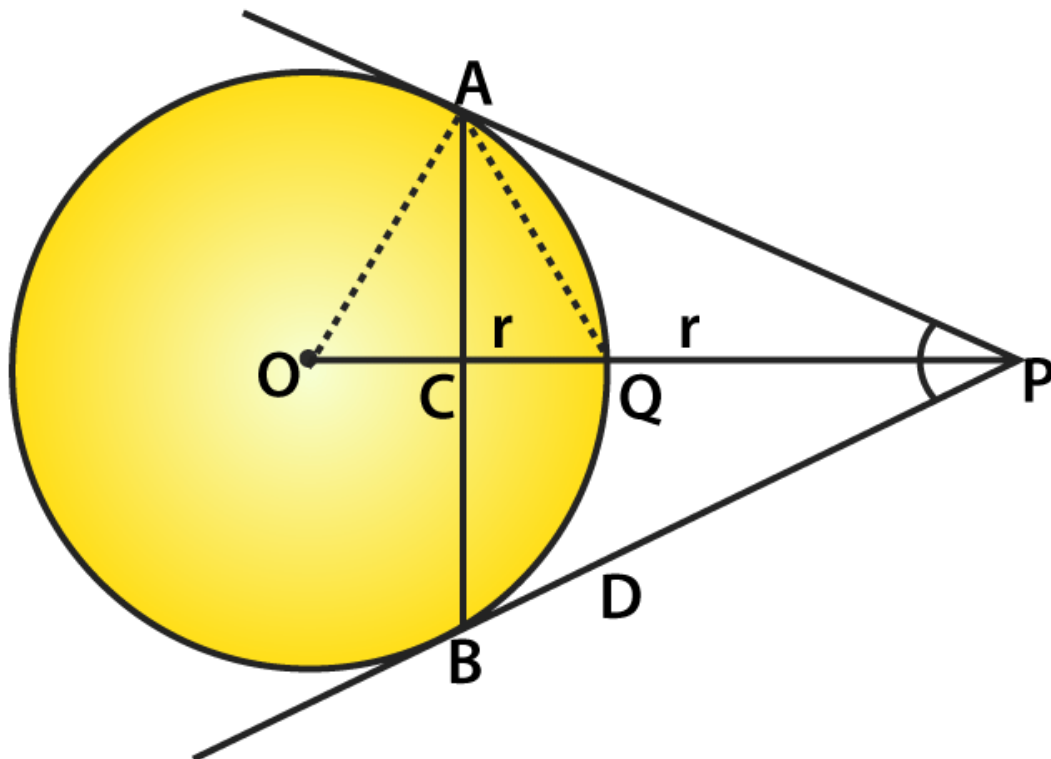
**Solution:**

Given: From a point P outside the circle with centre O, PA and PB are the tangents to the circle such that OP is diameter.

And, AB is joined.

Required to prove: APB is an equilateral triangle

Construction: Join OP, AQ, OA



Proof:

We know that,  $OP = 2r$

$\Rightarrow OQ + QP = 2r$

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$$\Rightarrow OQ = QP = r$$

Now in right  $\triangle OAP$ ,

OP is its hypotenuse and Q is its mid-point

$$\text{Then, } OA = AQ = OQ$$

(mid-point of hypotenuse of a right triangle is equidistance from its vertices)

Thus,  $\triangle OAQ$  is equilateral triangle. So,  $\angle AOQ = 60^\circ$

Now in right  $\triangle OAP$ ,

$$\angle APO = 90^\circ - 60^\circ = 30^\circ$$

$$\Rightarrow \angle APB = 2 \angle APO = 2 \times 30^\circ = 60^\circ$$

But  $PA = PB$  (Tangents from P to the circle)

$$\Rightarrow \angle PAB = \angle PBA = 60^\circ$$

Hence  $\triangle APB$  is an equilateral triangle.

**18. Two tangents segments PA and PB are drawn to a circle with centre O such that  $\angle APB = 120^\circ$ . Prove that  $OP = 2 AP$ .**

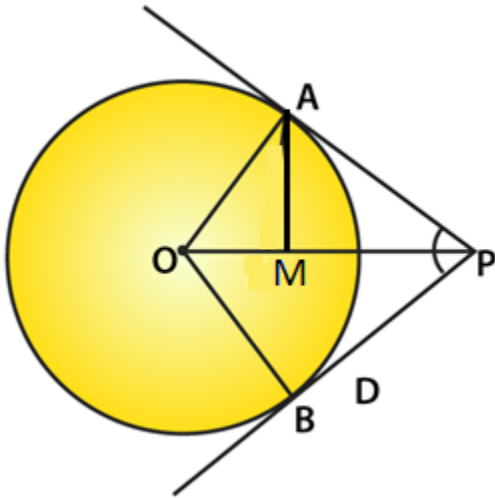
**Solution:**

Given: From a point P. Outside the circle with centre O, PA and PB are tangents drawn and  $\angle APB = 120^\circ$

And, OP is joined.

Required to prove:  $OP = 2 AP$

Construction: Take mid-point M of OP and join AM, join also OA and OB.



Proof:

In right  $\triangle OAP$ ,

$$\angle OPA = \frac{1}{2} \angle APB = \frac{1}{2} (120^\circ) = 60^\circ$$

$$\angle AOP = 90^\circ - 60^\circ = 30^\circ \text{ [Angle sum property]}$$

M is mid-point of hypotenuse OP of  $\triangle OAP$  [from construction]

So,  $MO = MA = MP$

$$\angle OAM = \angle AOM = 30^\circ \text{ and } \angle PAM = 90^\circ - 30^\circ = 60^\circ$$

Thus,  $\triangle AMP$  is an equilateral triangle

$$MA = MP = AP$$

But, M is mid-point of OP

So,

$$OP = 2 MP = 2 AP$$

– Hence proved.

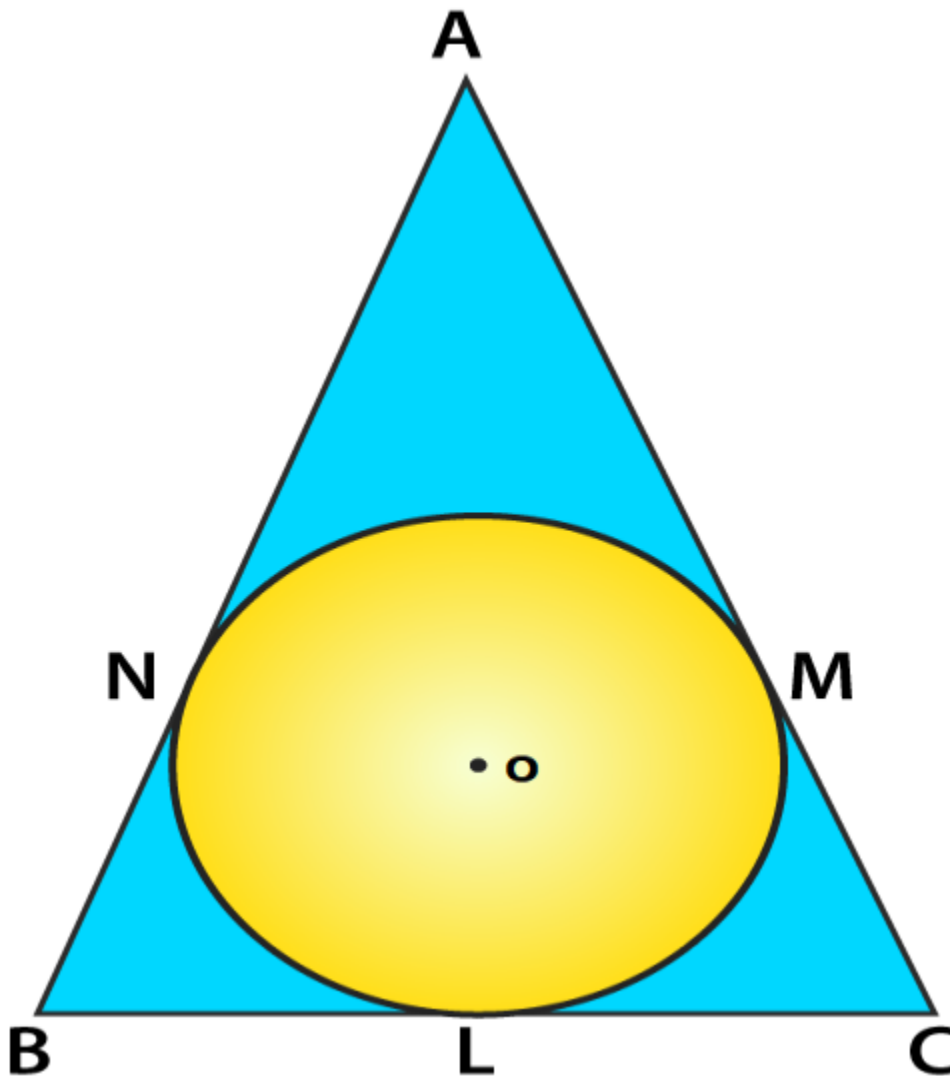
**19. If  $\triangle ABC$  is isosceles with  $AB = AC$  and  $C(0, r)$  is the incircle of the  $\triangle ABC$  touching  $BC$  at  $L$ . Prove that  $L$  bisects  $BC$ .**

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**Solution:**

Given: In  $\triangle ABC$ ,  $AB = AC$  and a circle with centre  $O$  and radius  $r$  touches the side  $BC$  of  $\triangle ABC$  at  $L$ .

Required to prove :  $L$  is mid-point of  $BC$ .



Proof :

$AM$  and  $AN$  are the tangents to the circle from  $A$ .

So,  $AM = AN$

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But  $AB = AC$  (given)

$$AB - AN = AC - AM$$

$$\Rightarrow BN = CM$$

Now  $BL$  and  $BN$  are the tangents from  $B$

$$\text{So, } BL = BN$$

Similarly,  $CL$  and  $CM$  are tangents

$$CL = CM$$

But  $BN = CM$  (proved above)

$$\text{So, } BL = CL$$

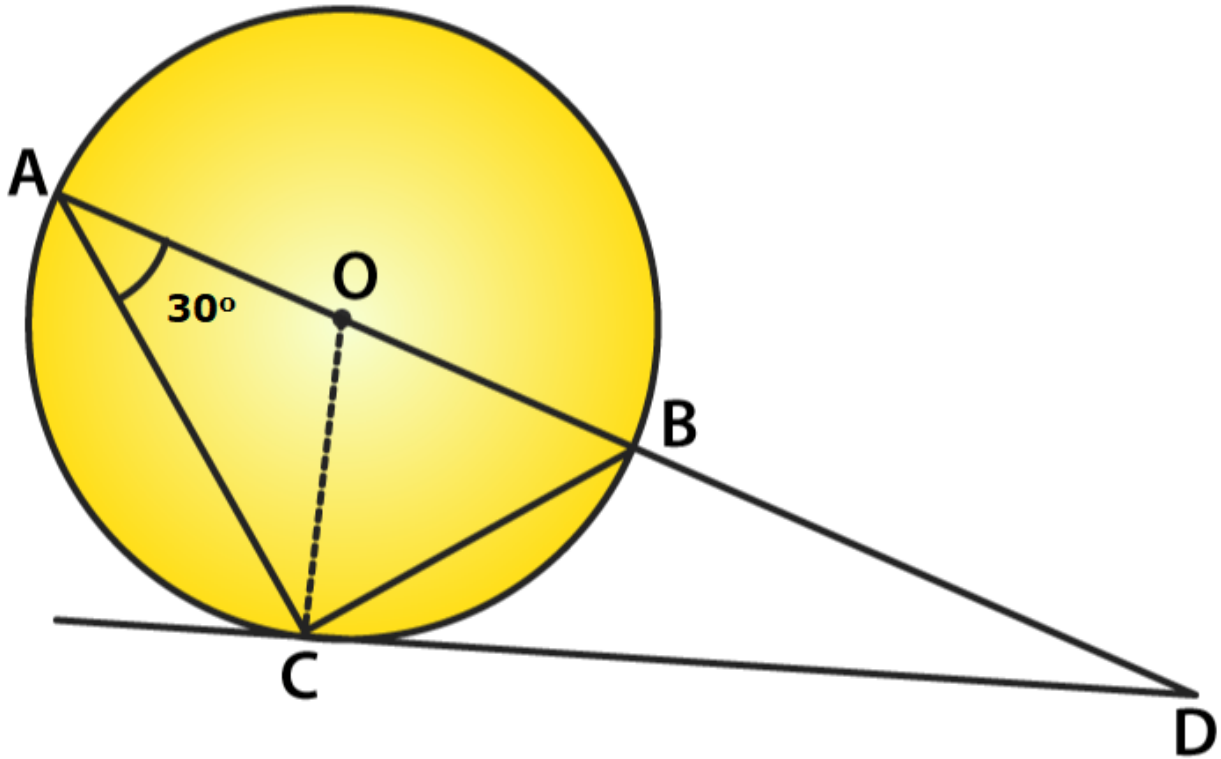
Therefore,  $L$  is mid-point of  $BC$ .

**20.  $AB$  is a diameter and  $AC$  is a chord of a circle with centre  $O$  such that  $\angle BAC = 30^\circ$ . The tangent at  $C$  intersects  $AB$  at a point  $D$ . Prove that  $BC = BD$ . [NCERT Exemplar]**

**Solution:**

Required to prove:  $BC = BD$

Join  $BC$  and  $OC$ .



Given,  $\angle BAC = 30^\circ$

$\Rightarrow \angle BCD = 30^\circ$  [angle between tangent and chord is equal to angle made by chord in the alternate segment]

$$\angle ACD = \angle ACO + \angle OCD$$

$$\angle ACD = 30^\circ + 90^\circ = 120^\circ \text{ [OC} \perp \text{CD and OA = OC = radius} \Rightarrow \angle OAC = \angle OCA = 30^\circ \text{]}$$

In  $\triangle ACD$ ,

$$\angle CAD + \angle ACD + \angle ADC = 180^\circ \text{ [Angle sum property of a triangle]}$$

$$\Rightarrow 30^\circ + 120^\circ + \angle ADC = 180^\circ$$

$$\Rightarrow \angle ADC = 180^\circ - 30^\circ - 120^\circ = 30^\circ$$

Now, in  $\triangle BCD$ ,

$$\angle BCD = \angle BDC = 30^\circ$$

$\Rightarrow BC = BD$  [As sides opposite to equal angles are equal]

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Hence Proved

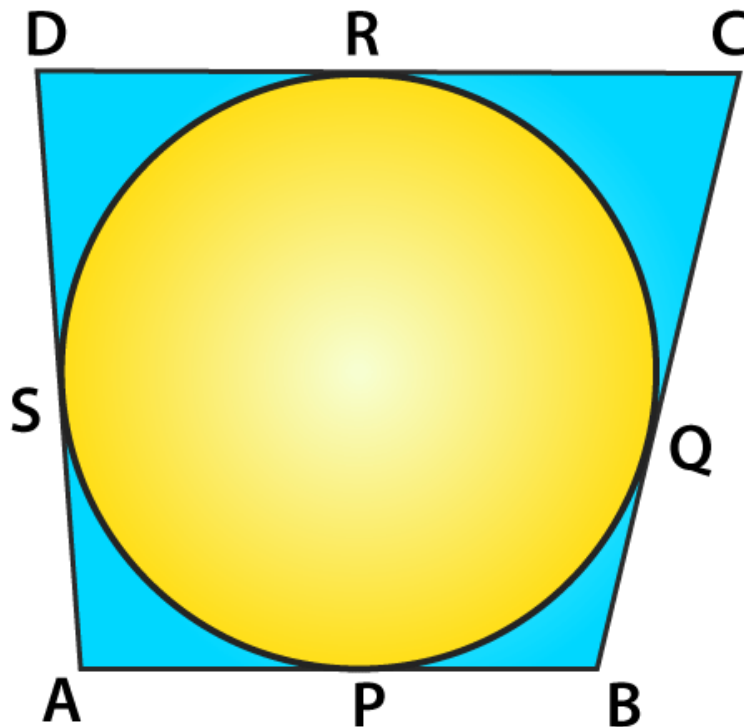
21. In the figure, a circle touches all the four sides of a quadrilateral ABCD with  $AB = 6$  cm,  $BC = 7$  cm, and  $CD = 4$  cm. Find AD.

**Solution:**

Given,

A circle touches the sides AB, BC, CD and DA of a quadrilateral ABCD at P, Q, R and S respectively.

$AB = 6$  cm,  $BC = 7$  cm,  $CD = 4$  cm



Let  $AD = x$

As AP and AS are the tangents to the circle

$AP = AS$

Similarly,

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$$BP = BQ$$

$$CQ = CR$$

$$\text{and } DR = DS$$

So, In ABCD

$$AB + CD = AD + BC \text{ (Property of a cyclic quadrilateral)}$$

$$\Rightarrow 6 + 4 = 7 + x$$

$$\Rightarrow 10 = 7 + x$$

$$\Rightarrow x = 10 - 7 = 3$$

Therefore,  $AD = 3 \text{ cm}$ .

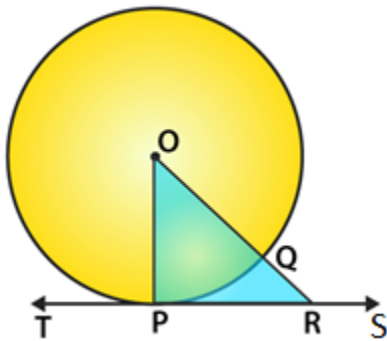
**22. Prove that the perpendicular at the point of contact to the tangent to a circle passes through the centre of the circle.**

**Solution:**

Given: TS is a tangent to the circle with centre O at P, and OP is joined.

Required to prove: OP is perpendicular to TS which passes through the centre of the circle

Construction: Draw a line OR which intersect the circle at Q and meets the tangent TS at R



Proof:

$$OP = OQ \text{ (radii of the same circle)}$$

$$\text{And } OQ < OR$$

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$\Rightarrow OP < OR$

similarly, we can prove that  $OP$  is less than all lines which can be drawn from  $O$  to  $TS$ .

$OP$  is the shortest

$OP$  is perpendicular to  $TS$

Therefore, the perpendicular through  $P$  will pass through the centre of the circle

– Hence proved.

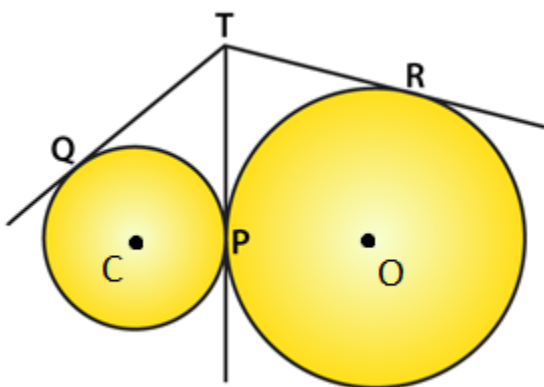
**23. Two circles touch externally at a point  $P$ . From a point  $T$  on the tangent at  $P$ , tangents  $TQ$  and  $TR$  are drawn to the circles with points of contact  $Q$  and  $R$  respectively. Prove that  $TQ = TR$ .**

**Solution:**

Given: Two circles with centres  $O$  and  $C$  touch each other externally at  $P$ .  $PT$  is its common tangent

From a point  $T$ :  $PT$ ,  $TR$  and  $TQ$  are the tangents drawn to the circles.

Required to prove:  $TQ = TR$



Proof:

From  $T$ ,  $TR$  and  $TP$  are two tangents to the circle with centre  $O$

So,  $TR = TP$  ....(i)

Similarly, from point  $T$

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TQ and TP are two tangents to the circle with centre C

$$TQ = TP \dots(ii)$$

From (i) and (ii)  $\Rightarrow$

$$TQ = TR$$

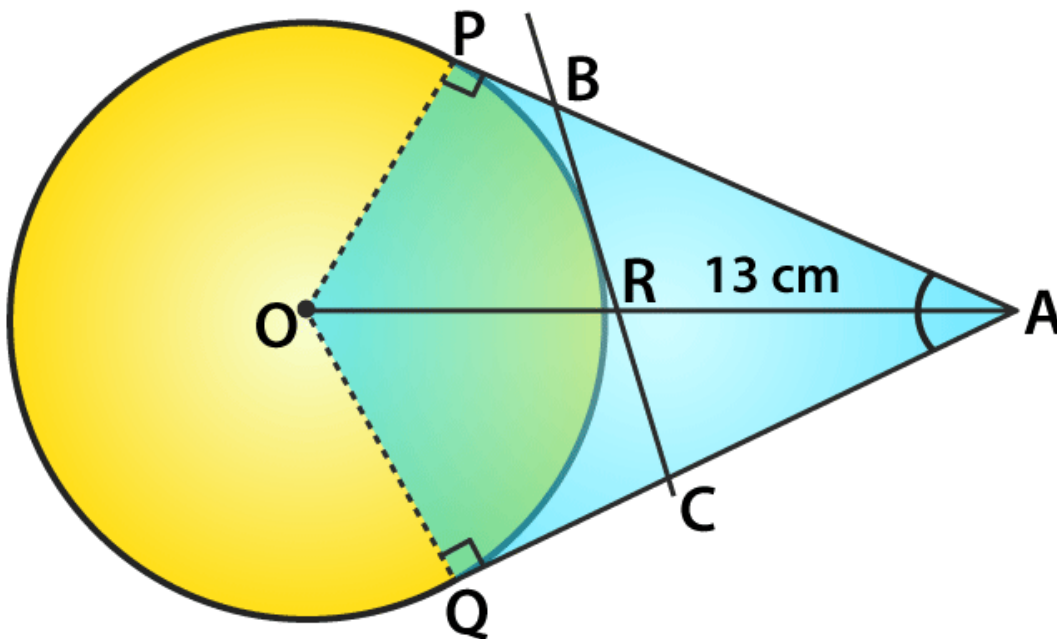
– Hence proved.

**24. A is a point at a distance 13 cm from the centre O of a circle of radius 5 cm. AP and AQ are the tangents to the circle at P and Q. If a tangent BC is drawn at a point R lying on the minor arc PQ to intersect AP at B and AQ at C, find the perimeter of the  $\triangle ABC$ .**

**Solution:**

Given: Two tangents are drawn from an external point A to the circle with centre O. Tangent BC is drawn at a point R and radius of circle = 5 cm.

Required to find : Perimeter of  $\triangle ABC$ .



Proof:

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We know that,

$\angle OPA = 90^\circ$  [Tangent at any point of a circle is perpendicular to the radius through the point of contact]

$$OA^2 = OP^2 + PA^2 \text{ [by Pythagoras Theorem]}$$

$$(13)^2 = 5^2 + PA^2$$

$$\Rightarrow PA^2 = 144 = 12^2$$

$$\Rightarrow PA = 12 \text{ cm}$$

Now, perimeter of  $\triangle ABC = AB + BC + CA = (AB + BR) + (RC + CA)$

$= AB + BP + CQ + CA$  [BR = BP, RC = CQ tangents from internal point to a circle are equal]

$= AP + AQ = 2AP = 2 \times (12) = 24 \text{ cm}$  [AP = AQ tangent from internal point to a circle are equal]

Therefore, the perimeter of  $\triangle ABC = 24 \text{ cm}$ .



# Chapterwise RD Sharma Solutions for Class 10 Maths :

- Chapter 1–Real Numbers
- Chapter 2–Polynomials
- Chapter 3–Pair of Linear Equations In Two Variables
- Chapter 4–Triangles
- Chapter 5–Trigonometric Ratios
- Chapter 6–Trigonometric Identities
- Chapter 7–Statistics
- Chapter 8–Quadratic Equations
- Chapter 9–Arithmetic Progressions
- Chapter 10–Circles
- Chapter 11–Constructions
- Chapter 12–Some Applications of Trigonometry
- Chapter 13–Probability
- Chapter 14–Co-ordinate Geometry
- Chapter 15–Areas Related To Circles
- Chapter 16–Surface Areas And Volumes

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# About RD Sharma

*RD Sharma isn't the kind of author you'd bump into at lit fests. But his bestselling books have helped many CBSE students lose their dread of maths. Sunday Times profiles the tutor turned internet star*

He dreams of algorithms that would give most people nightmares. And, spends every waking hour thinking of ways to explain concepts like 'series solution of linear differential equations'. Meet Dr Ravi Dutt Sharma — mathematics teacher and author of 25 reference books — whose name evokes as much awe as the subject he teaches. And though students have used his thick tomes for the last 31 years to ace the dreaded maths exam, it's only recently that a spoof video turned the tutor into a YouTube star.

R D Sharma had a good laugh but said he shared little with his on-screen persona except for the love for maths. "I like to spend all my time thinking and writing about maths problems. I find it relaxing," he says. When he is not writing books explaining mathematical concepts for classes 6 to 12 and engineering students, Sharma is busy dispensing his duty as vice-principal and head of department of science and humanities at Delhi government's Guru Nanak Dev Institute of Technology.

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