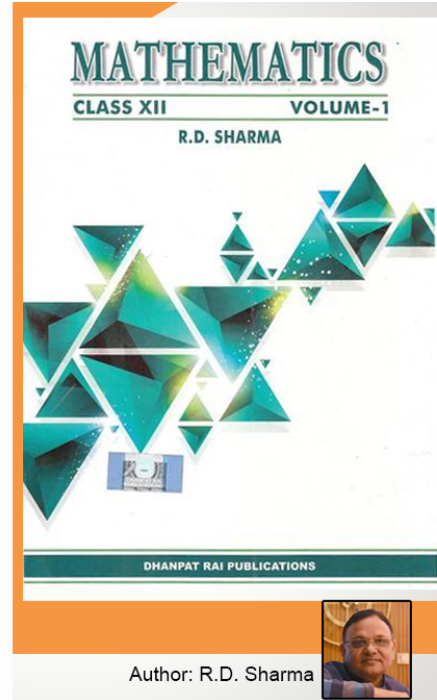


Class 12 - Chapter 5 Algebra of Matrices



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Exercise 5.1 Page No: 5.6

1. If a matrix has 8 elements, what are the possible orders it can have? What if it has 5 elements?

Solution:

If a matrix is of order $m \times n$ elements, it has $m \times n$ elements. So, if the matrix has 8 elements, we will find the ordered pairs m and n .

$$m \times n = 8$$

Then, ordered pairs m and n will be

$$m \times n \text{ be } (8 \times 1), (1 \times 8), (4 \times 2), (2 \times 4)$$

Now, if it has 5 elements

Possible orders are (5×1) , (1×5) .

$$2. \text{ If } A = [a_{ij}] = \begin{bmatrix} 2 & 3 & -5 \\ 1 & 4 & 9 \\ 0 & 7 & -2 \end{bmatrix} \text{ and } B = [b_{ij}] = \begin{bmatrix} 2 & -1 \\ -3 & 4 \\ 1 & 2 \end{bmatrix} \text{ then find}$$

$$(i) a_{22} + b_{21}$$

$$(ii) a_{11} b_{11} + a_{22} b_{22}$$

Solution:

(i)

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We know that

$$A = [a_{ij}] = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \dots (i)$$

$$\text{And } B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \\ b_{31} & b_{32} \end{bmatrix} \dots (ii)$$

Also given that

$$A = [a_{ij}] = \begin{bmatrix} 2 & 3 & -5 \\ 1 & 4 & 9 \\ 0 & 7 & -2 \end{bmatrix} \text{ and } B = [b_{ij}] = \begin{bmatrix} 2 & -1 \\ -3 & 4 \\ 1 & 2 \end{bmatrix}$$

Now, Comparing with equation (1) and (2)

$$a_{22} = 4 \text{ and } b_{21} = -3$$

$$a_{22} + b_{21} = 4 + (-3) = 1$$

(ii)

We know that

$$A = [a_{ij}] = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \dots (i)$$

$$\text{And } B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \\ b_{31} & b_{32} \end{bmatrix} \dots (ii)$$

Also given that

$$A = [a_{ij}] = \begin{bmatrix} 2 & 3 & -5 \\ 1 & 4 & 9 \\ 0 & 7 & -2 \end{bmatrix} \text{ and } B = [b_{ij}] = \begin{bmatrix} 2 & -1 \\ -3 & 4 \\ 1 & 2 \end{bmatrix}$$

Now, Comparing with equation (1) and (2)

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$$a_{11} = 2, a_{22} = 4, b_{11} = 2, b_{22} = 4$$

$$a_{11} b_{11} + a_{22} b_{22} = 2 \times 2 + 4 \times 4 = 4 + 16 = 20$$

3. Let A be a matrix of order 3×4 . If R_1 denotes the first row of A and C_2 denotes its second column, then determine the orders of matrices R_1 and C_2 .

Solution:

Given A be a matrix of order 3×4 .

$$\text{So, } A = [a_{ij}]_{3 \times 4}$$

$$R_1 = \text{first row of } A = [a_{11}, a_{12}, a_{13}, a_{14}]$$

$$\text{So, order of matrix } R_1 = 1 \times 4$$

C_2 = second column of

$$A = \begin{bmatrix} a_{12} \\ a_{22} \\ a_{32} \end{bmatrix}$$

Therefore order of $C_2 = 3 \times 1$

4. Construct a 2×3 matrix $A = [a_{ij}]$ whose elements a_{ij} are given by:

(i) $a_{ij} = i \times j$

(ii) $a_{ij} = 2i - j$

(iii) $a_{ij} = i + j$

(iv) $a_{ij} = (i + j)^2/2$

Solution:

(i) Given $a_{ij} = i \times j$

$$\text{Let } A = [a_{ij}]_{2 \times 3}$$

So, the elements in a 2×3 matrix are $[a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}]$

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$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$$a_{11} = 1 \times 1 = 1$$

$$a_{12} = 1 \times 2 = 2$$

$$a_{13} = 1 \times 3 = 3$$

$$a_{21} = 2 \times 1 = 2$$

$$a_{22} = 2 \times 2 = 4$$

$$a_{23} = 2 \times 3 = 6$$

Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \end{bmatrix}$$

(ii) Given $a_{ij} = 2i - j$

Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 2×3 matrix are

$a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$$a_{11} = 2 \times 1 - 1 = 2 - 1 = 1$$

$$a_{12} = 2 \times 1 - 2 = 2 - 2 = 0$$

$$a_{13} = 2 \times 1 - 3 = 2 - 3 = -1$$

$$a_{21} = 2 \times 2 - 1 = 4 - 1 = 3$$

$$a_{22} = 2 \times 2 - 2 = 4 - 2 = 2$$

$$a_{23} = 2 \times 2 - 3 = 4 - 3 = 1$$

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Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 1 & 0 & -1 \\ 3 & 2 & 1 \end{bmatrix}$$

(iii) Given $a_{ij} = i + j$

Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 2×3 matrix are

$a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$$a_{11} = 1 + 1 = 2$$

$$a_{12} = 1 + 2 = 3$$

$$a_{13} = 1 + 3 = 4$$

$$a_{21} = 2 + 1 = 3$$

$$a_{22} = 2 + 2 = 4$$

$$a_{23} = 2 + 3 = 5$$

Substituting these values in matrix A we get,

(iv) Given $a_{ij} = (i + j)^2/2$

Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 2×3 matrix are

$a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

Let $A = [a_{ij}]_{2 \times 3}$

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So, the elements in a 2×3 matrix are

$a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$a_{11} =$

$$\frac{(1+1)^2}{2} = \frac{2^2}{2} = \frac{4}{2} = 2$$

$a_{12} =$

$$\frac{(1+2)^2}{2} = \frac{3^2}{2} = \frac{9}{2} = 4.5$$

$a_{13} =$

$$\frac{(1+3)^2}{2} = \frac{4^2}{2} = \frac{16}{2} = 8$$

$a_{21} =$

$$\frac{(2+1)^2}{2} = \frac{3^2}{2} = \frac{9}{2} = 4.5$$

$a_{22} =$

$$\frac{(2+2)^2}{2} = \frac{4^2}{2} = \frac{16}{2} = 8$$

$a_{23} =$

$$\frac{(2+3)^2}{2} = \frac{5^2}{2} = \frac{25}{2} = 12.5$$

Substituting these values in matrix A we get,

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$$A = \begin{bmatrix} 2 & 4.5 & 8 \\ 4.5 & 8 & 12.5 \end{bmatrix} \quad A = \begin{bmatrix} 2 & \frac{9}{2} & 8 \\ \frac{9}{2} & 8 & \frac{25}{2} \end{bmatrix}$$

5. Construct a 2×2 matrix $A = [a_{ij}]$ whose elements a_{ij} are given by:

(i) $(i + j)^2 / 2$

(ii) $a_{ij} = (i - j)^2 / 2$

(iii) $a_{ij} = (i - 2j)^2 / 2$

(iv) $a_{ij} = (2i + j)^2 / 2$

(v) $a_{ij} = |2i - 3j| / 2$

(vi) $a_{ij} = |-3i + j| / 2$

(vii) $a_{ij} = e^{2ix} \sin x_j$

Solution:

(i) Given $(i + j)^2 / 2$

Let $A = [a_{ij}]_{2 \times 2}$

So, the elements in a 2×2 matrix are

$a_{11}, a_{12}, a_{21}, a_{22}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$a_{11} =$

$$\frac{(1+1)^2}{2} = \frac{2^2}{2} = \frac{4}{2} = 2$$

$a_{12} =$

$$\frac{(1+2)^2}{2} = \frac{3^2}{2} = \frac{9}{2} = 4.5$$

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$$a_{21} =$$

$$\frac{(2+1)^2}{2} = \frac{3^2}{2} = \frac{9}{2} = 4.5$$

$$a_{22} =$$

$$\frac{(2+2)^2}{2} = \frac{4^2}{2} = \frac{16}{2} = 8$$

Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 2 & 4.5 \\ 4.25 & 8 \end{bmatrix} \quad A = \begin{bmatrix} 2 & \frac{9}{2} \\ \frac{9}{2} & 8 \end{bmatrix}$$

(ii) Given $a_{ij} = (i-j)^2/2$

Let $A = [a_{ij}]_{2 \times 2}$

So, the elements in a 2×2 matrix are

$$a_{11}, a_{12}, a_{21}, a_{22}$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$$a_{11} =$$

$$\frac{(1-1)^2}{2} = \frac{0^2}{2} = 0$$

$$a_{12} =$$

$$\frac{(1-2)^2}{2} = \frac{1^2}{2} = \frac{1}{2} = 0.5$$

$$a_{21} =$$

$$\frac{(2-1)^2}{2} = \frac{1^2}{2} = \frac{1}{2} = 0.5$$

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$$a_{22} =$$

$$\frac{(2-2)^2}{2} = \frac{0^2}{2} = 0$$

Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 0 & 0.5 \\ 0.5 & 0 \end{bmatrix} \quad A = \begin{bmatrix} 0 & \frac{1}{2} \\ \frac{1}{2} & 0 \end{bmatrix}$$

(iii) Given $a_{ij} = (i - 2j)^2 / 2$

Let $A = [a_{ij}]_{2 \times 2}$

So, the elements in a 2×2 matrix are

$$a_{11}, a_{12}, a_{21}, a_{22}$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$$a_{11} =$$

$$\frac{(1-2 \times 1)^2}{2} = \frac{1^2}{2} = 0.5$$

$$a_{12} =$$

$$\frac{(1-2 \times 2)^2}{2} = \frac{3^2}{2} = \frac{9}{2} = 4.5$$

$$a_{21} =$$

$$\frac{(2-2 \times 1)^2}{2} = \frac{0^2}{2} = 0$$

$$a_{22} =$$

$$\frac{(2-2 \times 2)^2}{2} = \frac{2^2}{2} = \frac{4}{2} = 2$$

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Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 0.5 & 4.5 \\ 0 & 2 \end{bmatrix} \quad A = \begin{bmatrix} \frac{1}{2} & \frac{9}{2} \\ 0 & 2 \end{bmatrix}$$

(iv) Given $a_{ij} = (2i + j)^2 / 2$

Let $A = [a_{ij}]_{2 \times 2}$

So, the elements in a 2×2 matrix are

$a_{11}, a_{12}, a_{21}, a_{22}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$a_{11} =$

$$\frac{(2 \times 1 + 1)^2}{2} = \frac{3^2}{2} = \frac{9}{2} = 4.5$$

$a_{12} =$

$$\frac{(2 \times 1 + 2)^2}{2} = \frac{4^2}{2} = \frac{16}{2} = 8$$

$a_{21} =$

$$\frac{(2 \times 2 + 1)^2}{2} = \frac{5^2}{2} = \frac{25}{2} = 12.5$$

$a_{22} =$

$$\frac{(2 \times 2 + 2)^2}{2} = \frac{6^2}{2} = \frac{36}{2} = 18$$

Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 4.5 & 8 \\ 12.5 & 18 \end{bmatrix} \quad A = \begin{bmatrix} \frac{9}{2} & 8 \\ \frac{25}{2} & 18 \end{bmatrix}$$

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(v) Given $a_{ij} = |2i - 3j|/2$

Let $A = [a_{ij}]_{2 \times 2}$

So, the elements in a 2×2 matrix are

$a_{11}, a_{12}, a_{21}, a_{22}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$a_{11} =$

$$\frac{|2 \times 1 - 3 \times 1|}{2} = \frac{1}{2} = 0.5$$

$a_{12} =$

$$\frac{|2 \times 1 - 3 \times 2|}{2} = \frac{4}{2} = 2$$

$a_{21} =$

$$\frac{|2 \times 2 - 3 \times 1|}{2} = \frac{4 - 3}{2} = \frac{1}{2} = 0.5$$

$a_{22} =$

$$\frac{|2 \times 2 - 3 \times 2|}{2} = \frac{2}{2} = 1$$

Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 0.5 & 2 \\ 0.5 & 1 \end{bmatrix} \quad A = \begin{bmatrix} \frac{1}{2} & 2 \\ \frac{1}{2} & 1 \end{bmatrix}$$

(vi) Given $a_{ij} = |-3i + j|/2$

Let $A = [a_{ij}]_{2 \times 2}$

So, the elements in a 2×2 matrix are

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$a_{11}, a_{12}, a_{21}, a_{22}$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

$a_{11} =$

$$\frac{|-3 \times 1 + 1|}{2} = \frac{2}{2} = 1$$

$a_{12} =$

$$\frac{|-3 \times 1 + 2|}{2} = \frac{1}{2} = 0.5$$

$a_{21} =$

$$\frac{|-3 \times 2 + 1|}{2} = \frac{5}{2} = 2.5$$

$a_{22} =$

$$\frac{|-3 \times 2 + 2|}{2} = \frac{4}{2} = 2$$

Substituting these values in matrix A we get,

$$A = \begin{bmatrix} 1 & 0.5 \\ 2.5 & 2 \end{bmatrix} \quad A = \begin{bmatrix} 1 & \frac{1}{2} \\ \frac{5}{2} & 2 \end{bmatrix}$$

(vii) Given $a_{ij} = e^{2ix} \sin x j$

Let $A = [a_{ij}]_{2 \times 2}$

So, the elements in a 2×2 matrix are

$a_{11}, a_{12}, a_{21}, a_{22},$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

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$$a_{11} =$$

$$e^{2 \times 1x} \sin x \times 1 = e^{2x} \sin x$$

$$a_{12} =$$

$$e^{2 \times 1x} \sin x \times 2 = e^{2x} \sin 2x$$

$$a_{21} =$$

$$e^{2 \times 2x} \sin x \times 1 = e^{4x} \sin x$$

$$a_{22} =$$

$$e^{2 \times 2x} \sin x \times 2 = e^{4x} \sin 2x$$

Substituting these values in matrix A we get,

$$A = \begin{bmatrix} e^{2x} \sin x & e^{2x} \sin 2x \\ e^{4x} \sin x & e^{4x} \sin 2x \end{bmatrix}$$

6. Construct a 3×4 matrix $A = [a_{ij}]$ whose elements a_{ij} are given by:

(i) $a_{ij} = i + j$

(ii) $a_{ij} = i - j$

(iii) $a_{ij} = 2i$

(iv) $a_{ij} = j$

(v) $a_{ij} = \frac{1}{2} |-3i + j|$

Solution:

(i) Given $a_{ij} = i + j$

Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 3×4 matrix are

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$a_{11}, a_{12}, a_{13}, a_{14}, a_{21}, a_{22}, a_{23}, a_{24}, a_{31}, a_{32}, a_{33}, a_{34}$

A =

$$\begin{bmatrix} a_{11} & \cdots & a_{14} \\ \vdots & \ddots & \vdots \\ a_{31} & \cdots & a_{34} \end{bmatrix}$$

$$a_{11} = 1 + 1 = 2$$

$$a_{12} = 1 + 2 = 3$$

$$a_{13} = 1 + 3 = 4$$

$$a_{14} = 1 + 4 = 5$$

$$a_{21} = 2 + 1 = 3$$

$$a_{22} = 2 + 2 = 4$$

$$a_{23} = 2 + 3 = 5$$

$$a_{24} = 2 + 4 = 6$$

$$a_{31} = 3 + 1 = 4$$

$$a_{32} = 3 + 2 = 5$$

$$a_{33} = 3 + 3 = 6$$

$$a_{34} = 3 + 4 = 7$$

Substituting these values in matrix A we get,

A =

$$\begin{bmatrix} 2 & \cdots & 5 \\ \vdots & \ddots & \vdots \\ 4 & \cdots & 7 \end{bmatrix} A = \begin{bmatrix} 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 \\ 4 & 5 & 6 & 7 \end{bmatrix}$$

(ii) Given $a_{ij} = i - j$

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Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 3×4 matrix are

$a_{11}, a_{12}, a_{13}, a_{14}, a_{21}, a_{22}, a_{23}, a_{24}, a_{31}, a_{32}, a_{33}, a_{34}$

$A =$

$$\begin{bmatrix} a_{11} & \cdots & a_{14} \\ \vdots & \ddots & \vdots \\ a_{31} & \cdots & a_{34} \end{bmatrix}$$

$$a_{11} = 1 - 1 = 0$$

$$a_{12} = 1 - 2 = -1$$

$$a_{13} = 1 - 3 = -2$$

$$a_{14} = 1 - 4 = -3$$

$$a_{21} = 2 - 1 = 1$$

$$a_{22} = 2 - 2 = 0$$

$$a_{23} = 2 - 3 = -1$$

$$a_{24} = 2 - 4 = -2$$

$$a_{31} = 3 - 1 = 2$$

$$a_{32} = 3 - 2 = 1$$

$$a_{33} = 3 - 3 = 0$$

$$a_{34} = 3 - 4 = -1$$

Substituting these values in matrix A we get,

$A =$

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$$\begin{bmatrix} 0 & \dots & -3 \\ \vdots & \ddots & \vdots \\ 2 & \dots & -1 \end{bmatrix} A = \begin{bmatrix} 0 & -1 & -2 & -3 \\ 1 & 0 & -1 & -2 \\ 2 & 1 & 0 & -1 \end{bmatrix}$$

(iii) Given $a_{ij} = 2i$

Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 3×4 matrix are

$a_{11}, a_{12}, a_{13}, a_{14}, a_{21}, a_{22}, a_{23}, a_{24}, a_{31}, a_{32}, a_{33}, a_{34}$

$A =$

$$\begin{bmatrix} a_{11} & \dots & a_{14} \\ \vdots & \ddots & \vdots \\ a_{31} & \dots & a_{34} \end{bmatrix}$$

$$a_{11} = 2 \times 1 = 2$$

$$a_{12} = 2 \times 1 = 2$$

$$a_{13} = 2 \times 1 = 2$$

$$a_{14} = 2 \times 1 = 2$$

$$a_{21} = 2 \times 2 = 4$$

$$a_{22} = 2 \times 2 = 4$$

$$a_{23} = 2 \times 2 = 4$$

$$a_{24} = 2 \times 2 = 4$$

$$a_{31} = 2 \times 3 = 6$$

$$a_{32} = 2 \times 3 = 6$$

$$a_{33} = 2 \times 3 = 6$$

$$a_{34} = 2 \times 3 = 6$$

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Substituting these values in matrix A we get,

A =

$$\begin{bmatrix} 2 & \dots & 2 \\ \vdots & \ddots & \vdots \\ 6 & \dots & 6 \end{bmatrix} A = \begin{bmatrix} 2 & 2 & 2 & 2 \\ 4 & 4 & 4 & 4 \\ 6 & 6 & 6 & 6 \end{bmatrix}$$

(iv) Given $a_{ij} = j$

Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 3×4 matrix are

$a_{11}, a_{12}, a_{13}, a_{14}, a_{21}, a_{22}, a_{23}, a_{24}, a_{31}, a_{32}, a_{33}, a_{34}$

A =

$$\begin{bmatrix} a_{11} & \dots & a_{14} \\ \vdots & \ddots & \vdots \\ a_{31} & \dots & a_{34} \end{bmatrix}$$

$$a_{11} = 1$$

$$a_{12} = 2$$

$$a_{13} = 3$$

$$a_{14} = 4$$

$$a_{21} = 1$$

$$a_{22} = 2$$

$$a_{23} = 3$$

$$a_{24} = 4$$

$$a_{31} = 1$$

$$a_{32} = 2$$

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$$a_{33} = 3$$

$$a_{34} = 4$$

Substituting these values in matrix A we get,

A =

$$\begin{bmatrix} 1 & \dots & 4 \\ \vdots & \ddots & \vdots \\ 1 & \dots & 4 \end{bmatrix} A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{bmatrix}$$

(vi) Given $a_{ij} = \frac{1}{2} |-3i + j|$

Let $A = [a_{ij}]_{2 \times 3}$

So, the elements in a 3×4 matrix are

$a_{11}, a_{12}, a_{13}, a_{14}, a_{21}, a_{22}, a_{23}, a_{24}, a_{31}, a_{32}, a_{33}, a_{34}$

A =

$$\begin{bmatrix} a_{11} & \dots & a_{14} \\ \vdots & \ddots & \vdots \\ a_{31} & \dots & a_{34} \end{bmatrix}$$

$$a_{11} =$$

$$\frac{1}{2}(-3 \times 1 + 1) = \frac{1}{2}(-3 + 1) = \frac{1}{2}(-2) = -1$$

$$a_{12} =$$

$$\frac{1}{2}(-3 \times 1 + 2) = \frac{1}{2}(-3 + 2) = \frac{1}{2}(-1) = -\frac{1}{2}$$

$$a_{13} =$$

$$\frac{1}{2}(-3 \times 1 + 3) = \frac{1}{2}(-3 + 3) = \frac{1}{2}(0) = 0$$

$$a_{14} =$$

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$$\frac{1}{2}(-3 \times 1 + 4) = \frac{1}{2}(-3 + 4) = \frac{1}{2}(1) = \frac{1}{2}$$

$$a_{21} =$$

$$\frac{1}{2}(-3 \times 2 + 1) = \frac{1}{2}(-6 + 1) = \frac{1}{2}(-5) = -\frac{5}{2}$$

$$a_{22} =$$

$$\frac{1}{2}(-3 \times 2 + 2) = \frac{1}{2}(-6 + 2) = \frac{1}{2}(-4) = -2$$

$$a_{23} =$$

$$\frac{1}{2}(-3 \times 2 + 3) = \frac{1}{2}(-6 + 3) = \frac{1}{2}(-3) = -\frac{3}{2}$$

$$a_{24} =$$

$$\frac{1}{2}(-3 \times 2 + 4) = \frac{1}{2}(-6 + 4) = \frac{1}{2}(-2) = -1$$

$$a_{31} =$$

$$\frac{1}{2}(-3 \times 3 + 1) = \frac{1}{2}(-9 + 1) = \frac{1}{2}(-8) = -4$$

$$a_{32} =$$

$$\frac{1}{2}(-3 \times 3 + 2) = \frac{1}{2}(-9 + 2) = \frac{1}{2}(-7) = -\frac{7}{2}$$

$$a_{33} =$$

$$\frac{1}{2}(-3 \times 3 + 3) = \frac{1}{2}(-9 + 3) = \frac{1}{2}(-6) = -3$$

$$a_{34} =$$

$$\frac{1}{2}(-3 \times 3 + 4) = \frac{1}{2}(-9 + 4) = \frac{1}{2}(-5) = -\frac{5}{2}$$

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Substituting these values in matrix A we get,

A =

$$\begin{bmatrix} -1 & \cdots & \frac{1}{2} \\ \vdots & \ddots & \vdots \\ -4 & \cdots & -\frac{5}{2} \end{bmatrix}$$

Multiplying by negative sign we get,

7. Construct a 4×3 matrix $A = [a_{ij}]$ whose elements a_{ij} are given by:

(i) $a_{ij} = 2i + i/j$

(ii) $a_{ij} = (i - j)/(i + j)$

(iii) $a_{ij} = i$

Solution:

(i) Given $a_{ij} = 2i + i/j$

Let $A = [a_{ij}]_{4 \times 3}$

So, the elements in a 4×3 matrix are

$$a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}, a_{31}, a_{32}, a_{33}, a_{41}, a_{42}, a_{43}$$

A =

$$\begin{bmatrix} a_{11} & \cdots & a_{13} \\ \vdots & \ddots & \vdots \\ a_{41} & \cdots & a_{43} \end{bmatrix}$$

$a_{11} =$

$$2 \times 1 + \frac{1}{1} = 2 + 1 = 3$$

$a_{12} =$

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$$2 \times 1 + \frac{1}{2} = 2 + \frac{1}{2} = \frac{5}{2}$$

$$a_{13} =$$

$$2 \times 1 + \frac{1}{3} = 2 + \frac{1}{3} = \frac{7}{3}$$

$$a_{21} =$$

$$2 \times 2 + \frac{2}{1} = 4 + 2 = 6$$

$$a_{22} =$$

$$2 \times 2 + \frac{2}{2} = 4 + 1 = 5$$

$$a_{23} =$$

$$2 \times 2 + \frac{2}{3} = 4 + \frac{2}{3} = \frac{14}{3}$$

$$a_{31} =$$

$$2 \times 3 + \frac{3}{1} = 6 + 3 = 9$$

$$a_{32} =$$

$$2 \times 3 + \frac{3}{2} = 6 + \frac{3}{2} = \frac{15}{2}$$

$$a_{33} =$$

$$2 \times 3 + \frac{3}{3} = 6 + 1 = 7$$

$$a_{41} =$$

$$2 \times 4 + \frac{4}{1} = 8 + 4 = 12$$

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$$a_{42} =$$

$$2 \times 4 + \frac{4}{2} = 8 + 2 = 10$$

$$a_{43} =$$

$$2 \times 4 + \frac{4}{3} = 8 + \frac{4}{3} = \frac{28}{3}$$

Substituting these values in matrix A we get,

$$A =$$

$$\begin{bmatrix} 3 & \dots & \frac{7}{3} \\ \vdots & \ddots & \vdots \\ 12 & \dots & \frac{28}{3} \end{bmatrix} A = \begin{bmatrix} 3 & \frac{5}{2} & \frac{7}{3} \\ 6 & 5 & \frac{14}{3} \\ 9 & \frac{15}{2} & 7 \\ 12 & 10 & \frac{28}{3} \end{bmatrix}$$

(ii) Given $a_{ij} = (i - j) / (i + j)$

$$\text{Let } A = [a_{ij}]_{4 \times 3}$$

So, the elements in a 4×3 matrix are

$$a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}, a_{31}, a_{32}, a_{33}, a_{41}, a_{42}, a_{43}$$

$$A =$$

$$\begin{bmatrix} a_{11} & \dots & a_{13} \\ \vdots & \ddots & \vdots \\ a_{41} & \dots & a_{43} \end{bmatrix}$$

$$a_{11} =$$

$$\frac{1-1}{1+1} = \frac{0}{2} = 0$$

$$a_{12} =$$

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$$\frac{1-2}{1+2} = \frac{-1}{3}$$

$$a_{13} =$$

$$\frac{1-3}{1+3} = \frac{-2}{4} = -\frac{1}{2}$$

$$a_{21} =$$

$$\frac{2-1}{2+1} = \frac{1}{3}$$

$$a_{22} =$$

$$\frac{2-2}{2+2} = \frac{0}{4} = 0$$

$$a_{23} =$$

$$\frac{2-3}{2+3} = \frac{-1}{5}$$

$$a_{31} =$$

$$\frac{3-1}{3+1} = \frac{2}{4} = \frac{1}{2}$$

$$a_{32} =$$

$$\frac{3-2}{3+2} = \frac{1}{5}$$

$$a_{33} =$$

$$\frac{3-3}{3+3} = \frac{0}{6} = 0$$

$$a_{41} =$$

$$\frac{4-1}{4+1} = \frac{3}{5}$$

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$$a_{42} =$$

$$\frac{4-2}{4+2} = \frac{2}{6} = \frac{1}{3}$$

$$a_{43} =$$

$$\frac{4-3}{4+3} = \frac{1}{7}$$

Substituting these values in matrix A we get,

$$A =$$

$$\begin{bmatrix} 0 & \cdots & -\frac{1}{2} \\ \vdots & \ddots & \vdots \\ 3 & \cdots & \frac{1}{7} \\ 5 & \cdots & \frac{1}{7} \end{bmatrix} A = \begin{bmatrix} 0 & \frac{-1}{3} & \frac{-1}{2} \\ \frac{1}{3} & 0 & \frac{-1}{5} \\ \frac{1}{2} & \frac{1}{5} & 0 \\ \frac{3}{5} & \frac{1}{3} & \frac{1}{7} \end{bmatrix}$$

(iii) Given $a_{ij} = i$

$$\text{Let } A = [a_{ij}]_{4 \times 3}$$

So, the elements in a 4×3 matrix are

$$a_{11}, a_{12}, a_{13}, a_{21}, a_{22}, a_{23}, a_{31}, a_{32}, a_{33}, a_{41}, a_{42}, a_{43}$$

$$A =$$

$$\begin{bmatrix} a_{11} & \cdots & a_{13} \\ \vdots & \ddots & \vdots \\ a_{41} & \cdots & a_{43} \end{bmatrix}$$

$$a_{11} = 1$$

$$a_{12} = 1$$

$$a_{13} = 1$$

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$$a_{21} = 2$$

$$a_{22} = 2$$

$$a_{23} = 2$$

$$a_{31} = 3$$

$$a_{32} = 3$$

$$a_{33} = 3$$

$$a_{41} = 4$$

$$a_{42} = 4$$

$$a_{43} = 4$$

Substituting these values in matrix A we get,

A =

$$\begin{bmatrix} 1 & \dots & 1 \\ \vdots & \ddots & \vdots \\ 4 & \dots & 4 \end{bmatrix} A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \\ 4 & 4 & 4 \end{bmatrix}$$

8. Find x, y, a and b if

$$\begin{bmatrix} 3x + 4y & 2 & x - 2y \\ a + b & 2a - b & -1 \end{bmatrix} = \begin{bmatrix} 2 & 2 & 4 \\ 5 & -5 & -1 \end{bmatrix}$$

Solution:

Given

$$\begin{bmatrix} 3x + 4y & 2 & x - 2y \\ a + b & 2a - b & -1 \end{bmatrix} = \begin{bmatrix} 2 & 2 & 4 \\ 5 & -5 & -1 \end{bmatrix}$$

Given that two matrices are equal.

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We know that if two matrices are equal then the elements of each matrices are also equal.

Therefore by equating them we get,

$$3x + 4y = 2 \dots\dots (1)$$

$$x - 2y = 4 \dots\dots (2)$$

$$a + b = 5 \dots\dots (3)$$

$$2a - b = -5 \dots\dots (4)$$

Multiplying equation (2) by 2 and adding to equation (1), we get

$$3x + 4y + 2x - 4y = 2 + 8$$

$$\Rightarrow 5x = 10$$

$$\Rightarrow x = 2$$

Now, substituting the value of x in equation (1)

$$3 \times 2 + 4y = 2$$

$$\Rightarrow 6 + 4y = 2$$

$$\Rightarrow 4y = 2 - 6$$

$$\Rightarrow 4y = -4$$

$$\Rightarrow y = -1$$

Now by adding equation (3) and (4)

$$a + b + 2a - b = 5 + (-5)$$

$$\Rightarrow 3a = 5 - 5 = 0$$

$$\Rightarrow a = 0$$

Now, again by substituting the value of a in equation (3), we get

$$0 + b = 5$$

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$$\Rightarrow b = 5$$

$$\therefore a = 0, b = 5, x = 2 \text{ and } y = -1$$

9. Find x, y, a and b if

$$\begin{bmatrix} 2x - 3y & a - b & 3 \\ 1 & x + 4y & 3a + 4b \end{bmatrix} = \begin{bmatrix} 1 & -2 & 3 \\ 1 & 6 & 29 \end{bmatrix}$$

Solution:

$$\begin{bmatrix} 2x - 3y & a - b & 3 \\ 1 & x + 4y & 3a + 4b \end{bmatrix} = \begin{bmatrix} 1 & -2 & 3 \\ 1 & 6 & 29 \end{bmatrix}$$

We know that if two matrices are equal then the elements of each matrices are also equal.

Given that two matrices are equal.

Therefore by equating them we get,

$$2a + b = 4 \dots\dots (1)$$

$$\text{And } a - 2b = -3 \dots\dots (2)$$

$$\text{And } 5c - d = 11 \dots\dots (3)$$

$$4c + 3d = 24 \dots\dots (4)$$

Multiplying equation (1) by 2 and adding to equation (2)

$$4a + 2b + a - 2b = 8 - 3$$

$$\Rightarrow 5a = 5$$

$$\Rightarrow a = 1$$

Now, substituting the value of a in equation (1)

$$2 \times 1 + b = 4$$

$$\Rightarrow 2 + b = 4$$

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$$\Rightarrow b = 4 - 2$$

$$\Rightarrow b = 2$$

Multiplying equation (3) by 3 and adding to equation (4)

$$15c - 3d + 4c + 3d = 33 + 24$$

$$\Rightarrow 19c = 57$$

$$\Rightarrow c = 3$$

Now, substituting the value of c in equation (4)

$$4 \times 3 + 3d = 24$$

$$\Rightarrow 12 + 3d = 24$$

$$\Rightarrow 3d = 24 - 12$$

$$\Rightarrow 3d = 12$$

$$\Rightarrow d = 4$$

$$\therefore a = 1, b = 2, c = 3 \text{ and } d = 4$$

10. Find the values of a, b, c and d from the following equations:

$$\begin{bmatrix} 2a + b & a - 2b \\ 5c - d & 4c + 3d \end{bmatrix} = \begin{bmatrix} 4 & -3 \\ 11 & 24 \end{bmatrix}$$

Solution:

Given

$$\begin{bmatrix} 2a + b & a - 2b \\ 5c - d & 4c + 3d \end{bmatrix} = \begin{bmatrix} 4 & -3 \\ 11 & 24 \end{bmatrix}$$

We know that if two matrices are equal then the elements of each matrices are also equal.

Given that two matrices are equal.

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Therefore by equating them we get,

$$2a + b = 4 \dots\dots (1)$$

$$\text{And } a - 2b = -3 \dots\dots (2)$$

$$\text{And } 5c - d = 11 \dots\dots (3)$$

$$4c + 3d = 24 \dots\dots (4)$$

Multiplying equation (1) by 2 and adding to equation (2)

$$4a + 2b + a - 2b = 8 - 3$$

$$\Rightarrow 5a = 5$$

$$\Rightarrow a = 1$$

Now, substituting the value of a in equation (1)

$$2 \times 1 + b = 4$$

$$\Rightarrow 2 + b = 4$$

$$\Rightarrow b = 4 - 2$$

$$\Rightarrow b = 2$$

Multiplying equation (3) by 3 and adding to equation (4)

$$15c - 3d + 4c + 3d = 33 + 24$$

$$\Rightarrow 19c = 57$$

$$\Rightarrow c = 3$$

Now, substituting the value of c in equation (4)

$$4 \times 3 + 3d = 24$$

$$\Rightarrow 12 + 3d = 24$$

$$\Rightarrow 3d = 24 - 12$$

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$$\Rightarrow 3d = 12$$

$$\Rightarrow d = 4$$

$$\therefore a = 1, b = 2, c = 3 \text{ and } d = 4$$

Exercise 5.2 Page No: 5.18

1. Compute the following sums:

$$(i) \begin{bmatrix} 3 & -2 \\ 1 & 4 \end{bmatrix} + \begin{bmatrix} -2 & 4 \\ 1 & 3 \end{bmatrix} \quad (ii) \begin{bmatrix} 2 & 1 & 3 \\ 0 & 3 & 5 \\ -1 & 2 & 5 \end{bmatrix} + \begin{bmatrix} 1 & -2 & 3 \\ 2 & 6 & 1 \\ 0 & -3 & 1 \end{bmatrix}$$

Solution:

(i) Given

$$(i) \begin{bmatrix} 3 & -2 \\ 1 & 4 \end{bmatrix} + \begin{bmatrix} -2 & 4 \\ 1 & 3 \end{bmatrix}$$

Corresponding elements of two matrices should be added

Therefore, we get

$$= \begin{bmatrix} 3-2 & -2+4 \\ 1+1 & 4+3 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 2 \\ 2 & 7 \end{bmatrix}$$

$$\text{Hence, } \begin{bmatrix} 3 & -2 \\ 1 & 4 \end{bmatrix} + \begin{bmatrix} -2 & 4 \\ 1 & 3 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 2 & 7 \end{bmatrix}$$

Therefore,

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$$\begin{bmatrix} 3 & -2 \\ 1 & 4 \end{bmatrix} + \begin{bmatrix} -2 & 4 \\ 1 & 3 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 2 & 7 \end{bmatrix}$$

(ii) Given

$$(ii) \begin{bmatrix} 2 & 1 & 3 \\ 0 & 3 & 5 \\ -1 & 2 & 5 \end{bmatrix} + \begin{bmatrix} 1 & -2 & 3 \\ 2 & 6 & 1 \\ 0 & -3 & 1 \end{bmatrix} = \begin{bmatrix} 2+1 & 1-2 & 3+3 \\ 0+2 & 3+6 & 5+1 \\ -1+0 & 2-3 & 5+1 \end{bmatrix} = \begin{bmatrix} 3 & -1 & 6 \\ 2 & 9 & 6 \\ -1 & -1 & 6 \end{bmatrix}$$

Therefore,

$$\begin{bmatrix} 2 & 1 & 3 \\ 0 & 3 & 5 \\ -1 & 2 & 5 \end{bmatrix} + \begin{bmatrix} 1 & -2 & 3 \\ 2 & 6 & 1 \\ 0 & -3 & 1 \end{bmatrix} = \begin{bmatrix} 3 & -1 & 6 \\ 2 & 9 & 6 \\ -1 & -1 & 6 \end{bmatrix}$$

$$2. \text{Let } A = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} \quad \text{and } C = \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}.$$

Find each of the following:

(i) $2A - 3B$

(ii) $B - 4C$

(iii) $3A - C$

(iv) $3A - 2B + 3C$

Solution:

(i) Given

$$2. \text{Let } A = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} \quad \text{and } C = \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}.$$

First we have to compute $2A$

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$$2A = 2 \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} = \begin{bmatrix} 4 & 8 \\ 6 & 4 \end{bmatrix}$$

Now by computing $3B$ we get,

$$= 3B = 3 \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} = \begin{bmatrix} 3 & 9 \\ -6 & 15 \end{bmatrix}$$

Now by we have to compute $2A - 3B$ we get

$$= 2A - 3B = \begin{bmatrix} 4 & 8 \\ 6 & 4 \end{bmatrix} - \begin{bmatrix} 3 & 9 \\ -6 & 15 \end{bmatrix} = \begin{bmatrix} 4 - 3 & 8 - 9 \\ 6 + 6 & 4 - 15 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & -1 \\ 12 & -11 \end{bmatrix}$$

Therefore

$$2A - 3B = \begin{bmatrix} 1 & -1 \\ 12 & -11 \end{bmatrix}$$

(ii) Given

$$2. \text{ Let } A = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} \quad \text{and } C = \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}.$$

First we have to compute $4C$,

$$4C = 4 \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} -8 & 20 \\ 12 & 16 \end{bmatrix}$$

Now,

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$$B-4C = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} - \begin{bmatrix} -8 & 20 \\ 12 & 16 \end{bmatrix}$$

$$= \begin{bmatrix} 1+8 & 3-20 \\ -2-12 & 5-16 \end{bmatrix} = \begin{bmatrix} 9 & -17 \\ -14 & -11 \end{bmatrix}$$

Therefore we get,

$$B-4C = \begin{bmatrix} 9 & -17 \\ -14 & -11 \end{bmatrix}$$

(iii) Given

$$2. \text{Let } A = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} \quad \text{and } C = \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}.$$

First we have to compute $3A$,

$$3A = 3 \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} = \begin{bmatrix} 6 & 12 \\ 9 & 6 \end{bmatrix}$$

Now,

$$= 3A - C = \begin{bmatrix} 6 & 12 \\ 9 & 6 \end{bmatrix} - \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}$$

$$= \begin{bmatrix} 6+2 & 12-5 \\ 9-3 & 6-4 \end{bmatrix} = \begin{bmatrix} 8 & 7 \\ 6 & 2 \end{bmatrix}$$

Therefore,

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$$3A - C = \begin{bmatrix} 8 & 7 \\ 6 & 2 \end{bmatrix}$$

(iv) Given

$$2. \text{Let } A = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} \quad \text{and } C = \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}.$$

First we have to compute $3A$

$$3A = 3 \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} = \begin{bmatrix} 6 & 12 \\ 9 & 6 \end{bmatrix}$$

Now we have to compute $2B$

$$= 3C = 3 \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} -6 & 15 \\ 9 & 12 \end{bmatrix}$$

By computing $3C$ we get,

$$= 3A - 2B + 3C = \begin{bmatrix} 6 & 12 \\ 9 & 6 \end{bmatrix} - \begin{bmatrix} 2 & 6 \\ -4 & 10 \end{bmatrix} + \begin{bmatrix} -6 & 15 \\ 9 & 12 \end{bmatrix}$$

$$= 3C = 3 \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} -6 & 15 \\ 9 & 12 \end{bmatrix} = \begin{bmatrix} 6 - 2 - 6 & 12 - 6 + 15 \\ 9 + 4 + 9 & 6 - 10 + 12 \end{bmatrix} = \begin{bmatrix} -2 & 21 \\ 22 & 8 \end{bmatrix}$$

Therefore,

$$3A - 2B + 3C = \begin{bmatrix} -2 & 21 \\ 22 & 8 \end{bmatrix}$$

$$3. \text{If } A = \begin{bmatrix} 2 & 3 \\ 5 & 7 \end{bmatrix}, B = \begin{bmatrix} -1 & 0 & 2 \\ 3 & 4 & 1 \end{bmatrix}, C = \begin{bmatrix} -1 & 2 & 3 \\ 2 & 1 & 0 \end{bmatrix}, \text{ find}$$

(i) $A + B$ and $B + C$

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(ii) $2B + 3A$ and $3C - 4B$

Solution:

(i) Consider $A + B$,

$A + B$ is not possible because matrix A is an order of 2×2 and Matrix B is an order of 2×3 , so the Sum of the matrix is only possible when their order is same.

Now consider $B + C$

$$\Rightarrow B+C = \begin{bmatrix} -1 & 0 & 2 \\ 3 & 4 & 1 \end{bmatrix} + \begin{bmatrix} -1 & 2 & 3 \\ 2 & 1 & 0 \end{bmatrix}$$

$$\Rightarrow B+C = \begin{bmatrix} -1-1 & 0+2 & 2+3 \\ 3+2 & 4+1 & 1+0 \end{bmatrix}$$

$$\Rightarrow B+C = \begin{bmatrix} -2 & 2 & 5 \\ 5 & 5 & 1 \end{bmatrix}$$

(ii) Consider $2B + 3A$

$2B + 3A$ also does not exist because the order of matrix B and matrix A is different, so we cannot find the sum of these matrix.

Now consider $3C - 4B$,

$$\Rightarrow 3C - 4B = 3 \begin{bmatrix} -1 & 2 & 3 \\ 2 & 1 & 0 \end{bmatrix} - 4 \begin{bmatrix} -1 & 0 & 2 \\ 3 & 4 & 1 \end{bmatrix}$$

$$\Rightarrow 3C - 4B = \begin{bmatrix} -3 & 6 & 9 \\ 6 & 3 & 0 \end{bmatrix} - \begin{bmatrix} -4 & 0 & 8 \\ 12 & 16 & 4 \end{bmatrix}$$

$$\Rightarrow 3C - 4B = \begin{bmatrix} -3+4 & 6-0 & 9-8 \\ 6-12 & 3-16 & 0-4 \end{bmatrix}$$

$$\Rightarrow 3C - 4B = \begin{bmatrix} 1 & 6 & 1 \\ -6 & -13 & -4 \end{bmatrix}$$

4. Let $A = \begin{bmatrix} -1 & 0 & 2 \\ 3 & 1 & 4 \end{bmatrix}$, $B = \begin{bmatrix} 0 & -2 & 5 \\ 1 & -3 & 1 \end{bmatrix}$ and $C = \begin{bmatrix} 1 & -5 & 2 \\ 6 & 0 & -4 \end{bmatrix}$. Compute $2A - 3B + 4C$

Solution:

Given

$$A = \begin{bmatrix} -1 & 0 & 2 \\ 3 & 1 & 4 \end{bmatrix}, B = \begin{bmatrix} 0 & -2 & 5 \\ 1 & -3 & 1 \end{bmatrix} \text{ and } C = \begin{bmatrix} 1 & -5 & 2 \\ 6 & 0 & -4 \end{bmatrix}$$

Now we have to compute $2A - 3B + 4C$

$$2A - 3B + 4C = 2 \begin{bmatrix} -1 & 0 & 2 \\ 3 & 1 & 4 \end{bmatrix} - 3 \begin{bmatrix} 0 & -2 & 5 \\ 1 & -3 & 1 \end{bmatrix} + 4 \begin{bmatrix} 1 & -5 & 2 \\ 6 & 0 & -4 \end{bmatrix}$$

$$\Rightarrow 2A - 3B + 4C = \begin{bmatrix} -2 & 0 & 4 \\ 6 & 2 & 8 \end{bmatrix} - \begin{bmatrix} 0 & -6 & 15 \\ 3 & -9 & 3 \end{bmatrix} + \begin{bmatrix} 4 & -20 & 8 \\ 24 & 0 & -16 \end{bmatrix}$$

$$\Rightarrow 2A - 3B + 4C = \begin{bmatrix} -2 - 0 + 4 & 0 + 6 - 20 & 4 - 15 + 8 \\ 6 - 3 + 24 & 2 + 9 + 0 & 8 - 3 - 16 \end{bmatrix}$$

$$\Rightarrow 2A - 3B + 4C = \begin{bmatrix} 2 & -14 & -3 \\ 27 & 11 & -11 \end{bmatrix}$$

5. If $A = \text{diag } (2 \ -5 \ 9)$, $B = \text{diag } (1 \ 1 \ -4)$ and $C = \text{diag } (-6 \ 3 \ 4)$, find

(i) $A - 2B$

(ii) $B + C - 2A$

(iii) $2A + 3B - 5C$

Solution:

(i) Given $A = \text{diag } (2 \ -5 \ 9)$, $B = \text{diag } (1 \ 1 \ -4)$ and $C = \text{diag } (-6 \ 3 \ 4)$

Here,

$$A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -4 \end{bmatrix}$$

$$A - 2B$$

$$\Rightarrow A - 2B = \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix} - 2 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -4 \end{bmatrix}$$

$$\Rightarrow A - 2B = \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & -8 \end{bmatrix} - \begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & -8 \end{bmatrix}$$

$$\Rightarrow A - 2B = \begin{bmatrix} 0 & 0 & 0 \\ 0 & -7 & 0 \\ 0 & 0 & 17 \end{bmatrix} = \text{diag}(0 \ -7 \ 17)$$

(ii) Given $A = \text{diag}(2 \ -5 \ 9)$, $B = \text{diag}(1 \ 1 \ -4)$ and $C = \text{diag}(-6 \ 3 \ 4)$

We have to find $B + C - 2A$

Here,

Here,

$$A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -4 \end{bmatrix}$$

Now we have to compute $B + C - 2A$

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$$\Rightarrow B + C - 2A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -4 \end{bmatrix} + \begin{bmatrix} -6 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix} - 2 \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix}$$

$$\Rightarrow B + C - 2A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -4 \end{bmatrix} + \begin{bmatrix} -6 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix} - \begin{bmatrix} 4 & 0 & 0 \\ 0 & -10 & 0 \\ 0 & 0 & 18 \end{bmatrix}$$

$$\Rightarrow B + C - 2A = \begin{bmatrix} 1 - 6 - 4 & 0 + 0 - 0 & 0 + 0 - 0 \\ 0 + 0 - 0 & 1 + 3 + 10 & 0 + 0 - 0 \\ 0 + 0 - 0 & 0 + 0 - 0 & -4 + 4 - 18 \end{bmatrix}$$

$$\Rightarrow B + C - 2A = \begin{bmatrix} -9 & 0 & 0 \\ 0 & 14 & 0 \\ 0 & 0 & -18 \end{bmatrix} = \text{diag}(-9 \ 14 \ -18)$$

(iii) Given $A = \text{diag}(2 \ -5 \ 9)$, $B = \text{diag}(1 \ 1 \ -4)$ and $C = \text{diag}(-6 \ 3 \ 4)$

Now we have to find $2A + 3B - 5C$

Here,

$$A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -4 \end{bmatrix}$$

$$\text{and } C = \begin{bmatrix} -6 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix}$$

Now consider $2A + 3B - 5C$

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$$\begin{aligned}\Rightarrow 2A + 3B - 5C &= 2 \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix} + 3 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -4 \end{bmatrix} - 5 \begin{bmatrix} -6 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix} \\ \Rightarrow 2A + 3B - 5C &= \begin{bmatrix} 4 & 0 & 0 \\ 0 & -10 & 0 \\ 0 & 0 & 18 \end{bmatrix} + \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & -12 \end{bmatrix} - \begin{bmatrix} -30 & 0 & 0 \\ 0 & 15 & 0 \\ 0 & 0 & 20 \end{bmatrix} \\ \Rightarrow 2A + 3B - 5C &= \begin{bmatrix} 4 + 3 + 30 & 0 + 0 - 0 & 0 + 0 - 0 \\ 0 + 0 - 0 & -10 + 3 - 15 & 0 + 0 - 0 \\ 0 + 0 - 0 & 0 + 0 - 0 & 18 - 12 - 20 \end{bmatrix} \\ \Rightarrow 2A + 3B - 5C &= \begin{bmatrix} 37 & 0 & 0 \\ 0 & -22 & 0 \\ 0 & 0 & -14 \end{bmatrix} \\ &= \text{diag}(37 \ -22 \ -14)\end{aligned}$$

6. Given the matrices

$$A = \begin{bmatrix} 2 & 1 & 1 \\ 3 & -1 & 0 \\ 0 & 2 & 4 \end{bmatrix}, B = \begin{bmatrix} 9 & 7 & -1 \\ 3 & 5 & 4 \\ 2 & 1 & 6 \end{bmatrix} \text{ and } C = \begin{bmatrix} 2 & -4 & 3 \\ 1 & -1 & 0 \\ 9 & 4 & 5 \end{bmatrix}$$

Verify that $(A + B) + C = A + (B + C)$

Solution:

Given

$$A = \begin{bmatrix} 2 & 1 & 1 \\ 3 & -1 & 0 \\ 0 & 2 & 4 \end{bmatrix}, B = \begin{bmatrix} 9 & 7 & -1 \\ 3 & 5 & 4 \\ 2 & 1 & 6 \end{bmatrix} \text{ and } C = \begin{bmatrix} 2 & -4 & 3 \\ 1 & -1 & 0 \\ 9 & 4 & 5 \end{bmatrix}$$

Now we have to verify $(A + B) + C = A + (B + C)$

First consider LHS, $(A + B) + C$,

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$$= \left(\begin{bmatrix} 2 & 1 & 1 \\ 3 & -1 & 0 \\ 0 & 2 & 4 \end{bmatrix} + \begin{bmatrix} 9 & 7 & -1 \\ 3 & 5 & 4 \\ 2 & 1 & 6 \end{bmatrix} \right) + \begin{bmatrix} 2 & -4 & 3 \\ 1 & -1 & 0 \\ 9 & 4 & 5 \end{bmatrix}$$

$$= \left(\begin{bmatrix} 2+9 & 1+7 & 1-1 \\ 3+3 & -1+5 & 0+4 \\ 0+2 & 2+1 & 4+6 \end{bmatrix} \right) + \begin{bmatrix} 2 & -4 & 3 \\ 1 & -1 & 0 \\ 9 & 4 & 5 \end{bmatrix}$$

$$= \begin{bmatrix} 11 & 8 & 0 \\ 6 & 4 & 4 \\ 2 & 3 & 10 \end{bmatrix} + \begin{bmatrix} 2 & -4 & 3 \\ 1 & -1 & 0 \\ 9 & 4 & 5 \end{bmatrix}$$

$$= \begin{bmatrix} 11+2 & 8-4 & 0+3 \\ 6+1 & 4-1 & 4+0 \\ 2+9 & 3+4 & 10+5 \end{bmatrix}$$

$$= \begin{bmatrix} 13 & 4 & 3 \\ 7 & 3 & 4 \\ 11 & 7 & 15 \end{bmatrix}$$

Now consider RHS, that is $A + (B + C)$

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$$= \begin{bmatrix} 2 & 1 & 1 \\ 3 & -1 & 0 \\ 0 & 2 & 4 \end{bmatrix} + \left(\begin{bmatrix} 9 & 7 & -1 \\ 3 & 5 & 4 \\ 2 & 1 & 6 \end{bmatrix} + \begin{bmatrix} 2 & -4 & 3 \\ 1 & -1 & 0 \\ 9 & 4 & 5 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 2 & 1 & 1 \\ 3 & -1 & 0 \\ 0 & 2 & 4 \end{bmatrix} + \left(\begin{bmatrix} 9+2 & 7-4 & -1+3 \\ 3+1 & 5-1 & 4+0 \\ 2+9 & 1+4 & 6+5 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 2 & 1 & 1 \\ 3 & -1 & 0 \\ 0 & 2 & 4 \end{bmatrix} + \begin{bmatrix} 11 & 3 & 2 \\ 4 & 4 & 4 \\ 11 & 5 & 11 \end{bmatrix}$$

$$= \begin{bmatrix} 2+11 & 1+3 & 1+2 \\ 3+4 & -1+4 & 0+4 \\ 0+11 & 2+5 & 4+11 \end{bmatrix}$$

$$= \begin{bmatrix} 13 & 4 & 3 \\ 7 & 3 & 4 \\ 11 & 7 & 15 \end{bmatrix}$$

Therefore LHS = RHS

Hence $(A + B) + C = A + (B + C)$

7. Find the matrices X and Y,

$$\text{if } X + Y = \begin{bmatrix} 5 & 2 \\ 0 & 9 \end{bmatrix} \text{ and } X - Y = \begin{bmatrix} 3 & 6 \\ 0 & -1 \end{bmatrix}$$

Solution:

Consider,

$$(X + Y) + (X - Y) = \begin{bmatrix} 5 & 2 \\ 0 & 9 \end{bmatrix} + \begin{bmatrix} 3 & 6 \\ 0 & -1 \end{bmatrix}$$

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Now by simplifying we get,

$$\Rightarrow 2X = \begin{bmatrix} 5+3 & 2+6 \\ 0+0 & 9-1 \end{bmatrix}$$

$$\Rightarrow 2X = \begin{bmatrix} 8 & 8 \\ 0 & 8 \end{bmatrix}$$

$$\Rightarrow X = \frac{1}{2} \begin{bmatrix} 8 & 8 \\ 0 & 8 \end{bmatrix}$$

Therefore,

$$\Rightarrow X = \begin{bmatrix} 4 & 4 \\ 0 & 4 \end{bmatrix}$$

Again consider,

$$(X+Y) - (X-Y) = \begin{bmatrix} 5 & 2 \\ 0 & 9 \end{bmatrix} - \begin{bmatrix} 3 & 6 \\ 0 & -1 \end{bmatrix}$$

$$\Rightarrow X+Y - X+Y = \begin{bmatrix} 5-3 & 2-6 \\ 0-0 & 9+1 \end{bmatrix}$$

Now by simplifying we get,

$$\Rightarrow 2Y = \begin{bmatrix} 2 & -4 \\ 0 & 10 \end{bmatrix}$$

$$\Rightarrow Y = \frac{1}{2} \begin{bmatrix} 2 & -4 \\ 0 & 10 \end{bmatrix}$$

$$\Rightarrow Y = \begin{bmatrix} 1 & -2 \\ 0 & 5 \end{bmatrix}$$

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Therefore,

$$X = \begin{bmatrix} 4 & 4 \\ 0 & 4 \end{bmatrix} \text{ and } Y = \begin{bmatrix} 1 & -2 \\ 0 & 5 \end{bmatrix} \quad 8. \text{ Find } X, \text{ if } \begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix} \text{ and } 2X + Y = \begin{bmatrix} 1 & 0 \\ -3 & 2 \end{bmatrix}.$$

Solution:

Given

$$2X + Y = \begin{bmatrix} 1 & 0 \\ -3 & 2 \end{bmatrix}$$

Now by transposing, we get

$$\Rightarrow 2X + \begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ -3 & 2 \end{bmatrix}$$

$$\Rightarrow 2X = \begin{bmatrix} 1 & 0 \\ -3 & 2 \end{bmatrix} - \begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix}$$

$$\Rightarrow 2X = \begin{bmatrix} 1-3 & 0-2 \\ -3-1 & 2-4 \end{bmatrix}$$

$$\Rightarrow 2X = \begin{bmatrix} -2 & -2 \\ -4 & -2 \end{bmatrix}$$

$$\Rightarrow X = \frac{1}{2} \begin{bmatrix} -2 & -2 \\ -4 & -2 \end{bmatrix}$$

Therefore,

$$\Rightarrow X = \begin{bmatrix} -1 & -1 \\ -2 & -1 \end{bmatrix}$$

$$9. \text{ Find matrices } X \text{ and } Y, \text{ if } 2X - Y = \begin{bmatrix} 6 & -6 & 0 \\ -4 & 2 & 1 \end{bmatrix} \text{ and } X + 2Y = \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix}.$$

Solution:

Given

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$$(2X - Y) = \begin{bmatrix} 6 & -6 & 0 \\ -4 & 2 & 1 \end{bmatrix} \dots (1) \quad (X + 2Y) = \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix} \dots (2)$$

Now by multiplying equation (1) and (2) we get,

$$2(2X - Y) = 2 \begin{bmatrix} 6 & -6 & 0 \\ -4 & 2 & 1 \end{bmatrix} \Rightarrow 4X - 2Y = \begin{bmatrix} 12 & -12 & 0 \\ -8 & 4 & 2 \end{bmatrix} \dots (3)$$

Now by adding equation (2) and (3) we get,

$$(4X - 2Y) + (X + 2Y) = \begin{bmatrix} 12 & -12 & 0 \\ -8 & 4 & 2 \end{bmatrix} + \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix}$$

$$\Rightarrow 5X = \begin{bmatrix} 12 + 3 & -12 + 2 & 0 + 5 \\ -8 - 2 & 4 + 1 & 2 - 7 \end{bmatrix}$$

$$\Rightarrow 5X = \begin{bmatrix} 15 & -10 & 5 \\ -10 & 5 & -5 \end{bmatrix}$$

$$\Rightarrow X = \frac{1}{5} \begin{bmatrix} 15 & -10 & 5 \\ -10 & 5 & -5 \end{bmatrix}$$

$$\Rightarrow X = \begin{bmatrix} 3 & -2 & 1 \\ -2 & 1 & -1 \end{bmatrix}$$

Now by substituting X in equation (2) we get,

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$$(X + 2Y) = \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 3 & -2 & 1 \\ -2 & 1 & -1 \end{bmatrix} + 2Y = \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix}$$

$$\Rightarrow 2Y = \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix} - \begin{bmatrix} 3 & -2 & 1 \\ -2 & 1 & -1 \end{bmatrix}$$

$$\Rightarrow 2Y = \begin{bmatrix} 3-3 & 2+2 & 5-1 \\ -2+2 & 1-1 & -7+1 \end{bmatrix}$$

$$\Rightarrow Y = \begin{bmatrix} 0 & 2 & 2 \\ 0 & 0 & -3 \end{bmatrix}$$

10. If $X - Y = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$ and $X + Y = \begin{bmatrix} 3 & 5 & 1 \\ -1 & 1 & 1 \\ 11 & 8 & 0 \end{bmatrix}$ find X and Y .

Solution:

Consider

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$$X - Y + X + Y = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} + \begin{bmatrix} 3 & 5 & 1 \\ -1 & 1 & 4 \\ 11 & 8 & 0 \end{bmatrix}$$

$$\Rightarrow 2X = \begin{bmatrix} 1+3 & 1+5 & 1+1 \\ 1-1 & 1+1 & 0+1 \\ 1+11 & 0+8 & 0+0 \end{bmatrix}$$

$$\Rightarrow 2X = \begin{bmatrix} 4 & 6 & 2 \\ 0 & 2 & 4 \\ 12 & 8 & 0 \end{bmatrix}$$

$$\Rightarrow X = \frac{1}{2} \begin{bmatrix} 4 & 6 & 2 \\ 0 & 2 & 4 \\ 12 & 8 & 0 \end{bmatrix}$$

$$\Rightarrow X = \begin{bmatrix} 2 & 3 & 1 \\ 0 & 1 & 2 \\ 6 & 4 & 0 \end{bmatrix}$$

Now,

Now, again consider

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$$(X - Y) - (X + Y) = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} - \begin{bmatrix} 3 & 5 & 1 \\ -1 & 1 & 1 \\ 11 & 8 & 0 \end{bmatrix}$$

$$\Rightarrow X - Y - X - Y = \begin{bmatrix} 1 - 3 & 1 - 5 & 1 - 1 \\ 1 + 1 & 1 - 1 & 0 - 1 \\ 1 - 11 & 0 - 8 & 0 - 0 \end{bmatrix}$$

$$\Rightarrow -2Y = \begin{bmatrix} -2 & -4 & 0 \\ 2 & 0 & -1 \\ -10 & -8 & 0 \end{bmatrix}$$

$$\Rightarrow Y = -\frac{1}{2} \begin{bmatrix} -2 & -4 & 0 \\ 2 & 0 & -1 \\ -10 & -8 & 0 \end{bmatrix}$$

$$\Rightarrow Y = \begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & \frac{1}{2} \\ 5 & 4 & 0 \end{bmatrix}$$

Therefore,

$$\Rightarrow X = \begin{bmatrix} 2 & 3 & 1 \\ 0 & 1 & 2 \\ 6 & 4 & 0 \end{bmatrix}$$

And

$$Y = \begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & \frac{1}{2} \\ 5 & 4 & 0 \end{bmatrix}$$

Exercise 5.3 Page No: 5.41

1. Compute the indicated products:

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$$(i) \begin{bmatrix} a & b \\ -b & a \end{bmatrix} \begin{bmatrix} a & -b \\ b & a \end{bmatrix} \quad (ii) \begin{bmatrix} 1 & -2 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ -3 & 2 & 1 \end{bmatrix} \quad (iii) \begin{bmatrix} 2 & 3 & 4 \\ 3 & 4 & 5 \\ 4 & 5 & 6 \end{bmatrix} \begin{bmatrix} 1 & -3 & 5 \\ 0 & 2 & 4 \\ 3 & 0 & 5 \end{bmatrix}$$

Solution:

(i) Consider

$$\begin{aligned} & \begin{bmatrix} a & b \\ -b & a \end{bmatrix} \begin{bmatrix} a & -b \\ b & a \end{bmatrix} \\ \Rightarrow & \begin{bmatrix} a \times a + b \times b & a \times (-b) + b \times a \\ (-b) \times a + a \times b & (-b) \times (-b) + a \times a \end{bmatrix} \\ \Rightarrow & \begin{bmatrix} a^2 + b^2 & -ab + ab \\ -ab + ab & b^2 + a^2 \end{bmatrix} \end{aligned}$$

On simplification we get,

$$\Rightarrow \begin{bmatrix} a^2 + b^2 & 0 \\ 0 & a^2 + b^2 \end{bmatrix}$$

(ii) Consider

$$\begin{aligned} & \begin{bmatrix} 1 & -2 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ -3 & 2 & -1 \end{bmatrix} \\ \Rightarrow & \begin{bmatrix} 1 \times 1 + (-2) \times (-3) & 1 \times 2 + (-2) \times 2 & 1 \times 3 + (-2) \times (-1) \\ 2 \times 1 + 3 \times (-3) & 2 \times 2 + 3 \times 2 & 2 \times 3 + 3 \times (-1) \end{bmatrix} \\ \Rightarrow & \begin{bmatrix} 1 + 6 & 2 - 4 & 3 + 2 \\ 2 - 9 & 4 + 6 & 6 - 3 \end{bmatrix} \end{aligned}$$

On simplification we get,

$$\Rightarrow \begin{bmatrix} 7 & -2 & 5 \\ -7 & 10 & 3 \end{bmatrix}$$

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(iii) Consider

$$\begin{bmatrix} 2 & 3 & 4 \\ 3 & 4 & 5 \\ 4 & 5 & 6 \end{bmatrix} \begin{bmatrix} 1 & -3 & 5 \\ 0 & 2 & 4 \\ 3 & 0 & 5 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} 2 \times 1 + 3 \times 0 + 4 \times 3 & 2 \times (-3) + 3 \times 2 + 4 \times 0 & 2 \times 5 + 3 \times 4 + 4 \times 5 \\ 3 \times 1 + 4 \times 0 + 5 \times 3 & 3 \times (-3) + 4 \times 2 + 5 \times 0 & 3 \times 5 + 4 \times 4 + 5 \times 5 \\ 4 \times 1 + 5 \times 0 + 6 \times 3 & 4 \times (-3) + 5 \times 2 + 6 \times 0 & 4 \times 5 + 5 \times 4 + 6 \times 5 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} 2 + 0 + 12 & -6 + 6 + 0 & 10 + 12 + 20 \\ 3 + 0 + 15 & -9 + 8 + 0 & 15 + 16 + 25 \\ 4 + 0 + 18 & -12 + 10 + 0 & 20 + 20 + 30 \end{bmatrix}$$

On simplification we get,

$$\Rightarrow \begin{bmatrix} 14 & 0 & 42 \\ 18 & -1 & 56 \\ 22 & -2 & 70 \end{bmatrix}$$

2. Show that $AB \neq BA$ in each of the following cases:

$$(i) A = \begin{bmatrix} 5 & -1 \\ 6 & 7 \end{bmatrix} \text{ and } B = \begin{bmatrix} 2 & 1 \\ 3 & 4 \end{bmatrix} \quad (ii) A = \begin{bmatrix} -1 & 1 & 0 \\ 0 & -1 & 1 \\ 2 & 3 & 4 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 0 \\ 1 & 1 & 0 \end{bmatrix}$$
$$(iii) A = \begin{bmatrix} 1 & 3 & 0 \\ 1 & 1 & 0 \\ 4 & 1 & 0 \end{bmatrix} \text{ and } B = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 5 & 1 \end{bmatrix}$$

Solution:

(i) Consider,

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$$\Rightarrow AB = \begin{bmatrix} 10 - 3 & 5 - 4 \\ 12 + 21 & 6 + 28 \end{bmatrix}$$

$$AB = \begin{bmatrix} 5 & -1 \\ 6 & 7 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 3 & 4 \end{bmatrix} \Rightarrow AB = \begin{bmatrix} 7 & 1 \\ 33 & 34 \end{bmatrix} \dots\dots\dots(1)$$

Again consider,

$$BA = \begin{bmatrix} 2 & 1 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} 5 & -1 \\ 6 & 7 \end{bmatrix}$$

$$\Rightarrow BA = \begin{bmatrix} 10 + 6 & -2 + 7 \\ 15 + 24 & -3 + 28 \end{bmatrix}$$

$$\Rightarrow BA = \begin{bmatrix} 16 & 5 \\ 39 & 25 \end{bmatrix} \dots\dots\dots(2)$$

From equation (1) and (2), it is clear that

$$AB \neq BA$$

(ii) Consider,

$$AB = \begin{bmatrix} -1 & 1 & 0 \\ 0 & -1 & 1 \\ 2 & 3 & 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 0 \\ 1 & 1 & 0 \end{bmatrix}$$

$$\Rightarrow AB = \begin{bmatrix} -1 + 0 + 0 & -2 + 1 + 0 & -3 + 0 + 0 \\ 0 + 0 + 1 & 0 - 1 + 1 & 0 + 0 + 0 \\ 2 + 0 + 4 & 4 + 3 + 4 & 6 + 0 + 0 \end{bmatrix}$$

$$\Rightarrow AB = \begin{bmatrix} -1 & -1 & -3 \\ 1 & 0 & 0 \\ 6 & 11 & 6 \end{bmatrix} \dots\dots\dots (1)$$

Now again consider,

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$$BA = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 0 \\ 1 & 1 & 0 \end{bmatrix} \begin{bmatrix} -1 & 1 & 0 \\ 0 & -1 & 1 \\ 2 & 3 & 4 \end{bmatrix}$$
$$\Rightarrow BA = \begin{bmatrix} -1+0+6 & 1-2+9 & 0+2+12 \\ 0+0+0 & 0-1+0 & 0+1+0 \\ -1+0+0 & 1-1+0 & 0+1+0 \end{bmatrix}$$
$$\Rightarrow BA = \begin{bmatrix} 5 & 8 & 14 \\ 0 & -1 & 1 \\ -1 & 0 & 1 \end{bmatrix} \dots\dots\dots(2)$$

From equation (1) and (2), it is clear that

$$AB \neq BA$$

(iii) Consider,

$$AB = \begin{bmatrix} 1 & 3 & 0 \\ 1 & 1 & 0 \\ 4 & 1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 5 & 1 \end{bmatrix}$$
$$\Rightarrow AB = \begin{bmatrix} 0+3+0 & 1+0+0 & 0+0+0 \\ 0+1+0 & 1+0+0 & 0+0+0 \\ 0+1+0 & 4+0+0 & 0+0+0 \end{bmatrix}$$
$$\Rightarrow AB = \begin{bmatrix} 3 & 1 & 0 \\ 1 & 1 & 0 \\ 1 & 4 & 0 \end{bmatrix} \dots\dots\dots(1)$$

Now again consider,

$$BA = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 5 & 1 \end{bmatrix} \begin{bmatrix} 1 & 3 & 0 \\ 1 & 1 & 0 \\ 4 & 1 & 0 \end{bmatrix}$$

$$\Rightarrow BA = \begin{bmatrix} 0+1+0 & 0+1+1 & 0+0+0 \\ 1+0+0 & 3+0+0 & 0+0+0 \\ 0+5+4 & 0+5+1 & 0+0+0 \end{bmatrix}$$

$$\Rightarrow BA = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 3 & 0 \\ 9 & 6 & 0 \end{bmatrix} \dots\dots\dots(2)$$

From equation (1) and (2), it is clear that

$AB \neq BA$

3. Compute the products AB and BA whichever exists in each of the following cases:

$$(i) A = \begin{bmatrix} 1 & -2 \\ 2 & 3 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \end{bmatrix} \quad (ii) A = \begin{bmatrix} 3 & 2 \\ -1 & 0 \\ -1 & 1 \end{bmatrix} \text{ and } B = \begin{bmatrix} 4 & 5 & 6 \\ 0 & 1 & 2 \end{bmatrix}$$

$$(iii) A = \begin{bmatrix} 1 & -1 & 2 & 3 \end{bmatrix} \text{ and } B = \begin{bmatrix} 0 \\ 1 \\ 3 \\ 2 \end{bmatrix} \quad (iv) \begin{bmatrix} a & b \end{bmatrix} \begin{bmatrix} c \\ d \end{bmatrix} + \begin{bmatrix} a & b & c & d \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix}$$

Solution:

(i) Consider,

$$\begin{aligned}AB &= \begin{bmatrix} 1 & -2 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \end{bmatrix} \\ \Rightarrow AB &= \begin{bmatrix} 1-4 & 2-6 & 3-2 \\ 2+6 & 4+9 & 6+3 \end{bmatrix} \\ \Rightarrow AB &= \begin{bmatrix} -3 & -4 & 1 \\ 8 & 13 & 9 \end{bmatrix}\end{aligned}$$

BA does not exist

Because the number of columns in B is greater than the rows in A

(ii) Consider,

$$\begin{aligned}AB &= \begin{bmatrix} 3 & 2 \\ -1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} 4 & 5 & 6 \\ 0 & 1 & 2 \end{bmatrix} \\ \Rightarrow AB &= \begin{bmatrix} 12+0 & 15+2 & 18+4 \\ -4+0 & -5+0 & -6+0 \\ -4+0 & -5+1 & -6+2 \end{bmatrix} \\ \Rightarrow AB &= \begin{bmatrix} 12 & 17 & 22 \\ -4 & -5 & -6 \\ -4 & -4 & -4 \end{bmatrix}\end{aligned}$$

Again consider,

$$\begin{aligned}BA &= \begin{bmatrix} 4 & 5 & 6 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} 3 & 2 \\ -1 & 0 \\ -1 & 1 \end{bmatrix} \\ \Rightarrow BA &= \begin{bmatrix} 12-5-6 & 8+0+6 \\ 0-1-2 & 0+0+2 \end{bmatrix} \\ \Rightarrow BA &= \begin{bmatrix} 1 & 14 \\ -3 & 2 \end{bmatrix}\end{aligned}$$

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(iii) Consider,

$$AB = \begin{bmatrix} 1 & -1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 3 \\ 2 \end{bmatrix}$$

$$AB = [0 + (-1) + 6 + 6]$$

$$AB = 11$$

Again consider,

$$BA = \begin{bmatrix} 0 \\ 1 \\ 3 \\ 2 \end{bmatrix} \begin{bmatrix} 1 & -1 & 2 & 3 \end{bmatrix}$$

$$\Rightarrow BA = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & -1 & 2 & 3 \\ 3 & -3 & 6 & 9 \\ 2 & -2 & 4 & 6 \end{bmatrix}$$

(iv) Consider,

$$(iv) \begin{bmatrix} a & b \end{bmatrix} \begin{bmatrix} c \\ d \end{bmatrix} + \begin{bmatrix} a & b & c & d \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} \Rightarrow [ac + bd] + [a^2 + b^2 + c^2 + d^2]$$
$$[a^2 + b^2 + c^2 + d^2 + ac + bd]$$

4. Show that $AB \neq BA$ in each of the following cases:

$$(i) A = \begin{bmatrix} 1 & 3 & -1 \\ 2 & -1 & -1 \\ 3 & 0 & -1 \end{bmatrix} \text{ and } B = \begin{bmatrix} -2 & 3 & -1 \\ -1 & 2 & -1 \\ -6 & 9 & -4 \end{bmatrix}$$

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Solution:

(i) Consider,

$$\begin{aligned}AB &= \begin{bmatrix} 1 & 3 & -1 \\ 2 & -1 & -1 \\ 3 & 0 & -1 \end{bmatrix} \begin{bmatrix} -2 & 3 & -1 \\ -1 & 2 & -1 \\ -6 & 9 & -4 \end{bmatrix} \\ \Rightarrow AB &= \begin{bmatrix} -2-3+6 & 3+6-9 & -1-3+4 \\ -4+1+6 & 6-2-9 & -2+1+4 \\ -6-0+6 & 9+0-9 & -3-0+4 \end{bmatrix} \\ \Rightarrow AB &= \begin{bmatrix} 1 & 0 & 0 \\ 3 & -5 & 3 \\ 0 & 0 & 1 \end{bmatrix} \dots\dots\dots(1)\end{aligned}$$

Again consider,

$$\begin{aligned}BA &= \begin{bmatrix} -2 & 3 & -1 \\ -1 & 2 & -1 \\ -6 & 9 & -4 \end{bmatrix} \begin{bmatrix} 1 & 3 & -1 \\ 2 & -1 & -1 \\ 3 & 0 & -1 \end{bmatrix} \\ \Rightarrow BA &= \begin{bmatrix} -2+6-3 & -6-3+0 & 2-3+1 \\ -1+4-3 & -3-2+0 & 1-2+1 \\ -6+18-12 & -18-9+0 & 6-9+4 \end{bmatrix} \\ \Rightarrow BA &= \begin{bmatrix} 1 & -9 & 0 \\ 0 & -5 & 0 \\ 0 & -27 & 1 \end{bmatrix} \dots\dots\dots(2)\end{aligned}$$

From equation (1) and (2), it is clear that

$AB \neq BA$

(ii) Consider,

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$$AB = \begin{bmatrix} 10 & -4 & -1 \\ -11 & 5 & 0 \\ 9 & -5 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 1 \\ 3 & 4 & 2 \\ 1 & 3 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 10 - 12 - 1 & 20 - 16 - 3 & 10 - 8 - 2 \\ -11 + 15 + 0 & -22 + 20 + 0 & -11 + 10 + 0 \\ 9 - 15 + 1 & 18 - 20 + 3 & 9 - 10 + 2 \end{bmatrix}$$

$$AB = \begin{bmatrix} -3 & 1 & 0 \\ 4 & -2 & -1 \\ -5 & 1 & 1 \end{bmatrix} \dots\dots(1)$$

Again consider,

$$BA = \begin{bmatrix} 1 & 2 & 1 \\ 3 & 4 & 2 \\ 1 & 3 & 2 \end{bmatrix} \begin{bmatrix} 10 & -4 & -1 \\ -11 & 5 & 0 \\ 9 & -5 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 10 - 22 + 9 & -4 + 10 - 5 & -9 + 0 + 1 \\ 30 - 44 + 10 & -12 + 20 - 10 & -3 + 0 + 2 \\ 10 - 33 + 18 & -4 + 15 - 10 & -1 + 0 + 2 \end{bmatrix}$$

$$BA = \begin{bmatrix} -3 & 1 & 0 \\ 4 & -2 & -1 \\ -5 & 1 & 1 \end{bmatrix} \dots\dots(2)$$

From equation (1) and (2) it is clear that,

$$AB \neq BA$$

5. Evaluate the following:

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$$(i) \left(\begin{bmatrix} 1 & 3 \\ -1 & -4 \end{bmatrix} + \begin{bmatrix} 3 & -2 \\ -1 & 1 \end{bmatrix} \right) \begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{bmatrix} \quad (ii) \begin{bmatrix} 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 0 & 2 \\ 2 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} 2 \\ 4 \\ 6 \end{bmatrix}$$
$$(iii) \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 2 & 3 \end{bmatrix} \left(\begin{bmatrix} 1 & 0 & 2 \\ 2 & 0 & 1 \end{bmatrix} - \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 2 \end{bmatrix} \right)$$

Solution:

(i) Given

$$(i) \left(\begin{bmatrix} 1 & 3 \\ -1 & -4 \end{bmatrix} + \begin{bmatrix} 3 & -2 \\ -1 & 1 \end{bmatrix} \right) \begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{bmatrix}$$

First we have to add first two matrix,

$$\Rightarrow \left(\begin{bmatrix} 1+3 & 3-2 \\ -1-1 & -4+1 \end{bmatrix} \right) \begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} 4 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} 4+2 & 12+4 & 20+6 \\ -2-6 & -6-12 & -10-18 \end{bmatrix}$$

On simplifying, we get

$$\Rightarrow \begin{bmatrix} 6 & 16 & 26 \\ -8 & -18 & -28 \end{bmatrix}$$

(ii) Given,

$$(ii) \begin{bmatrix} 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 0 & 2 \\ 2 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} 2 \\ 4 \\ 6 \end{bmatrix}$$

First we have to multiply first two given matrix,

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$$\Rightarrow [1 + 4 + 0 \quad 0 + 0 + 3 \quad 2 + 2 + 6] \begin{bmatrix} 2 \\ 4 \\ 6 \end{bmatrix}$$

$$\Rightarrow [5 \quad 3 \quad 10] \begin{bmatrix} 2 \\ 4 \\ 6 \end{bmatrix}$$

$$\Rightarrow [10 + 12 + 60]$$

$$= 82$$

(iii) Given

$$(iii) \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 2 & 3 \end{bmatrix} \left(\begin{bmatrix} 1 & 0 & 2 \\ 2 & 0 & 1 \end{bmatrix} - \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 2 \end{bmatrix} \right)$$

First we have subtract the matrix which is inside the bracket,

$$\Rightarrow \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & -1 & 0 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 1-1 & -1+0 & 0+1 \\ 0+2 & 0+0 & 0-2 \\ 2+3 & -2+0 & 0-3 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} 1-0 & 0-1 & 2-2 \\ 2-1 & 0-0 & 1-2 \end{bmatrix} \Rightarrow \begin{bmatrix} 0 & -1 & 1 \\ 2 & 0 & -2 \\ 5 & -2 & -3 \end{bmatrix}$$

6.If $A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, $B = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$ and $C = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$, show that $A^2 = B^2 = C^2 = I_2$

Solution:

Given

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$$A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \text{ and } C = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

We know that,

$$A^2 = AA$$

$$\Rightarrow A^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 1+0 & 0+1 \\ 0+0 & 0+1 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \dots\dots\dots(1)$$

Again we know that,

$$B^2 = BB$$

$$\Rightarrow B^2 = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

$$\Rightarrow B^2 = \begin{bmatrix} 1+0 & 0-0 \\ 0-0 & 0+1 \end{bmatrix}$$

$$\Rightarrow B^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \dots\dots\dots(2)$$

Now, consider,

$$C^2 = CC$$

$$\Rightarrow B^2 = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$\Rightarrow B^2 = \begin{bmatrix} 0+1 & 0+0 \\ 0+0 & 1+0 \end{bmatrix}$$

$$\Rightarrow B^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \dots\dots\dots(3)$$

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We have,

$$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \dots\dots\dots(4)$$

Now, from equation (1), (2), (3) and (4), it is clear that $A^2 = B^2 = C^2 = I_2$

7.If $A = \begin{bmatrix} 2 & -1 \\ 3 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 0 & 4 \\ -1 & 7 \end{bmatrix}$, find $3A^2 - 2B + I$

Solution:

Given

7.If $A = \begin{bmatrix} 2 & -1 \\ 3 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 0 & 4 \\ -1 & 7 \end{bmatrix}$, find $3A^2 - 2B + I$

Consider,

$$A^2 = A A$$

$$\Rightarrow A^2 = \begin{bmatrix} 2 & -1 \\ 3 & 2 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 3 & 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 4 - 3 & -2 - 2 \\ 6 + 6 & -3 + 4 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 1 & -4 \\ 12 & 1 \end{bmatrix}$$

Now we have to find,

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$$3A^2 - 2B + I$$

$$\Rightarrow 3A^2 - 2B + I = 3 \begin{bmatrix} 1 & -4 \\ 12 & 1 \end{bmatrix} - 2 \begin{bmatrix} 0 & 4 \\ -1 & 7 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow 3A^2 - 2B + I = \begin{bmatrix} 3 & -12 \\ 36 & 3 \end{bmatrix} - \begin{bmatrix} 0 & 8 \\ -2 & 14 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow 3A^2 - 2B + I = \begin{bmatrix} 3 - 0 + 1 & -12 - 8 + 0 \\ 36 + 2 + 0 & 3 - 14 + 1 \end{bmatrix}$$

$$\Rightarrow 3A^2 - 2B + I = \begin{bmatrix} 4 & -20 \\ 38 & -10 \end{bmatrix}$$

8.If $A = \begin{bmatrix} 4 & 2 \\ -1 & 1 \end{bmatrix}$, prove that $(A - 2I)(A - 3I) = 0$.

Solution:

Given

8.If $A = \begin{bmatrix} 4 & 2 \\ -1 & 1 \end{bmatrix}$, prove that $(A - 2I)(A - 3I) = 0$.

Consider,

$$\Rightarrow (A-2I)(A-3I) = \left(\begin{bmatrix} 4 & 2 \\ -1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \right) \left(\begin{bmatrix} 4 & 2 \\ -1 & 1 \end{bmatrix} - 3 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \right)$$

$$\Rightarrow (A-2I)(A-3I) = \left(\begin{bmatrix} 4 & 2 \\ -1 & 1 \end{bmatrix} - \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix} \right) \left(\begin{bmatrix} 4 & 2 \\ -1 & 1 \end{bmatrix} - \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix} \right)$$

$$\Rightarrow (A-2I)(A-3I) = \begin{bmatrix} 4-2 & 2-0 \\ -1-0 & 1-2 \end{bmatrix} \begin{bmatrix} 4-3 & 2-0 \\ -1-0 & 1-3 \end{bmatrix}$$

$$\Rightarrow (A-2I)(A-3I) = \begin{bmatrix} 2 & 2 \\ -1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ -1 & -2 \end{bmatrix}$$

$$\Rightarrow (A-2I)(A-3I) = \begin{bmatrix} 2-2 & 4-4 \\ -1+1 & -2+2 \end{bmatrix}$$

$$\Rightarrow (A-2I)(A-3I) = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\Rightarrow (A-2I)(A-3I) = 0$$

Hence the proof.

9.If $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$, show that $A^2 = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$ and $A^3 = \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix}$

Solution:

Given,

9.If $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$, show that $A^2 = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$ and $A^3 = \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix}$

Consider,

$$A^2 = A A$$

$$A^2 = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 1+0 & 1+1 \\ 0+0 & 0+1 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$

Again consider,

$$A^3 = A^2 A$$

$$A^3 = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow A^3 = \begin{bmatrix} 1+0 & 1+2 \\ 0+0 & 0+1 \end{bmatrix}$$

$$A^3 = \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix}$$

Hence the proof.

10.If $A = \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix}$, show that $A^2 = 0$

Solution:

Given,

10.If $A = \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix}$, show that $A^2 = 0$

Consider,

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$$A^2 = A A$$

$$\Rightarrow A^2 = \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix} \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix} \Rightarrow A^2 \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$
$$\Rightarrow A^2 = \begin{bmatrix} a^2b^2 - a^2b^2 & ab^3 - ab^3 \\ -a^3b + a^3b & -a^2b^2 + a^2b^2 \end{bmatrix} \Rightarrow A^2 = 0$$

Hence the proof.

11. If $A = \begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$, find A^2

Solution:

Given,

11. If $A = \begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$, find A^2

Consider,

$$A^2 = A A$$

$$\Rightarrow A^2 = \begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix} \begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$$
$$\Rightarrow A^2 = \begin{bmatrix} \cos^2(2\theta) - \sin^2(2\theta) & \cos(2\theta)\sin 2\theta + \cos(2\theta)\sin 2\theta \\ -\cos(2\theta)\sin 2\theta - \sin 2\theta\cos 2\theta & -\sin^2(2\theta) + \cos^2(2\theta) \end{bmatrix}$$

We know that,

$$\cos^2\theta - \sin^2\theta = \cos^2(2\theta) \Rightarrow A^2 = \begin{bmatrix} \cos(2 \times 2\theta) & 2 \sin 2\theta \cos 2\theta \\ -2 \sin 2\theta \cos(2\theta) & \cos(2 \times 2\theta) \end{bmatrix}$$

Again we have,

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$$\Rightarrow A^2 = \begin{bmatrix} \cos 4\theta & \sin(2 \times 2\theta) \\ -\sin(2 \times 2\theta) & \cos 4\theta \end{bmatrix}$$

$$\sin 2\theta = 2 \sin\theta \cos\theta \Rightarrow A^2 = \begin{bmatrix} \cos 4\theta & \sin 4\theta \\ -\sin 4\theta & \cos 4\theta \end{bmatrix}$$

12. If $A = \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} -1 & 3 & 5 \\ 1 & -3 & -5 \\ -1 & 3 & 5 \end{bmatrix}$ show that $AB = BA = 0_{3 \times 3}$

Solution:

Given,

12. If $A = \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} -1 & 3 & 5 \\ 1 & -3 & -5 \\ -1 & 3 & 5 \end{bmatrix}$ show that $AB =$
 $BA = 0_{3 \times 3}$

Consider,

$$\begin{aligned} AB &= \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix} \begin{bmatrix} -1 & 3 & 5 \\ 1 & -3 & -5 \\ -1 & 3 & 5 \end{bmatrix} \\ &= \begin{bmatrix} -2 - 3 + 5 & 6 + 9 - 15 & 5 + 15 - 20 \\ 1 + 4 - 5 & -3 - 12 + 15 & -5 - 15 + 20 \\ -1 - 3 + 4 & 3 + 9 - 12 & 5 + 15 - 20 \end{bmatrix} \\ &= \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \end{aligned}$$

$$AB = 0_{3 \times 3} \dots\dots(1)$$

Again consider,

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$$\begin{aligned}BA &= \begin{bmatrix} -1 & 3 & 5 \\ 1 & -3 & -5 \\ -1 & 3 & 5 \end{bmatrix} \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix} \\&= \begin{bmatrix} -2 - 3 + 5 & 3 + 12 - 15 & 5 + 15 - 20 \\ 2 + 3 - 5 & -3 - 12 + 15 & -5 - 15 + 20 \\ -2 - 3 + 5 & 3 + 9 - 12 & 5 + 15 - 20 \end{bmatrix} \\&= \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}\end{aligned}$$

$$BA = 0_{3 \times 3} \dots\dots(2)$$

From equation (1) and (2) $AB = BA = 0_{3 \times 3}$

13. If $A = \begin{bmatrix} 0 & c & -b \\ -c & 0 & a \\ b & -a & 0 \end{bmatrix}$ and $B = \begin{bmatrix} a^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{bmatrix}$ show that $AB = BA = 0_{3 \times 3}$

Solution:

Given

13. If $A = \begin{bmatrix} 0 & c & -b \\ -c & 0 & a \\ b & -a & 0 \end{bmatrix}$ and $B = \begin{bmatrix} a^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{bmatrix}$ show that $AB = BA = 0_{3 \times 3}$

Consider,

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$$AB = \begin{bmatrix} 0 & c & -b \\ -c & 0 & a \\ b & -a & 0 \end{bmatrix} \begin{bmatrix} a^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{bmatrix}$$

$$\Rightarrow AB = \begin{bmatrix} 0 + abc - abc & 0 + b^2c - b^2c & 0 + bc^2 - bc^2 \\ -a^2c + 0 + a^2c & -abc + 0 + abc & -ac^2 + 0 + ac^2 \\ a^2b - a^2b + 0 & ab^2 - ab^2 + 0 & abc - abc + 0 \end{bmatrix}$$

$$\Rightarrow AB = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\Rightarrow AB = O_{3 \times 3} \dots (1)$$

Again consider,

$$BA = \begin{bmatrix} a^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{bmatrix} \begin{bmatrix} 0 & c & -b \\ -c & 0 & a \\ b & -a & 0 \end{bmatrix}$$

$$\Rightarrow BA = \begin{bmatrix} 0 - abc + abc & a^2c + 0 - a^2c & -a^2b + a^2b + 0 \\ 0 - b^2c + b^2c & abc + 0 - abc & -ab^2 + ab^2 + 0 \\ 0 - bc^2 + bc^2 & ac^2 + 0 - ac^2 & -abc + abc + 0 \end{bmatrix} \Rightarrow BA = O_{3 \times 3} \dots (2)$$

From equation (1) and (2) $AB = BA = O_{3 \times 3}$

14. If $A = \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{bmatrix}$ show that $AB = A$ and $BA = B$.

Solution:

Given

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14. If $A = \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{bmatrix}$ show that $AB = A$ and $BA = B$.

Now consider,

$$\begin{aligned} AB &= \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix} \begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{bmatrix} \\ &= \begin{bmatrix} 4 + 3 - 5 & -4 - 9 + 10 & -8 - 12 + 15 \\ -2 - 4 + 5 & 2 + 12 - 10 & 4 + 16 - 15 \\ 2 + 3 - 4 & -2 - 9 + 18 & -4 - 12 + 12 \end{bmatrix} \\ &= \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix} \end{aligned}$$

Therefore $AB = A$

Again consider, BA we get,

$$\begin{aligned} BA &= \begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{bmatrix} \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix} \\ &= \begin{bmatrix} 4 + 2 - 4 & -6 - 8 + 12 & -10 - 10 + 16 \\ -2 - 3 + 4 & 3 + 12 - 12 & 5 + 15 - 16 \\ 2 + 2 - 3 & -3 - 8 + 9 & -5 - 10 + 12 \end{bmatrix} \\ &= \begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{bmatrix} \end{aligned}$$

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Hence $BA = B$

Hence the proof.

15. Let $A = \begin{bmatrix} -1 & 1 & -1 \\ 3 & -3 & 3 \\ 5 & 5 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 0 & 4 & 3 \\ 1 & -3 & -3 \\ -1 & 4 & 4 \end{bmatrix}$, compute $A^2 - B^2$.

Solution:

Given,

15. Let $A = \begin{bmatrix} -1 & 1 & -1 \\ 3 & -3 & 3 \\ 5 & 5 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 0 & 4 & 3 \\ 1 & -3 & -3 \\ -1 & 4 & 4 \end{bmatrix}$, compute $A^2 - B^2$.

Consider,

$$A^2 = \begin{bmatrix} -1 & 1 & -1 \\ 3 & -3 & 3 \\ 5 & 5 & 5 \end{bmatrix} \begin{bmatrix} -1 & 1 & -1 \\ 3 & -3 & 3 \\ 5 & 5 & 5 \end{bmatrix}$$
$$= \begin{bmatrix} 1 + 3 + 5 & -1 - 3 - 5 & 1 + 3 - 5 \\ -3 - 9 + 15 & 3 + 9 + 15 & -3 - 9 + 15 \\ -5 + 15 + 25 & 5 - 15 + 25 & -5 + 15 + 25 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} -1 & 9 & -1 \\ 3 & 27 & 3 \\ 35 & 15 & 35 \end{bmatrix} \dots\dots(1)$$

Now again consider, B^2

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$$\begin{aligned} B^2 &= \begin{bmatrix} 0 & 4 & 3 \\ 1 & -3 & -3 \\ -1 & 4 & 4 \end{bmatrix} \begin{bmatrix} 0 & 4 & 3 \\ 1 & -3 & -3 \\ -1 & 4 & 4 \end{bmatrix} \\ &= \begin{bmatrix} 0+4+3 & 0-12+12 & 0-12+12 \\ 0-3+3 & 4+9-12 & 3+9-12 \\ 0+4-4 & -4-12+16 & -3-12+16 \end{bmatrix} \\ &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \dots\dots(2) \end{aligned}$$

Now by subtracting equation (2) from equation (1) we get,

$$\begin{aligned} A^2 - B^2 &= \begin{bmatrix} -1 & 9 & -1 \\ 3 & 27 & 3 \\ 35 & 15 & 35 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \\ &= \begin{bmatrix} -2 & 9 & -1 \\ 3 & 26 & 3 \\ 35 & 15 & 34 \end{bmatrix} \end{aligned}$$

16. For the following matrices verify the associativity of matrix multiplication i.e. (AB) C = A (BC)

$$(i) A = \begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 0 & 3 \end{bmatrix}, \text{ and } C = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$(ii) A = \begin{bmatrix} 4 & 2 & 3 \\ 1 & 1 & 2 \\ 3 & 0 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & -1 & 1 \\ 0 & 1 & 2 \\ 2 & -1 & 1 \end{bmatrix}, \text{ and } C = \begin{bmatrix} 1 & 2 & -1 \\ 3 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

Solution:

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(i) Given

$$(i) A = \begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 0 & 3 \end{bmatrix}, \text{ and } C = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

Consider,

$$(AB)C = \left(\begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 0 & 3 \end{bmatrix} \right) \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 - 2 + 0 & 0 + 4 + 0 \\ -1 + 0 + 0 & 0 + 0 + 3 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$= \begin{bmatrix} -1 & 4 \\ -1 & 3 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$= \begin{bmatrix} -1 - 4 \\ -1 - 3 \end{bmatrix}$$

$$(AB)C = \begin{bmatrix} -5 \\ -4 \end{bmatrix} \dots\dots(1)$$

Now consider RHS,

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$$A(BC) = \begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & 1 \end{bmatrix} \left(\begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 0 & 3 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 + 0 \\ -1 - 2 \\ 0 - 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 2 & 0 \\ -1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ -3 \\ -3 \end{bmatrix}$$

$$= \begin{bmatrix} 1 - 6 + 0 \\ -1 + 0 - 3 \end{bmatrix}$$

$$A(BC) = \begin{bmatrix} -5 \\ -4 \end{bmatrix} \dots\dots(2)$$

From equation (1) and (2), it is clear that $(AB)C = A(BC)$

(ii) Given,

$$(ii) A = \begin{bmatrix} 4 & 2 & 3 \\ 1 & 1 & 2 \\ 3 & 0 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & -1 & 1 \\ 0 & 1 & 2 \\ 2 & -1 & 1 \end{bmatrix}, \text{ and } C = \begin{bmatrix} 1 & 2 & -1 \\ 3 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

Consider the LHS,

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$$\begin{aligned}(AB)C &= \begin{bmatrix} 4 & 2 & 3 \\ 1 & 1 & 2 \\ 3 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & -1 & 1 \\ 0 & 1 & 2 \\ 2 & -1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & -1 \\ 3 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \\&= \begin{bmatrix} 4 + 0 + 6 & -4 + 2 - 3 & 4 + 4 + 3 \\ 1 + 0 + 4 & -1 + 1 - 2 & 1 + 2 + 2 \\ 3 + 0 + 2 & -3 + 0 - 1 & 3 + 0 + 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & -1 \\ 3 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \\&= \begin{bmatrix} 10 & -5 & 11 \\ 5 & -2 & 5 \\ 5 & -4 & 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -1 \\ 3 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \\&= \begin{bmatrix} 10 - 15 + 0 & 20 + 0 + 0 & -10 + 5 + 11 \\ 5 - 6 + 0 & 10 + 0 + 0 & -5 - 2 + 5 \\ 5 - 12 + 0 & 10 + 0 + 0 & -5 - 4 + 4 \end{bmatrix} \\(AB)C &= \begin{bmatrix} -5 & 20 & -4 \\ -1 & 10 & -2 \\ -7 & 10 & -5 \end{bmatrix} \dots\dots(1)\end{aligned}$$

Now consider RHS,

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$$\begin{aligned}
 A(BC) &= \begin{bmatrix} 4 & 2 & 3 \\ 1 & 1 & 2 \\ 3 & 0 & 1 \end{bmatrix} \left(\begin{bmatrix} 1 & -1 & 1 \\ 0 & 1 & 2 \\ 2 & -1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & -1 \\ 3 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \right) \\
 &= \begin{bmatrix} 4 & 2 & 3 \\ 1 & 1 & 2 \\ 3 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1-3+0 & 2+0+0 & -1-1+1 \\ 0+3+0 & 0+0+0 & 0+1+2 \\ 2-3+0 & 4+0+0 & -2-1+1 \end{bmatrix} \\
 &= \begin{bmatrix} 4 & 2 & 3 \\ 1 & 1 & 2 \\ 3 & 0 & 1 \end{bmatrix} \begin{bmatrix} -2 & 2 & 1 \\ 3 & 0 & 3 \\ -1 & 4 & -2 \end{bmatrix} \\
 &= \begin{bmatrix} -8+6-3 & 8+0+12 & -4+6-6 \\ -2+3-2 & 2+0+8 & -1+3-4 \\ -6+0-1 & 6+0+4 & -3+0-2 \end{bmatrix} \\
 A(BC) &= \begin{bmatrix} -5 & 20 & -4 \\ -1 & 10 & -2 \\ -7 & 10 & -5 \end{bmatrix} \dots\dots(2)
 \end{aligned}$$

From equation (1) and (2), it is clear that $(AB)C = A(BC)$

17. For the following matrices verify the distributivity of matrix multiplication over matrix addition i.e. $A(B + C) = AB + AC$.

$$\begin{aligned}
 (i) \quad A &= \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix}, \quad B = \begin{bmatrix} -1 & 0 \\ 2 & 1 \end{bmatrix}, \quad \text{and } C = \begin{bmatrix} 0 & 1 \\ 1 & -1 \end{bmatrix} \\
 (ii) \quad A &= \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ -1 & 2 \end{bmatrix}, \quad B = \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix}, \quad \text{and } C = \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}
 \end{aligned}$$

Solution:

(i) Given

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$$(i) A = \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix}, B = \begin{bmatrix} -1 & 0 \\ 2 & 1 \end{bmatrix}, \text{ and } C = \begin{bmatrix} 0 & 1 \\ 1 & -1 \end{bmatrix}$$

Consider LHS,

$$\begin{aligned} A(B + C) &= \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \left(\begin{bmatrix} -1 & 0 \\ 2 & 1 \end{bmatrix} + \begin{bmatrix} 0 & 1 \\ 1 & -1 \end{bmatrix} \right) \\ &= \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} -1 + 0 & 0 + 1 \\ 2 + 1 & 1 - 1 \end{bmatrix} &= \begin{bmatrix} -1 - 3 & 1 + 0 \\ 0 + 6 & 0 + 0 \end{bmatrix} \\ &= \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 3 & 0 \end{bmatrix} &A(B + C) = \begin{bmatrix} -4 & 1 \\ 6 & 0 \end{bmatrix} \dots\dots(1) \end{aligned}$$

Now consider RHS,

$$\begin{aligned} AB + AC &= \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} -1 & 0 \\ 2 & 1 \end{bmatrix} + \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & -1 \end{bmatrix} \\ &= \begin{bmatrix} -1 - 2 & 0 - 1 \\ 0 + 4 & 0 + 2 \end{bmatrix} + \begin{bmatrix} 0 + -1 & 1 + 1 \\ 0 + 2 & 0 - 2 \end{bmatrix} \\ &= \begin{bmatrix} -3 & -1 \\ 4 & 2 \end{bmatrix} + \begin{bmatrix} -1 & 2 \\ 2 & -2 \end{bmatrix} \\ &= \begin{bmatrix} -3 - 1 & -1 + 2 \\ 4 + 2 & 2 - 2 \end{bmatrix} \\ AB + AC &= \begin{bmatrix} -4 & 1 \\ 6 & 0 \end{bmatrix} \dots\dots(2) \end{aligned}$$

From equation (1) and (2), it is clear that $A(B + C) = AB + AC$

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(ii) Given,

$$(ii) A = \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ -1 & 2 \end{bmatrix}, B = \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix}, \text{ and } C = \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}$$

Consider the LHS

$$= \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1 & 2 \end{bmatrix}$$

$$A(B + C) = \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} + \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 2+1 & 0+1 \\ 1+1 & 0+1 \\ -1+2 & 0+1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 0+1 & 1+1 \\ 1+0 & 1+1 \end{bmatrix} \qquad A(B + C) = \begin{bmatrix} 1 & -2 \\ 2 & 2 \\ 1 & 4 \end{bmatrix} \dots\dots(1)$$

Now consider RHS,

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$$AB + AC = \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} + \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 + 1 & 2 - 1 \\ 0 + 1 & 1 + 1 \\ 0 + 2 & -1 + 2 \end{bmatrix} + \begin{bmatrix} 2 + 0 & -2 - 1 \\ 1 + 0 & -1 + 1 \\ -1 + 0 & 1 + 2 \end{bmatrix}$$

$$= \begin{bmatrix} -1 & 1 \\ 1 & 2 \\ 2 & 1 \end{bmatrix} + \begin{bmatrix} 2 & -3 \\ 1 & 0 \\ -1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} -1 + 2 & 1 - 3 \\ 1 + 1 & 2 + 0 \\ 2 - 1 & 1 + 3 \end{bmatrix}$$

$$AB + AC = \begin{bmatrix} 1 & -2 \\ 2 & 2 \\ 1 & 4 \end{bmatrix} \dots\dots(2)$$

18. If $A = \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}$, $B = \begin{bmatrix} 0 & 5 & -4 \\ -2 & 1 & 3 \\ -1 & 0 & 2 \end{bmatrix}$, and $C = \begin{bmatrix} 1 & 5 & 2 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}$,

verify that $A(B - C) = AB - AC$.

Solution:

Given,

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$$A = \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}, B = \begin{bmatrix} 0 & 5 & -4 \\ -2 & 1 & 3 \\ -1 & 0 & 2 \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 5 & 2 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}$$

$$A(B - C) = \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix} \left(\begin{bmatrix} 0 & 5 & -4 \\ -2 & 1 & 3 \\ -1 & 0 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 5 & 2 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 0 & 6 \\ -1 & 0 & 3 \\ -1 & 1 & 1 \end{bmatrix}$$

Consider the LHS,

$$A(B - C) = \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix} \left(\begin{bmatrix} 0 & 5 & -4 \\ -2 & 1 & 3 \\ -1 & 0 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 5 & 2 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 0 & 6 \\ -1 & 0 & 3 \\ -1 & 1 & 1 \end{bmatrix}$$

$$A(B - C) = \begin{bmatrix} 1 & -2 & -8 \\ -2 & 0 & -21 \\ 0 & 1 & 16 \end{bmatrix}$$

Now consider RHS

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$$\begin{aligned}AB - AC &= \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0 & 5 & -4 \\ -2 & 1 & 3 \\ -1 & 0 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 5 & 2 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix} \\&= \begin{bmatrix} 2 & 5 & -8 \\ 2 & 14 & -15 \\ -3 & -9 & 13 \end{bmatrix} - \begin{bmatrix} 1 & 7 & 0 \\ 4 & 14 & 6 \\ -3 & -10 & -3 \end{bmatrix} \\&= \begin{bmatrix} 1 & -2 & -8 \\ -2 & 0 & -21 \\ 0 & 1 & 16 \end{bmatrix}\end{aligned}$$

From the above equations LHS = RHS

Therefore, $A(B - C) = AB - AC$.

19. Compute the elements a_{43} and a_{22} of the matrix:

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 2 & 0 & 2 \\ 0 & 3 & 2 \\ 4 & 0 & 4 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ -3 & 2 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 & 2 & -2 \\ 3 & -3 & 4 & -4 & 0 \end{bmatrix}$$

Solution:

Given

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 2 & 0 & 2 \\ 0 & 3 & 2 \\ 4 & 0 & 4 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ -3 & 2 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 & 2 & -2 \\ 3 & -3 & 4 & -4 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} -3 & 2 \\ 12 & 4 \\ -1 & 12 \\ 24 & 8 \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 & 2 & -2 \\ 3 & -3 & 4 & -4 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} 6 & -9 & 11 & -14 & 6 \\ 12 & 0 & 4 & 8 & -24 \\ 36 & -37 & 49 & -50 & 2 \\ 24 & 0 & 8 & 16 & -48 \end{bmatrix}$$

From the above matrix, $a_{43} = 8$ and $a_{22} = 0$

20. If $A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix}$ and I is the identity matrix of order 3, that $A^3 = pI + qA + rA^2$

Solution:

Given

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix}$$

Consider,

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$$A^2 = A.A$$

$$= \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix}$$

$$= \begin{bmatrix} 0 + 0 + 0 & 0 + 0 + 0 & 0 + 1 + 0 \\ 0 + 0 + p & 0 + 0 + q & 0 + 0 + r \\ 0 + 0 + pr & p + 0 + qr & 0 + q + r^2 \end{bmatrix}$$

$$A^3 = A^2.A$$

$$= \begin{bmatrix} 0 + 0 + 0 & 0 + 0 + 0 & 0 + 1 + 0 \\ 0 + 0 + p & 0 + 0 + q & 0 + 0 + r \\ 0 + 0 + pr & p + 0 + qr & 0 + q + r^2 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix}$$

$$= \begin{bmatrix} 0 + 0 + p & 0 + 0 + q & 0 + 0 + r \\ 0 + 0 + pr & p + 0 + qr & 0 + q + r^2 \\ 0 + 0 + pq + pr^2 & pr + 0 + q^2 + qr^2 & 0 + p + qr + qr + r^2 \end{bmatrix}$$

Again consider,

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$$A^3 = A^2 \cdot A$$

$$\begin{aligned}
 &= \begin{bmatrix} 0+0+0 & 0+0+0 & 0+1+0 \\ 0+0+p & 0+0+q & 0+0+r \\ 0+0+pr & p+0+qr & 0+q+r^2 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix} \\
 &= \begin{bmatrix} 0+0+p & 0+0+q & 0+0+r \\ 0+0+pr & p+0+qr & 0+q+r^2 \\ 0+0+pq+pr^2 & pr+0+q^2+qr^2 & 0+p+qr+qr+r^2 \end{bmatrix} \\
 &= \begin{bmatrix} p & q & r \\ pr & p+qr & q+r^2 \\ pq+pr^2 & pr+q^2+qr^2 & p+2qr+r^2 \end{bmatrix}
 \end{aligned}$$

Now, consider the RHS

$$\begin{aligned}
 &pI + qA + rA^2 \\
 &= p \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + q \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix} + r \begin{bmatrix} 0 & 0 & 1 \\ p & q & r \\ pr & p+qr & q+r^2 \end{bmatrix} \\
 &= \begin{bmatrix} p & q & r \\ pr & p+qr & q+r^2 \\ pq+pr^2 & pr+q^2+qr^2 & p+2qr+r^2 \end{bmatrix}
 \end{aligned}$$

Therefore, $A^3 = pI + qA + rA^2$

Hence the proof.

21. If ω is a complex cube root of unity, show that

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$$\left(\begin{bmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{bmatrix} + \begin{bmatrix} \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \\ \omega & \omega^2 & 1 \end{bmatrix} \right) \begin{bmatrix} 1 \\ \omega \\ \omega^2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Solution:

Given

$$\left(\begin{bmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{bmatrix} + \begin{bmatrix} \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \\ \omega & \omega^2 & 1 \end{bmatrix} \right) \begin{bmatrix} 1 \\ \omega \\ \omega^2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

It is also given that ω is a complex cube root of unity,

Consider the LHS,

$$= \begin{bmatrix} 1 + \omega & \omega + \omega^2 & \omega^2 + 1 \\ \omega + \omega^2 & \omega^2 + 1 & 1 + \omega \\ \omega^2 + \omega & 1 + \omega^2 & \omega + 1 \end{bmatrix} \begin{bmatrix} 1 \\ \omega \\ \omega^2 \end{bmatrix}$$

We know that $1 + \omega + \omega^2 = 0$ and $\omega^3 = 1$

$$= \begin{bmatrix} -\omega^2 & -1 & -\omega \\ -1 & -\omega & -\omega^2 \\ -1 & -\omega & -\omega^2 \end{bmatrix} \begin{bmatrix} 1 \\ \omega \\ \omega^2 \end{bmatrix}$$

Now by simplifying we get,

$$= \begin{bmatrix} -\omega^2 & -\omega & -\omega^3 \\ -1 & -\omega^2 & -\omega^4 \\ -1 & -\omega^2 & -\omega^4 \end{bmatrix}$$

Again by substituting $1 + \omega + \omega^2 = 0$ and $\omega^3 = 1$ in above matrix we get,

$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

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Therefore LHS = RHS

Hence the proof.

Solution:

Given,

22. If $A = \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix}$, show that $A^2 = A$

Consider A^2

$$A^2 = A.A$$

$$= \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix} \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix}$$

$$= \begin{bmatrix} 4 + 3 - 5 & -6 - 12 + 15 & -10 - 15 + 20 \\ -2 - 4 + 5 & 3 + 16 - 15 & 5 + 20 - 20 \\ 2 + 3 - 4 & -3 - 12 + 12 & -5 - 15 + 16 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -3 & -5 \\ -1 & 4 & 5 \\ 1 & -3 & -4 \end{bmatrix} = A$$

Therefore $A^2 = A$

23. If $A = \begin{bmatrix} 4 & -1 & -4 \\ 3 & 0 & -4 \\ 3 & -1 & -3 \end{bmatrix}$, show that $A^2 = I_3$

Solution:

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Given

$$23. \text{ If } A = \begin{bmatrix} 4 & -1 & -4 \\ 3 & 0 & -4 \\ 3 & -1 & -3 \end{bmatrix}, \text{ show that } A^2 = I_3$$

Consider A^2 ,

$$A^2 = A.A$$

$$= \begin{bmatrix} 4 & -1 & -4 \\ 3 & 0 & -4 \\ 3 & -1 & -3 \end{bmatrix} \begin{bmatrix} 4 & -1 & -4 \\ 3 & 0 & -4 \\ 3 & -1 & -3 \end{bmatrix}$$

$$= \begin{bmatrix} 16 - 3 - 12 & -4 + 0 + 4 & 16 + 4 + 12 \\ 12 + 0 - 12 & -3 + 0 + 4 & -12 + 0 + 12 \\ 12 - 3 - 9 & -3 + 0 + 3 & -12 + 4 + 9 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = I_3$$

Hence $A^2 = I_3$

$$24. (i) \text{ If } \begin{bmatrix} 1 & 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = 0, \text{ find } x.$$

$$(ii) \text{ If } \begin{bmatrix} 2 & 3 \\ 5 & 7 \end{bmatrix} \begin{bmatrix} 1 & -3 \\ -2 & 4 \end{bmatrix} = \begin{bmatrix} -4 & 6 \\ -9 & x \end{bmatrix}, \text{ find } x.$$

Solution:

(i) Given

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24. (i) If $\begin{bmatrix} 1 & 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = 0$, find x .

(ii) If $\begin{bmatrix} 2 & 3 \\ 5 & 7 \end{bmatrix} \begin{bmatrix} 1 & -3 \\ -2 & 4 \end{bmatrix} = \begin{bmatrix} -4 & 6 \\ -9 & x \end{bmatrix}$, find x .

$$\Rightarrow [1 + 2x + 0 \quad x + 0 + 2 \quad 2 + 1 + 0] \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = 0$$

$$\Rightarrow [2x + 4 \quad x + 2 \quad 2x + 4] \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = 0$$

$$= [2x + 1 + 2 + x + 3] = 0$$

$$= [3x + 6] = 0$$

$$= 3x = -6$$

$$x = -6/3$$

$$x = -2$$

(ii) Given,

24. (i) If $\begin{bmatrix} 1 & 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = 0$, find x .

(ii) If $\begin{bmatrix} 2 & 3 \\ 5 & 7 \end{bmatrix} \begin{bmatrix} 1 & -3 \\ -2 & 4 \end{bmatrix} = \begin{bmatrix} -4 & 6 \\ -9 & x \end{bmatrix}$, find x .

$$\Rightarrow \begin{bmatrix} 2 - 6 & -6 + 12 \\ 5 - 14 & -15 + 28 \end{bmatrix} = \begin{bmatrix} -4 & 6 \\ -9 & x \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} -4 & 6 \\ -9 & 13 \end{bmatrix} = \begin{bmatrix} -4 & 6 \\ -9 & x \end{bmatrix}$$

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On comparing the above matrix we get,

$$x = 13$$

25. If $\begin{bmatrix} x & 4 & 1 \end{bmatrix} \begin{bmatrix} 2 & 1 & 2 \\ 1 & 0 & 2 \\ 0 & 2 & -4 \end{bmatrix} \begin{bmatrix} x \\ 4 \\ -1 \end{bmatrix} = 0$, find x .

Solution:

Given

24. If $\begin{bmatrix} x & 4 & 1 \end{bmatrix} \begin{bmatrix} 2 & 1 & 2 \\ 1 & 0 & 2 \\ 0 & 2 & -4 \end{bmatrix} \begin{bmatrix} x \\ 4 \\ -1 \end{bmatrix} = 0$, find x .

$$\Rightarrow [2x + 4 + 0 \quad x + 0 + 2 \quad 2x + 8 - 4] \begin{bmatrix} x \\ 4 \\ -1 \end{bmatrix} = 0$$

$$\Rightarrow [2x + 4 \quad x + 2 \quad 2x + 4] \begin{bmatrix} x \\ 4 \\ -1 \end{bmatrix} = 0$$

$$\Rightarrow [(2x + 4)x + 4(x + 2) - 1(2x + 4)] = 0$$

$$\Rightarrow 2x^2 + 4x + 4x + 8 - 2x - 4 = 0$$

$$\Rightarrow 2x^2 + 6x + 4 = 0$$

$$\Rightarrow 2x^2 + 2x + 4x + 4 = 0$$

$$\Rightarrow 2x(x + 1) + 4(x + 1) = 0$$

$$\Rightarrow (x + 1)(2x + 4) = 0$$

$$\Rightarrow x = -1 \text{ or } x = -2$$

Hence, $x = -1$ or $x = -2$

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26. If $\begin{bmatrix} 1 & -1 & x \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 \\ 2 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} = 0$, find x .

Solution:

Given

$$\begin{bmatrix} 1 & -1 & x \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 \\ 2 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} = 0$$

By multiplying we get,

$$\Rightarrow \begin{bmatrix} 0 - 2 + x & x & (-1) - 3 + x \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} = 0$$

$$\Rightarrow \begin{bmatrix} x - 2 & x & x - 4 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} = 0$$

$$[(x - 2) \times 0 + x \times 1 + (x - 4) \times 1] = 0$$

$$\Rightarrow x + x - 4 = 0$$

$$\Rightarrow 2x = 4 \Rightarrow x = 2$$

27. If $A = \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then prove that $A^2 - A + 2I = 0$.

Solution:

Given

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27. If $A = \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then prove that $A^2 - A + 2I = 0$.

Now we have to prove $A^2 - A + 2I = 0$

Now, we will find the matrix for A^2 , we get

$$\begin{aligned}A^2 &= A \times A = \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix} \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 3 \times 3 + (-2 \times 4) & 3 \times (-2) + (-2 \times -2) \\ 4 \times 3 + (-2 \times 4) & 4 \times (-2) + (-2 \times -2) \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 9 - 8 & -6 + 4 \\ 12 - 8 & -8 + 4 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 1 & -2 \\ 4 & -4 \end{bmatrix} \dots \dots \dots (i)\end{aligned}$$

Now, we will find the matrix for $2I$, we get

$$\begin{aligned}2I &= 2 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \\ \Rightarrow 2I &= \begin{bmatrix} 2 \times 1 & 2 \times 0 \\ 2 \times 0 & 2 \times 1 \end{bmatrix} \\ \Rightarrow 2I &= \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix} \dots \dots \dots (ii)\end{aligned}$$

$$A^2 - A + 2I$$

Substitute corresponding values from eqn (i) and eqn (ii), we get

$$\begin{aligned}\Rightarrow &= \begin{bmatrix} 1 & -2 \\ 4 & -4 \end{bmatrix} - \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix} + \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix} \\ \Rightarrow &= \begin{bmatrix} 1 - 3 + 2 & -2 - (-2) + 0 \\ 4 - 4 + 0 & -4 - (-2) + 2 \end{bmatrix} \\ \Rightarrow &= \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = 0\end{aligned}$$

Therefore,

$$A^2 - A + 2I = 0$$

Hence proved

28. If $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then prove that $A^2 = 5A + \lambda I$.

Solution:

Given

28. If $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then prove that $A^2 = 5A + \lambda I$.

Now, we have to find A^2 ,

$$\begin{aligned} A^2 &= A \times A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 3 \times 3 + (1 \times -1) & 3 \times 1 + 1 \times 2 \\ (-1 \times 3) + 2 \times (-1) & (-1 \times 1) + 2 \times 2 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 9 - 1 & 3 + 2 \\ -3 - 2 & -1 + 4 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} \dots \dots \dots (i) \end{aligned}$$

Now, we will find the matrix for $5A$, we get

$$\begin{aligned} 5A &= 5 \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} \\ \Rightarrow 5A &= \begin{bmatrix} 5 \times 3 & 5 \times 1 \\ 5 \times (-1) & 5 \times 2 \end{bmatrix} \\ \Rightarrow 5A &= \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} \dots \dots \dots (ii) \end{aligned}$$

So,

$$A^2 = 5A + \lambda I$$

Substitute corresponding values from eqn (i) and eqn (ii), we get

$$\Rightarrow \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} = \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} + \lambda \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} = \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} + \begin{bmatrix} \lambda & 0 \\ 0 & \lambda \end{bmatrix}$$

$$\begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} = \begin{bmatrix} 15 + \lambda & 5 + 0 \\ -5 + 0 & 10 + \lambda \end{bmatrix}$$

And to satisfy the above condition of equality, the corresponding entries of the matrices should be equal,

Hence,

$$8 = 15 + \lambda \Rightarrow \lambda = -7$$

$$3 = 10 + \lambda \Rightarrow \lambda = -7$$

29. If $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$ show that $A^2 - 5A + 7I_2 = 0$.

Solution:

Given

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29. If $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$ show that $A^2 - 5A + 7I_2 = 0$.

I_2 is an identity matrix of size 2, so

$$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

To show that

$$A^2 - 5A + 7I_2 = 0$$

Now, we will find the matrix for A^2 , we get

$$A^2 = A \times A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 3 \times 3 + (1 \times -1) & 3 \times 1 + 1 \times 2 \\ (-1 \times 3) + 2 \times (-1) & (-1 \times 1) + 2 \times 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 9 - 1 & 3 + 2 \\ -3 - 2 & -1 + 4 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} \dots \dots \dots (i)$$

Now, we will find the matrix for $5A$, we get

$$5A = 5 \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$

$$\Rightarrow 5A = \begin{bmatrix} 5 \times 3 & 5 \times 1 \\ 5 \times (-1) & 5 \times 2 \end{bmatrix}$$

$$\Rightarrow 5A = \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} \dots\dots\dots (ii)$$

Now,

$$7I_2 = 7 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 7 & 0 \\ 0 & 7 \end{bmatrix} \dots\dots\dots (iii)$$

So,

$$A^2 - 5A + 7I_2$$

Substitute corresponding values from eqn (i), (ii) and (iii), we get

$$\Rightarrow = \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} - \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} + \begin{bmatrix} 7 & 0 \\ 0 & 7 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 8 - 15 + 7 & 5 - 5 + 0 \\ -5 - (-5) + 0 & 3 - 10 + 7 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = 0$$

Hence the proof.

30. If $A = \begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix}$ show that $A^2 - 2A + 3I_2 = 0$.

Solution:

Given

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30. If $A = \begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix}$ show that $A^2 - 2A + 3I_2 = 0$.

I_2 is an identity matrix of size 2, so

$$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

Now we have to show,

$$A^2 - 2A + 3I_2 = 0$$

Now, we will find the matrix for A^2 , we get

$$\begin{aligned} A^2 &= A \times A = \begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 2 \times 2 + (3 \times -1) & 2 \times 3 + 3 \times 0 \\ (-1 \times 2) + 0 \times (-1) & (-1 \times 3) + 0 \times 0 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 4 - 3 & 6 + 0 \\ -2 + 0 & -3 + 0 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 1 & 6 \\ -2 & -3 \end{bmatrix} \dots \dots \dots (i) \end{aligned}$$

Now, we will find the matrix for $2A$, we get

$$\begin{aligned} 2A &= 2 \begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix} \\ \Rightarrow 2A &= \begin{bmatrix} 2 \times 2 & 2 \times 3 \\ 2 \times (-1) & 2 \times 0 \end{bmatrix} \\ \Rightarrow 2A &= \begin{bmatrix} 4 & 6 \\ -2 & 0 \end{bmatrix} \dots \dots \dots (ii) \end{aligned}$$

Now,

$$3I_2 = 3 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix} \dots \dots \dots (iii)$$

So,

$$A^2 - 2A + 3I_2$$

Substitute corresponding values from eqn (i), (ii) and (iii), we get

$$\Rightarrow = \begin{bmatrix} 1 & 6 \\ -2 & -3 \end{bmatrix} - \begin{bmatrix} 4 & 6 \\ -2 & 0 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 1 - 4 + 3 & 6 - 6 + 0 \\ -2 - (-2) + 0 & -3 - 0 + 3 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = 0$$

Hence the proof.

31. Show that the matrix $A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$ satisfies the equation $A^3 - 4A^2 + A = 0$.

Solution:

Given

31. Show that the matrix $A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$ satisfies the equation $A^3 - 4A^2 + A = 0$.

To show that $A^3 - 4A^2 + A = 0$

Now, we will find the matrix for A^2 , we get

$$A^2 = (A \times A) = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 2 \times 2 + (3 \times 1) & 2 \times 3 + 3 \times 2 \\ 1 \times 2 + 2 \times 1 & 1 \times 3 + 2 \times 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 4 + 3 & 6 + 6 \\ 2 + 2 & 3 + 4 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 7 & 12 \\ 4 & 7 \end{bmatrix} \dots \dots \dots (i)$$

Now, we will find the matrix for A^3 , we get

$$A^3 = A^2 \times A = \begin{bmatrix} 7 & 12 \\ 4 & 7 \end{bmatrix} \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$$

$$\Rightarrow A^3 = \begin{bmatrix} 7 \times 2 + 12 \times 1 & 7 \times 3 + 12 \times 2 \\ 4 \times 2 + 7 \times 1 & 4 \times 3 + 7 \times 2 \end{bmatrix}$$

$$\Rightarrow A^3 = \begin{bmatrix} 14 + 12 & 21 + 24 \\ 8 + 7 & 12 + 14 \end{bmatrix}$$

$$\Rightarrow A^3 = \begin{bmatrix} 26 & 45 \\ 15 & 26 \end{bmatrix} \dots \dots \dots (ii)$$

So,

$$A^3 - 4A^2 + A$$

Substitute corresponding values from eqn (i) and (ii), we get

$$\Rightarrow = \begin{bmatrix} 26 & 45 \\ 15 & 26 \end{bmatrix} - 4 \begin{bmatrix} 7 & 12 \\ 4 & 7 \end{bmatrix} + \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$$

I is an identity matrix so $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

To show that $A^2 - 12A - I = 0$

Now, we will find the matrix for A^2 , we get

$$A^2 = A \times A = \begin{bmatrix} 5 & 3 \\ 12 & 7 \end{bmatrix} \begin{bmatrix} 5 & 3 \\ 12 & 7 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 5 \times 5 + 3 \times 12 & 5 \times 3 + 3 \times 7 \\ 12 \times 5 + 7 \times 12 & 12 \times 3 + 7 \times 7 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 25 + 36 & 15 + 21 \\ 60 + 84 & 36 + 49 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 61 & 36 \\ 144 & 85 \end{bmatrix} \dots \dots \dots (i)$$

32. Show that the matrix $A = \begin{bmatrix} 5 & 3 \\ 12 & 7 \end{bmatrix}$ satisfies the equation $A^2 - 12A - I = 0$.

Solution:

Given

32. Show that the matrix $A = \begin{bmatrix} 5 & 3 \\ 12 & 7 \end{bmatrix}$ satisfies the equation $A^2 - 12A - I = 0$.

I is an identity matrix so $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

To show that $A^2 - 12A - I = 0$

Now, we will find the matrix for A^2 , we get

$$A^2 = A \times A = \begin{bmatrix} 5 & 3 \\ 12 & 7 \end{bmatrix} \begin{bmatrix} 5 & 3 \\ 12 & 7 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 5 \times 5 + 3 \times 12 & 5 \times 3 + 3 \times 7 \\ 12 \times 5 + 7 \times 12 & 12 \times 3 + 7 \times 7 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 25 + 36 & 15 + 21 \\ 60 + 84 & 36 + 49 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 61 & 36 \\ 144 & 85 \end{bmatrix} \dots \dots \dots (i)$$

Now, we will find the matrix for $12A$, we get

$$12A = 12 \begin{bmatrix} 5 & 3 \\ 12 & 7 \end{bmatrix}$$

$$\Rightarrow 12A = \begin{bmatrix} 12 \times 5 & 12 \times 3 \\ 12 \times 12 & 12 \times 7 \end{bmatrix}$$

$$\Rightarrow 12A = \begin{bmatrix} 60 & 36 \\ 144 & 84 \end{bmatrix} \dots \dots \dots (ii)$$

So,

$$A^2 - 12A - I$$

Substitute corresponding values from eqn (i) and (ii), we get

$$\Rightarrow = \begin{bmatrix} 61 & 36 \\ 144 & 85 \end{bmatrix} - \begin{bmatrix} 60 & 36 \\ 144 & 84 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 61 - 60 - 1 & 36 - 36 - 0 \\ 144 - 144 - 0 & 85 - 84 - 1 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = 0$$

Therefore,

$$A^2 - 12A - I = 0$$

Hence matrix A is the root of the given equation.

33. If $A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix}$ find $A^2 - 5A - 14I$.

Solution:

Given

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I is identity matrix so

$$33. \text{ If } A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix} \text{ find } A^2 - 5A - 14I. \quad 14I = 14 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 14 & 0 \\ 0 & 14 \end{bmatrix}$$

To find $A^2 - 5A - 14I$

Now, we will find the matrix for A^2 , we get

$$A^2 = A \times A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix} \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 3 \times 3 + (-5 \times -4) & 3 \times (-5) + (-5 \times 2) \\ (-4 \times 3) + (2 \times -4) & (-4 \times -5) + 2 \times 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 9 + 20 & -15 - 10 \\ -12 - 8 & 20 + 4 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 29 & -25 \\ -20 & 24 \end{bmatrix} \dots \dots \dots (i)$$

Now, we will find the matrix for $5A$, we get

$$5A = 5 \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix}$$

$$\Rightarrow 5A = \begin{bmatrix} 5 \times 3 & 5 \times (-5) \\ 5 \times (-4) & 5 \times 2 \end{bmatrix}$$

$$\Rightarrow 5A = \begin{bmatrix} 15 & -25 \\ -20 & 10 \end{bmatrix} \dots \dots \dots (ii)$$

So,

$$A^2 - 5A - 14I$$

Substitute corresponding values from eqn (i) and (ii), we get

$$\Rightarrow = \begin{bmatrix} 29 & -25 \\ -20 & 24 \end{bmatrix} - \begin{bmatrix} 15 & -25 \\ -20 & 10 \end{bmatrix} - \begin{bmatrix} 14 & 0 \\ 0 & 14 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 29 - 15 - 14 & -25 + 25 - 0 \\ -20 + 20 - 0 & 24 - 10 - 14 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = 0$$

34. If $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$ show that $A^2 - 5A + 7I = 0$. Use this to find A^4 .

Solution:

Given

34. If $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$ show that $A^2 - 5A + 7I = 0$. Use this to find A^4 .

I is identity matrix so

$$7I = 7 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 7 & 0 \\ 0 & 7 \end{bmatrix}$$

To show that $A^2 - 5A + 7I = 0$

Now, we will find the matrix for A^2 , we get

$$A^2 = A \times A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 3 \times 3 + (1 \times -1) & 3 \times 1 + 1 \times 2 \\ (-1 \times 3) + (2 \times -1) & (-1 \times 1) + 2 \times 2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 9 - 1 & 3 + 2 \\ -3 - 2 & -1 + 4 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} \dots \dots \dots (i)$$

Now, we will find the matrix for $5A$, we get

$$5A = 5 \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$

$$\Rightarrow 5A = \begin{bmatrix} 5 \times 3 & 5 \times 1 \\ 5 \times (-1) & 5 \times 2 \end{bmatrix}$$

$$\Rightarrow 5A = \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} \dots \dots \dots (ii)$$

So,

$$A^2 - 5A + 7I$$

Substitute corresponding values from eqn (i) and (ii), we get

$$\Rightarrow = \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} - \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} - \begin{bmatrix} 7 & 0 \\ 0 & 7 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 8-15-7 & 5-5-0 \\ -5+5-0 & 3-10-7 \end{bmatrix}$$

$$\Rightarrow = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = 0$$

Therefore

$$A^2 - 5A + 7I = 0$$

Hence proved

We will find A^4

$$A^2 - 5A + 7I = 0$$

Multiply both sides by A^2 , we get

$$A^2(A^2 - 5A + 7I) = A^2(0)$$

$$\Rightarrow A^4 - 5A^2.A + 7I.A^2$$

$$\Rightarrow A^4 = 5A^2.A - 7I.A^2$$

$$\Rightarrow A^4 = 5A^2A - 7A^2$$

As multiplying by the identity matrix, I don't change anything. Now will substitute the corresponding values we get

$$\Rightarrow A^4 = 5 \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix} \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} - 7 \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix}$$

$$\Rightarrow A^4 = 5 \begin{bmatrix} 24-5 & 8+10 \\ -15-3 & -5+6 \end{bmatrix} - 7 \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix}$$

$$\Rightarrow A^4 = 5 \begin{bmatrix} 19 & 18 \\ -18 & 1 \end{bmatrix} - 7 \begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix}$$

$$\Rightarrow A^4 = \begin{bmatrix} 5 \times 19 & 5 \times 18 \\ 5 \times (-18) & 5 \times 1 \end{bmatrix} - \begin{bmatrix} 7 \times 8 & 7 \times 5 \\ 7 \times (-5) & 7 \times 3 \end{bmatrix}$$

$$\Rightarrow A^4 = \begin{bmatrix} 95 & 90 \\ -90 & 5 \end{bmatrix} - \begin{bmatrix} 56 & 35 \\ -35 & 21 \end{bmatrix}$$

$$\Rightarrow A^4 = \begin{bmatrix} 95-56 & 90-35 \\ -90+35 & 5-21 \end{bmatrix}$$

$$\Rightarrow A^4 = \begin{bmatrix} 39 & 55 \\ -55 & -16 \end{bmatrix}$$

35. If $A = \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix}$ find k such that $A^2 = kA - 2I_2$.

Solution:

Given

35. If $A = \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix}$ find k such that $A^2 = kA - 2I_2$.

I_2 is an identity matrix of size 2, so

$$2I_2 = 2 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$$

Also given,

$$A^2 = kA - 2I_2$$

Now, we will find the matrix for A^2 , we get

$$A^2 = A \times A = \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix} \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 3 \times 3 + (-2 \times 4) & 3 \times (-2) + (-2 \times -2) \\ (4 \times 3) + (-2 \times 4) & (4 \times -2) + (-2 \times -2) \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 9 - 8 & -6 + 4 \\ 12 - 8 & -8 + 4 \end{bmatrix}$$

$$\Rightarrow A^2 = \begin{bmatrix} 1 & -2 \\ 4 & -4 \end{bmatrix} \dots \dots \dots (i)$$

Now, we will find the matrix for kA , we get

$$kA = k \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix}$$

$$\Rightarrow kA = \begin{bmatrix} k \times 3 & k \times (-2) \\ k \times 4 & k \times (-2) \end{bmatrix}$$

So,

$$A^2 = kA - 2I_2$$

Substitute corresponding values from eqn (i) and (ii), we get

$$\Rightarrow \begin{bmatrix} 1 & -2 \\ 4 & -4 \end{bmatrix} = \begin{bmatrix} 3k & -2k \\ 4k & -2k \end{bmatrix} - \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 1 & -2 \\ 4 & -4 \end{bmatrix} = \begin{bmatrix} 3k-2 & -2k-0 \\ 4k-0 & -2k-2 \end{bmatrix}$$

And to satisfy the above condition of equality, the corresponding entries of the matrices should be equal

$$\text{Hence, } 3k - 2 = 1 \Rightarrow k = 1$$

Therefore, the value of k is 1

36. If $A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$ find k such that $A^2 - 8A + kI = 0$.

Solution:

Given

36. If $A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$ find k such that $A^2 - 8A + kI = 0$.

I is identity matrix, so

$$kI = k \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix}$$

Also given,

$$A^2 - 8A + kI = 0$$

Now, we have to find A^2 , we get

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$$A^2 = A \times A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix} \Rightarrow A^2 = \begin{bmatrix} 1 \times 1 + 0 & 0 + 0 \\ (-1 \times 1) + 7 \times (-1) & 0 + 7 \times 7 \end{bmatrix} \\ \Rightarrow A^2 = \begin{bmatrix} 1 & 0 \\ -8 & 49 \end{bmatrix} \dots \dots \dots (i)$$

Now, we will find the matrix for $8A$, we get

$$8A = 8 \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix} \Rightarrow 8A = \begin{bmatrix} 8 \times 1 & 8 \times 0 \\ 8 \times (-1) & 8 \times 7 \end{bmatrix} \Rightarrow 8A = \begin{bmatrix} 8 & 0 \\ -8 & 56 \end{bmatrix} \dots \dots \dots (ii)$$

So,

$$A^2 - 8A + kI = 0$$

Substitute corresponding values from eqn (i) and (ii), we get

$$\Rightarrow \begin{bmatrix} 1 & 0 \\ -8 & 49 \end{bmatrix} - \begin{bmatrix} 8 & 0 \\ -8 & 56 \end{bmatrix} + \begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix} = 0 \\ \Rightarrow \begin{bmatrix} 1 - 8 + k & 0 - 0 + 0 \\ -8 + 8 + 0 & 49 - 56 + k \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

And to satisfy the above condition of equality, the corresponding entries of the matrices should be equal

Hence,

$$1 - 8 + k = 0 \Rightarrow k = 7$$

Therefore, the value of k is 7

37. If $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$ and $f(x) = x^2 - 2x - 3$ show that $f(A) = 0$

Solution:

Given

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37. If $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$ and $f(x) = x^2 - 2x - 3$ show that $f(A) = 0$

To show that $f(A) = 0$

Substitute $x = A$ in $f(x)$, we get

$$f(A) = A^2 - 2A - 3I \dots \dots \dots (i)$$

I is identity matrix, so

$$3I = 3 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$$

Now, we will find the matrix for A^2 , we get

$$\begin{aligned} A^2 &= A \times A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix} \Rightarrow A^2 = \begin{bmatrix} 1 \times 1 + 2 \times 2 & 1 \times 2 + 2 \times 1 \\ 2 \times 1 + 1 \times 2 & 2 \times 2 + 1 \times 1 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 1 + 4 & 2 + 2 \\ 2 + 2 & 4 + 1 \end{bmatrix} \Rightarrow A^2 = \begin{bmatrix} 5 & 4 \\ 4 & 5 \end{bmatrix} \dots \dots \dots (ii) \end{aligned}$$

Now, we will find the matrix for $2A$, we get

$$2A = 2 \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix} \Rightarrow 2A = \begin{bmatrix} 2 \times 1 & 2 \times 2 \\ 2 \times 2 & 2 \times 1 \end{bmatrix} \Rightarrow 2A = \begin{bmatrix} 2 & 4 \\ 4 & 2 \end{bmatrix} \dots \dots \dots (iii)$$

Substitute corresponding values from eqn (ii) and (iii) in eqn (i), we get

$$\begin{aligned} f(A) &= A^2 - 2A - 3I \Rightarrow f(A) = \begin{bmatrix} 5 & 4 \\ 4 & 5 \end{bmatrix} - \begin{bmatrix} 2 & 4 \\ 4 & 2 \end{bmatrix} - \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix} \\ \Rightarrow f(A) &= \begin{bmatrix} 5 - 2 - 3 & 4 - 4 - 0 \\ 4 - 4 - 0 & 5 - 2 - 3 \end{bmatrix} \Rightarrow f(A) = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \end{aligned}$$

So,

$$\Rightarrow f(A) = 0$$

Hence Proved

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38. If $A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ then find λ, μ so that $A^2 = \lambda A + \mu I$

Solution:

Given

38. If $A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ then find λ, μ so that $A^2 = \lambda A + \mu I$

So

$$\mu I = \mu \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} \mu & 0 \\ 0 & \mu \end{bmatrix}$$

Now, we will find the matrix for A^2 , we get

$$\begin{aligned} A^2 &= A \times A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix} \Rightarrow A^2 = \begin{bmatrix} 2 \times 2 + 3 \times 1 & 2 \times 3 + 3 \times 2 \\ 1 \times 2 + 2 \times 1 & 1 \times 3 + 2 \times 2 \end{bmatrix} \\ \Rightarrow A^2 &= \begin{bmatrix} 7 & 12 \\ 4 & 7 \end{bmatrix} \dots \dots \dots (i) \end{aligned}$$

Now, we will find the matrix for λA , we get

$$\lambda A = \lambda \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix} \Rightarrow \lambda A = \begin{bmatrix} \lambda \times 2 & \lambda \times 3 \\ \lambda \times 1 & \lambda \times 2 \end{bmatrix} \Rightarrow \lambda A = \begin{bmatrix} 2\lambda & 3\lambda \\ \lambda & 2\lambda \end{bmatrix} \dots \dots \dots (ii)$$

But given, $A^2 = \lambda A + \mu I$

Substitute corresponding values from equation (i) and (ii), we get

$$\Rightarrow \begin{bmatrix} 7 & 12 \\ 4 & 7 \end{bmatrix} = \begin{bmatrix} 2\lambda & 3\lambda \\ \lambda & 2\lambda \end{bmatrix} + \begin{bmatrix} \mu & 0 \\ 0 & \mu \end{bmatrix} \Rightarrow \begin{bmatrix} 7 & 12 \\ 4 & 7 \end{bmatrix} = \begin{bmatrix} 2\lambda + \mu & 3\lambda + 0 \\ \lambda + 0 & 2\lambda + \mu \end{bmatrix}$$

And to satisfy the above condition of equality, the corresponding entries of the matrices should be equal

Hence, $\lambda + 0 = 4 \Rightarrow \lambda = 4$

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And also, $2\lambda + \mu = 7$

Substituting the obtained value of λ in the above equation, we get

$$2(4) + \mu = 7 \Rightarrow 8 + \mu = 7 \Rightarrow \mu = -1$$

Therefore, the value of λ and μ are 4 and -1 respectively

39. Find the value of x for which the matrix product

$$\begin{bmatrix} 2 & 0 & 7 \\ 0 & 1 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} -x & 14x & 7x \\ 0 & 1 & 0 \\ x & -4x & -2x \end{bmatrix} \text{ equal to an identity matrix.}$$

Solution:

We know,

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

is identity matrix of size 3.

So according to the given criteria

$$\begin{bmatrix} 2 & 0 & 7 \\ 0 & 1 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} -x & 14x & 7x \\ 0 & 1 & 0 \\ x & -4x & -2x \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Now we will multiply the two matrices on LHS using the formula $c_{ij} = a_{i1}b_{1j} + a_{i2}b_{2j} + \dots + a_{in}b_{nj}$, we get

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$$\begin{bmatrix} 2 \times (-x) + 0 + 7 \times x & 2 \times 14x + 0 + 7 \times (-4x) & 2 \times 7x + 0 + 7 \times (-2x) \\ 0 + 0 + 0 & 0 + 1 \times 1 + 0 & 0 + 0 + 0 \\ 1 \times (-x) + 0 + 1 \times x & 1 \times 14x + (-2 \times 1) + (1 \times -4x) & 1 \times 7x + 0 + 1 \times (-2x) \end{bmatrix} \\
 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \\
 \Rightarrow \begin{bmatrix} 5x & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 10x - 2 & 5x \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

And to satisfy the above condition of equality, the corresponding entries of the matrices should be equal

So we get

$$5x = 1 \Rightarrow x = \frac{1}{5}$$

So the value of x is

$$\frac{1}{5}$$

Exercise 5.4 Page No: 5.54

1. Let $A = \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix}$ verify that

(i) $(2A)^T = 2A^T$

(ii) $(A + B)^T = A^T + B^T$

(iii) $(A - B)^T = A^T - B^T$

(iv) $(AB)^T = B^T A^T$

Solution:

(i) Given

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1. Let $A = \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix}$ verify that

Consider,

$$(2A)^T = 2A^T$$

Put the value of A

$$\begin{aligned} \Rightarrow \left(2 \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix} \right)^T &= 2 \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}^T \Rightarrow \begin{bmatrix} 4 & -6 \\ -14 & 10 \end{bmatrix}^T = 2 \begin{bmatrix} 2 & -7 \\ -3 & 5 \end{bmatrix} \\ \Rightarrow \begin{bmatrix} 4 & -14 \\ -6 & 10 \end{bmatrix} &= \begin{bmatrix} 4 & -14 \\ -6 & 10 \end{bmatrix} \end{aligned}$$

L.H.S = R.H.S

(ii) Given

1. Let $A = \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix}$ verify that

Consider,

$$(A + B)^T = A^T + B^T$$

$$\begin{aligned} \Rightarrow \left(\begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix} \right)^T &= \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}^T + \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix}^T \\ \Rightarrow \begin{bmatrix} 2+1 & -3+0 \\ -7+2 & 5-4 \end{bmatrix}^T &= \begin{bmatrix} 2 & -7 \\ -3 & 5 \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ 0 & -4 \end{bmatrix} \Rightarrow \begin{bmatrix} 3 & -3 \\ -5 & 1 \end{bmatrix}^T = \begin{bmatrix} 3 & -5 \\ -3 & 1 \end{bmatrix} \\ \Rightarrow \begin{bmatrix} 3 & -5 \\ -3 & 1 \end{bmatrix} &= \begin{bmatrix} 3 & -5 \\ -3 & 1 \end{bmatrix} \end{aligned}$$

L.H.S = R.H.S

Hence proved.

(iii) Given

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1. Let $A = \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix}$ verify that

Consider,

$$\begin{aligned} (A - B)^T &= A^T - B^T \Rightarrow \left(\begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix} \right)^T = \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}^T - \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix}^T \\ &\Rightarrow \begin{bmatrix} 2-1 & -3-0 \\ -7-2 & 5+4 \end{bmatrix}^T = \begin{bmatrix} 2 & -7 \\ -3 & 5 \end{bmatrix} - \begin{bmatrix} 1 & 2 \\ 0 & -4 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 & -3 \\ -9 & 9 \end{bmatrix}^T = \begin{bmatrix} 1 & -9 \\ -3 & 9 \end{bmatrix} \\ &\Rightarrow \begin{bmatrix} 1 & -9 \\ -3 & 9 \end{bmatrix} = \begin{bmatrix} 1 & -9 \\ -3 & 9 \end{bmatrix} \end{aligned}$$

L.H.S = R.H.S

(iv) Given

$$\begin{aligned} 1. \text{ Let } A &= \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix} \text{ verify that } (AB)^T = B^T A^T \\ &\Rightarrow \left(\begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix} \right)^T = \begin{bmatrix} 1 & 0 \\ 2 & -4 \end{bmatrix}^T \begin{bmatrix} 2 & -3 \\ -7 & 5 \end{bmatrix}^T \\ \begin{bmatrix} 2-6 & 0+12 \\ -7+10 & 0-20 \end{bmatrix}^T &= \begin{bmatrix} 1 & 2 \\ 0 & -4 \end{bmatrix} \begin{bmatrix} 2 & -7 \\ -3 & 5 \end{bmatrix} \begin{bmatrix} -4 & 12 \\ 3 & -20 \end{bmatrix}^T = \begin{bmatrix} 2-6 & -7+10 \\ 0+12 & 0-20 \end{bmatrix} \\ \begin{bmatrix} -4 & 3 \\ 12 & -20 \end{bmatrix} &= \begin{bmatrix} -4 & 3 \\ 12 & -20 \end{bmatrix} \end{aligned}$$

So,

$$(AB)^T = B^T A^T \quad 2. A = \begin{bmatrix} 3 \\ 5 \\ 2 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 0 & 4 \end{bmatrix} \text{ verify that } (AB)^T = B^T A^T$$

Solution:

Given

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2. $A = \begin{bmatrix} 3 \\ 5 \\ 2 \end{bmatrix}$ and $B = [1 \ 0 \ 4]$ verify that $(AB)^T = B^T A^T$ $(AB)^T = B^T A^T$

$$\Rightarrow \left(\begin{bmatrix} 3 \\ 5 \\ 2 \end{bmatrix} [1 \ 0 \ 4] \right)^T = [1 \ 0 \ 4]^T \begin{bmatrix} 3 \\ 5 \\ 2 \end{bmatrix}^T \Rightarrow \begin{bmatrix} 3 & 0 & 12 \\ 5 & 0 & 20 \\ 2 & 0 & 8 \end{bmatrix}^T = \begin{bmatrix} 1 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 3 & 5 & 2 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 3 & 5 & 2 \\ 0 & 0 & 0 \\ 12 & 20 & 8 \end{bmatrix} = \begin{bmatrix} 3 & 5 & 2 \\ 0 & 0 & 0 \\ 12 & 20 & 8 \end{bmatrix}$$

L.H.S = R.H.S

So,

$$(AB)^T = B^T A^T$$

3. Let $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix}$ find A^T, B^T and verify that

(i) $(A + B)^T = A^T + B^T$

(ii) $(AB)^T = B^T A^T$

(iii) $(2A)^T = 2 A^T$

Solution:

(i) Given

3. Let $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix}$ find A^T, B^T and verify that

Consider,

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$$(A + B)^T = A^T + B^T$$

$$\left(\begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix} \right)^T = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix}^T + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix}^T$$

$$\left(\begin{bmatrix} 1+1 & -1+2 & 0+3 \\ 2+2 & 1+1 & 3+3 \\ 1+0 & 2+1 & 1+1 \end{bmatrix} \right)^T = \begin{bmatrix} 1 & 2 & 1 \\ -1 & 1 & 2 \\ 0 & 3 & 1 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 0 \\ 2 & 1 & 1 \\ 3 & 3 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 1 & 3 \\ 4 & 2 & 6 \\ 1 & 3 & 2 \end{bmatrix}^T = \begin{bmatrix} 1+1 & 2+2 & 1+0 \\ -1+2 & 1+1 & 2+1 \\ 0+3 & 3+3 & 1+1 \end{bmatrix} \begin{bmatrix} 2 & 4 & 1 \\ 1 & 2 & 3 \\ 3 & 6 & 2 \end{bmatrix} = \begin{bmatrix} 2 & 4 & 1 \\ 1 & 2 & 3 \\ 3 & 6 & 2 \end{bmatrix}$$

L.H.S = R.H.S

So,

$$(A + B)^T = A^T + B^T$$

(ii) Given

3. Let $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix}$ find A^T, B^T and verify that

Consider,

$$(AB)^T = B^T A^T \left(\begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix} \right)^T = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix}^T \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix}^T$$

$$\begin{bmatrix} 1-2+0 & 2-1+0 & 3-3+0 \\ 2+2+0 & 4+1+3 & 6+3+3 \\ 1+4+0 & 2+2+1 & 3+6+1 \end{bmatrix}^T = \begin{bmatrix} 1 & 2 & 0 \\ 2 & 1 & 1 \\ 3 & 3 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 1 \\ -1 & 1 & 2 \\ 0 & 3 & 1 \end{bmatrix}$$

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$$\begin{bmatrix} -1 & 1 & 0 \\ 4 & 8 & 12 \\ 5 & 5 & 10 \end{bmatrix}^T = \begin{bmatrix} 1-2+0 & 2+2+0 & 1+4+0 \\ 2-1+0 & 4+1+3 & 2+2+1 \\ 3-3+0 & 6+3+3 & 3+6+1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 4 & 5 \\ 1 & 8 & 5 \\ 0 & 12 & 10 \end{bmatrix} = \begin{bmatrix} -1 & 4 & 5 \\ 1 & 8 & 5 \\ 0 & 12 & 10 \end{bmatrix}$$

L.H.S = R.H.S

So,

$$(AB)^T = B^T A^T$$

(iii) Given

$$3. \text{ Let } A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix} \text{ find } A^T, B^T \text{ and verify that}$$

Consider,

$$(2A)^T = 2A^T \Rightarrow \left(2 \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix} \right)^T = 2 \begin{bmatrix} 1 & -1 & 0 \\ 2 & 1 & 3 \\ 1 & 2 & 1 \end{bmatrix}^T$$

$$\Rightarrow \begin{bmatrix} 2 & -2 & 0 \\ 4 & 2 & 6 \\ 2 & 4 & 2 \end{bmatrix}^T = 2 \begin{bmatrix} 1 & 2 & 1 \\ -1 & 1 & 2 \\ 0 & 3 & 1 \end{bmatrix} \Rightarrow \begin{bmatrix} 2 & 4 & 2 \\ -2 & 2 & 4 \\ 0 & 6 & 2 \end{bmatrix} = \begin{bmatrix} 2 & 4 & 2 \\ -2 & 2 & 4 \\ 0 & 6 & 2 \end{bmatrix}$$

L.H.S = R.H.S

So,

$$(2A)^T = 2A^T$$

$$4. \text{ If } A = \begin{bmatrix} -2 \\ 4 \\ 5 \end{bmatrix}, B = [1 \ 3 \ -6], \text{ verify that } (AB)^T = B^T A^T$$

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Solution:

Given

4. If $A = \begin{bmatrix} -2 \\ 4 \\ 5 \end{bmatrix}$, $B = [1 \ 3 \ -6]$, verify that $(AB)^T = B^T A^T$

Consider,

$$\begin{aligned}(AB)^T &= B^T A^T \Rightarrow \left(\begin{bmatrix} -2 \\ 4 \\ 5 \end{bmatrix} [1 \ 3 \ -6] \right)^T = [1 \ 3 \ -6]^T \begin{bmatrix} -2 \\ 4 \\ 5 \end{bmatrix}^T \\&\Rightarrow \begin{bmatrix} -2 & -6 & -12 \\ 4 & 12 & -24 \\ 5 & 15 & -30 \end{bmatrix}^T = \begin{bmatrix} 1 \\ 3 \\ -6 \end{bmatrix}^T [-2 \ 4 \ 5] \\&\Rightarrow \begin{bmatrix} -2 & 4 & 5 \\ -6 & 12 & 15 \\ -12 & -24 & -30 \end{bmatrix} = \begin{bmatrix} -2 & 4 & 5 \\ -6 & 12 & 15 \\ -12 & -24 & -30 \end{bmatrix}\end{aligned}$$

L.H.S = R.H.S

So,

5. If $A = \begin{bmatrix} 2 & 4 & -1 \\ -1 & 0 & 2 \end{bmatrix}$, $\begin{bmatrix} 3 & 4 \\ -1 & 2 \\ 2 & 1 \end{bmatrix}$, find $(AB)^T$

Solution:

Given

5. If $A = \begin{bmatrix} 2 & 4 & -1 \\ -1 & 0 & 2 \end{bmatrix}$, $\begin{bmatrix} 3 & 4 \\ -1 & 2 \\ 2 & 1 \end{bmatrix}$, find $(AB)^T$

Now we have to find $(AB)^T$

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$$\Rightarrow \left(\begin{bmatrix} 2 & 4 & -1 \\ -1 & 0 & 2 \end{bmatrix} \begin{bmatrix} 3 & 4 \\ -1 & 2 \\ 2 & 1 \end{bmatrix} \right)^T \Rightarrow \begin{bmatrix} 6-4-2 & 8+8-1 \\ -3-0+4 & -4+0+2 \end{bmatrix}^T \Rightarrow \begin{bmatrix} 0 & 15 \\ 1 & -2 \end{bmatrix}^T \\ \Rightarrow \begin{bmatrix} 0 & 1 \\ 15 & -2 \end{bmatrix}$$

So,

$$(AB)^T = \begin{bmatrix} 0 & 1 \\ 15 & -2 \end{bmatrix}$$

Exercise 5.5 Page No: 5.60

1. If $A = \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}$, prove that $A - A^T$ is a skew-symmetric matrix.

Solution:

Given

1. If $A = \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}$, that $A - A^T$ is a skew-symmetric matrix.

Consider,

$$(A - A^T) = \left(\begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix} - \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}^T \right) = \left(\begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix} - \begin{bmatrix} 2 & 4 \\ 3 & 5 \end{bmatrix} \right) = \begin{bmatrix} 2-2 & 3-4 \\ 4-3 & 5-5 \end{bmatrix}$$

$$(A - A^T) = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$$

... (i)

$$-(A - A^T)^T = -\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}^T = -\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} = (A - A^T)$$

... (ii)

From (i) and (ii) we can see that

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A skew-symmetric matrix is a square matrix whose transpose equal to its negative, that is,

$$X = -X^T$$

So, $A - A^T$ is a skew-symmetric.

2. If $A = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$, show that $A - A^T$ is a skew - symmetric matrix.

Solution:

Given

2. If $A = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$, show that $A - A^T$ is a skew - symmetric matrix.

Consider,

$$(A - A^T) = \begin{bmatrix} 0 & -5 \\ 5 & 0 \end{bmatrix}$$

... (i)

$$-(A - A^T)^T = -\begin{bmatrix} 0 & -5 \\ 5 & 0 \end{bmatrix}^T = -\begin{bmatrix} 0 & 5 \\ -5 & 0 \end{bmatrix} = -(A - A^T) = \begin{bmatrix} 0 & -5 \\ 5 & 0 \end{bmatrix}$$

... (ii)

From (i) and (ii) we can see that

A skew-symmetric matrix is a square matrix whose transpose equals its negative, that is,

$$X = -X^T$$

So, $A - A^T$ is a skew-symmetric matrix.

3. If the matrix $A = \begin{bmatrix} 5 & 2 & x \\ y & z & -3 \\ 4 & t & -7 \end{bmatrix}$, is a symmetric matrix matrix find x, y, z and t

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Solution:

Given,

$$A = \begin{bmatrix} 5 & 2 & x \\ y & z & -3 \\ 4 & t & -7 \end{bmatrix}$$

is a symmetric matrix.

We know that $A = [a_{ij}]_{m \times n}$ is a symmetric matrix if $a_{ij} = a_{ji}$

So,

$$x = a_{13} = a_{31} = 4 \quad y = a_{21} = a_{12} = 2 \quad z = a_{22} = a_{22} = z \quad t = a_{32} = a_{23} = -3$$

Hence, $x = 4$, $y = 2$, $t = -3$ and z can have any value.

4. Let. Find matrices X and Y such that $X + Y = A$, where X is a symmetric and y is a skew-symmetric matrix.

Solution:

Given,

$$A = \begin{bmatrix} 3 & 2 & 7 \\ 1 & 4 & 3 \\ -2 & 5 & 8 \end{bmatrix}$$

Then

$$A^T = \begin{bmatrix} 3 & 1 & -2 \\ 2 & 4 & 5 \\ 7 & 3 & 8 \end{bmatrix} \quad X = \frac{1}{2}(A + A^T) = \frac{1}{2} \left(\begin{bmatrix} 3 & 2 & 7 \\ 1 & 4 & 3 \\ -2 & 5 & 8 \end{bmatrix} + \begin{bmatrix} 3 & 1 & -2 \\ 2 & 4 & 5 \\ 7 & 3 & 8 \end{bmatrix} \right)$$

$$= \frac{1}{2} \begin{bmatrix} 3+3 & 2+1 & 7-2 \\ 1+2 & 4+4 & 3+5 \\ -2+7 & 5+3 & 8+8 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 6 & 3 & 5 \\ 3 & 8 & 8 \\ 5 & 8 & 16 \end{bmatrix} \quad X = \begin{bmatrix} 3 & \frac{3}{2} & \frac{5}{2} \\ \frac{3}{2} & 4 & 4 \\ \frac{5}{2} & 4 & 8 \end{bmatrix}$$

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Now,

$$Y = \frac{1}{2}(A - A^T) = \frac{1}{2} \left(\begin{bmatrix} 3 & 2 & 7 \\ 1 & 4 & 3 \\ -2 & 5 & 8 \end{bmatrix} - \begin{bmatrix} 3 & 1 & -2 \\ 2 & 4 & 5 \\ 7 & 3 & 8 \end{bmatrix} \right) = \frac{1}{2} \begin{bmatrix} 3-3 & 2-1 & 7+2 \\ 1-2 & 4-4 & 3-5 \\ -2-7 & 5-3 & 8-8 \end{bmatrix}$$

$$= \frac{1}{2} \begin{bmatrix} 0 & 1 & 9 \\ -1 & 0 & -2 \\ -9 & 2 & 0 \end{bmatrix} \quad Y = \begin{bmatrix} 0 & \frac{1}{2} & \frac{9}{2} \\ -\frac{1}{2} & 0 & -1 \\ -\frac{9}{2} & 1 & 0 \end{bmatrix}$$

Now,

$$X^T = \begin{bmatrix} 3 & \frac{3}{2} & \frac{5}{2} \\ \frac{3}{2} & 4 & 4 \\ \frac{5}{2} & 4 & 8 \end{bmatrix}^T = \begin{bmatrix} 3 & \frac{3}{2} & \frac{5}{2} \\ \frac{3}{2} & 4 & 4 \\ \frac{5}{2} & 4 & 8 \end{bmatrix} = X$$

X is a symmetric matrix.

Now,

$$-Y^T = - \begin{bmatrix} 0 & \frac{1}{2} & \frac{9}{2} \\ -\frac{1}{2} & 0 & -1 \\ -\frac{9}{2} & 1 & 0 \end{bmatrix}^T = - \begin{bmatrix} 0 & -\frac{1}{2} & -\frac{9}{2} \\ \frac{1}{2} & 0 & 1 \\ \frac{9}{2} & -1 & 0 \end{bmatrix} \quad -Y^T = \begin{bmatrix} 0 & \frac{1}{2} & \frac{9}{2} \\ -\frac{1}{2} & 0 & -1 \\ -\frac{9}{2} & 1 & 0 \end{bmatrix}$$

$$-Y^T = Y$$

Y is a skew symmetric matrix.

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$$\begin{aligned} X + Y &= \begin{bmatrix} 3 & \frac{3}{2} & \frac{5}{2} \\ \frac{3}{2} & 4 & 4 \\ \frac{5}{2} & 4 & 8 \end{bmatrix} + \begin{bmatrix} 0 & \frac{1}{2} & \frac{9}{2} \\ -\frac{1}{2} & 0 & -1 \\ -\frac{9}{2} & 1 & 0 \end{bmatrix} = \begin{bmatrix} 3+0 & \frac{3}{2}+\frac{1}{2} & \frac{5}{2}+\frac{9}{2} \\ \frac{3}{2}-\frac{1}{2} & 4+0 & 4-1 \\ \frac{5}{2}-\frac{9}{2} & 4+1 & 8+0 \end{bmatrix} \\ &= \begin{bmatrix} 3 & 2 & 7 \\ 1 & 4 & 3 \\ -2 & 5 & 8 \end{bmatrix} = A \end{aligned}$$

Hence, $X + Y = A$



Chapterwise RD Sharma Solutions for Class 12 Maths :

- Chapter 1–Relation
- Chapter 2–Functions
- Chapter 3–Binary Operations
- Chapter 4–Inverse Trigonometric Functions
- Chapter 5–Algebra of Matrices
- Chapter 6–Determinants
- Chapter 7–Adjoint and Inverse of a Matrix
- Chapter 8–Solution of Simultaneous Linear Equations
- Chapter 9–Continuity
- Chapter 10–Differentiability
- Chapter 11–Differentiation
- Chapter 12–Higher Order Derivatives
- Chapter 13–Derivatives as a Rate Measurer
- Chapter 14–Differentials, Errors and Approximations
- Chapter 15–Mean Value Theorems
- Chapter 16–Tangents and Normals
- Chapter 17–Increasing and Decreasing Functions
- Chapter 18–Maxima and Minima
- Chapter 19–Indefinite Integrals

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About RD Sharma

RD Sharma isn't the kind of author you'd bump into at lit fests. But his bestselling books have helped many CBSE students lose their dread of maths. Sunday Times profiles the tutor turned internet star

He dreams of algorithms that would give most people nightmares. And, spends every waking hour thinking of ways to explain concepts like 'series solution of linear differential equations'. Meet Dr Ravi Dutt Sharma — mathematics teacher and author of 25 reference books — whose name evokes as much awe as the subject he teaches. And though students have used his thick tomes for the last 31 years to ace the dreaded maths exam, it's only recently that a spoof video turned the tutor into a YouTube star.

R D Sharma had a good laugh but said he shared little with his on-screen persona except for the love for maths. "I like to spend all my time thinking and writing about maths problems. I find it relaxing," he says. When he is not writing books explaining mathematical concepts for classes 6 to 12 and engineering students, Sharma is busy dispensing his duty as vice-principal and head of department of science and humanities at Delhi government's Guru Nanak Dev Institute of Technology.

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