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NCERT Solutions for 9th Class Maths : Chapter 9 Areas of Parallelograms and Triangles



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NCERT Solutions for 9th Class Maths : Chapter 9 Areas of Parallelograms and Triangles

Class 9: Maths Chapter 9 solutions. Complete Class 9 Maths Chapter 9 Notes.

NCERT Solutions for 9th Class Maths : Chapter 9 Areas of Parallelograms and Triangles

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Exercise 9.1

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1. Which of the following figures lie on the same base and between the same parallels. In such a case, write the common base and the two parallels.

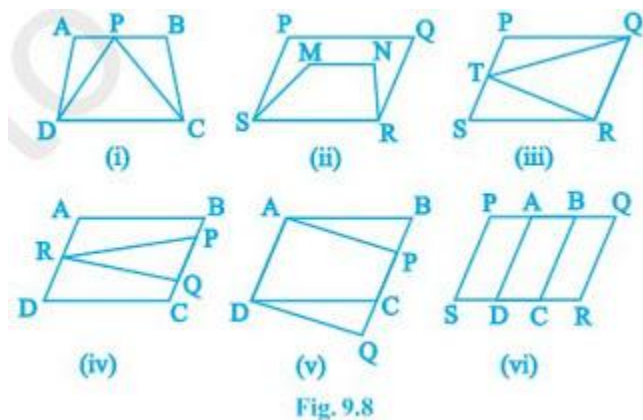


Fig. 9.8

Answer

(i) Trapezium ABCD and $\triangle PDC$ lie on the same DC and between the same parallel lines AB and DC.

(ii) Parallelogram PQRS and trapezium SMNR lie on the same base SR but not between the same parallel lines.

(iii) Parallelogram PQRS and $\triangle RTQ$ lie on the same base QR and between the same parallel lines QR and PS.

(iv) Parallelogram ABCD and $\triangle PQR$ do not lie on the same base but between the same parallel lines BC and AD.

(v) Quadrilateral ABQD and trapezium APCD lie on the same base AD and between the same parallel lines AD and BQ.

(vi) Parallelogram PQRS and parallelogram ABCD do not lie on the same base SR but between the same parallel lines SR and PQ.

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Exercise 9.2

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1. In Fig. 9.15, ABCD is a parallelogram, $AE \perp DC$ and $CF \perp AD$. If $AB = 16$ cm, $AE = 8$ cm and $CF = 10$ cm, find AD .

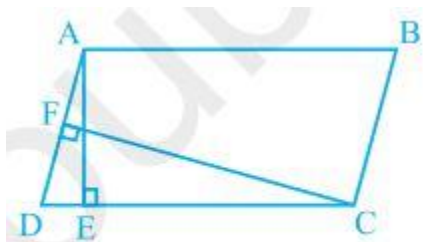


Fig. 9.15

Answer

Given,

$AB = CD = 16$ cm (Opposite sides of a parallelogram)

$CF = 10$ cm and $AE = 8$ cm

Now,

Area of parallelogram = Base $\times$ Altitude

$$= CD \times AE = AD \times CF$$

$$\Rightarrow 16 \times 8 = AD \times 10$$

$$\Rightarrow AD = 128/10 \text{ cm}$$

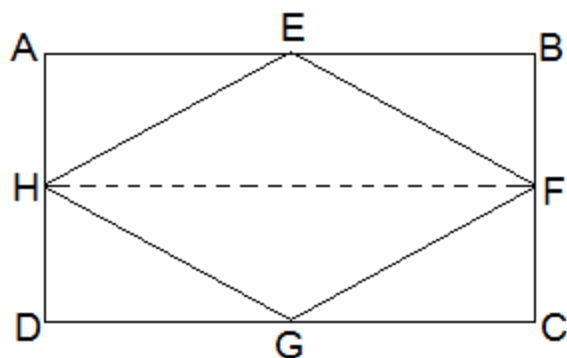
$$\Rightarrow AD = 12.8 \text{ cm}$$

2. If E,F,G and H are respectively the mid-points of the sides of a parallelogram ABCD, show that

$$\text{ar}(EFGH) = \frac{1}{2} \text{ar}(ABCD).$$

Answer

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Given,

E, F, G and H are respectively the mid-points of the sides of a parallelogram ABCD.

To Prove,

$$\text{ar}(\text{EFGH}) = \frac{1}{2} \text{ar}(\text{ABCD})$$

Construction,

H and F are joined.

Proof,

$AD \parallel BC$ and $AD = BC$ (Opposite sides of a parallelogram)

$$\Rightarrow \frac{1}{2} AD = \frac{1}{2} BC$$

Also,

$AH \parallel BF$ and $DH \parallel CF$

$$\Rightarrow AH = BF \text{ and } DH = CF \text{ (H and F are mid points)}$$

Thus, ABFH and HFCD are parallelograms.

Now,

$\triangle EFH$ and $\parallel\text{gm ABFH}$ lie on the same base FH and between the same parallel lines AB and HF.

$$\therefore \text{area of EFH} = \frac{1}{2} \text{area of ABFH} \text{ --- (i)}$$

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also, area of GHF = $\frac{1}{2}$ area of HFCD --- (ii)

Adding (i) and (ii),

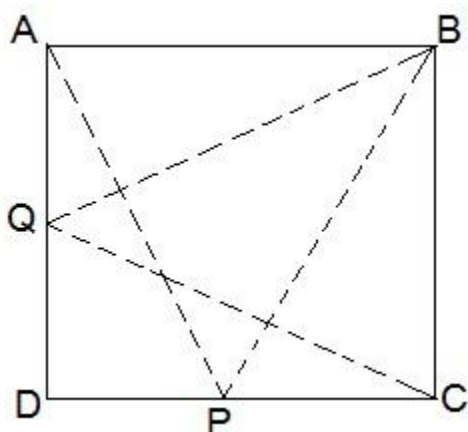
area of $\triangle EFH$ + area of $\triangle GHF$ = $\frac{1}{2}$ area of ABFH + $\frac{1}{2}$ area of HFCD

$\Rightarrow$ area of EFGH = area of ABFH

$\Rightarrow \text{ar}(\text{EFGH}) = \frac{1}{2} \text{ar}(\text{ABCD})$

3. P and Q are any two points lying on the sides DC and AD respectively of a parallelogram ABCD. Show that $\text{ar}(\triangle APB) = \text{ar}(\triangle BQC)$.

Answer



$\triangle APB$ and $\parallel\text{gm ABCD}$ are on the same base AB and between same parallel AB and DC.

Therefore,

$\text{ar}(\triangle APB) = \frac{1}{2} \text{ar}(\parallel\text{gm ABCD})$ --- (i)

Similarly,

$\text{ar}(\triangle BQC) = \frac{1}{2} \text{ar}(\parallel\text{gm ABCD})$ --- (ii)

From (i) and (ii),

we have $\text{ar}(\triangle APB) = \text{ar}(\triangle BQC)$

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4. In Fig. 9.16, P is a point in the interior of a parallelogram ABCD. Show that

(i) $\text{ar}(\text{APB}) + \text{ar}(\text{PCD}) = \frac{1}{2} \text{ar}(\text{ABCD})$

(ii) $\text{ar}(\text{APD}) + \text{ar}(\text{PBC}) = \text{ar}(\text{APB}) + \text{ar}(\text{PCD})$

[Hint : Through P, draw a line parallel to AB.]

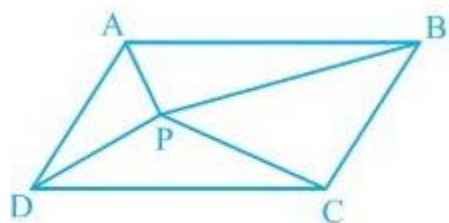
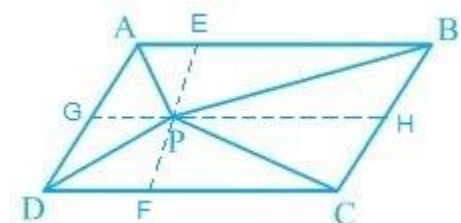


Fig. 9.16

Answer



(i) A line GH is drawn parallel to AB passing through P.

In a parallelogram,

$AB \parallel GH$ (by construction) --- (i)

Thus,

$AD \parallel BC \Rightarrow AG \parallel BH$ --- (ii)

From equations (i) and (ii),

ABHG is a parallelogram.

Now,

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In $\triangle APB$ and parallelogram $ABHG$ are lying on the same base AB and between the same parallel lines AB and GH .

$$\therefore \text{ar}(\triangle APB) = \frac{1}{2} \text{ar}(ABHG) \text{ --- (iii)}$$

also,

In $\triangle PCD$ and parallelogram $CDGH$ are lying on the same base CD and between the same parallel lines CD and GH .

$$\therefore \text{ar}(\triangle PCD) = \frac{1}{2} \text{ar}(CDGH) \text{ --- (iv)}$$

Adding equations (iii) and (iv),

$$\text{ar}(\triangle APB) + \text{ar}(\triangle PCD) = \frac{1}{2} \{\text{ar}(ABHG) + \text{ar}(CDGH)\}$$

$$\Rightarrow \text{ar}(APB) + \text{ar}(PCD) = \frac{1}{2} \text{ar}(ABCD)$$

(ii) A line EF is drawn parallel to AD passing through P .

In a parallelogram,

$$AD \parallel EF \text{ (by construction) --- (i)}$$

Thus,

$$AB \parallel CD \Rightarrow AE \parallel DF \text{ --- (ii)}$$

From equations (i) and (ii),

$AEDF$ is a parallelogram.

Now,

In $\triangle APD$ and parallelogram $AEFD$ are lying on the same base AD and between the same parallel lines AD and EF .

$$\therefore \text{ar}(\triangle APD) = \frac{1}{2} \text{ar}(AEFD) \text{ --- (iii)}$$

also,

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In $\triangle PBC$ and parallelogram $BCFE$ are lying on the same base BC and between the same parallel lines BC and EF .

$$\therefore \text{ar}(\triangle PBC) = \frac{1}{2} \text{ar}(BCFE) \text{ --- (iv)}$$

Adding equations (iii) and (iv),

$$\text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \frac{1}{2} \{\text{ar}(AEFD) + \text{ar}(BCFE)\}$$

$$\Rightarrow \text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \text{ar}(\triangle APB) + \text{ar}(\triangle PCD)$$

5. In Fig. 9.17, PQRS and ABRS are parallelograms and X is any point on side BR. Show that

$$(i) \text{ar}(\text{PQRS}) = \text{ar}(\text{ABRS})$$

$$(ii) \text{ar}(\triangle AXS) = \frac{1}{2} \text{ar}(\text{PQRS})$$

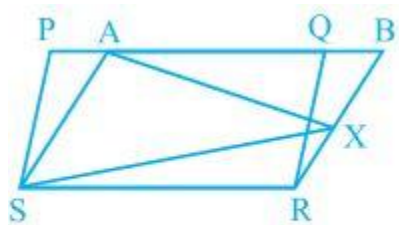


Fig. 9.17

Answer

(i) Parallelogram PQRS and ABRS lie on the same base SR and between the same parallel lines SR and PB.

$$\therefore \text{ar}(\text{PQRS}) = \text{ar}(\text{ABRS}) \text{ --- (i)}$$

(ii) In $\triangle AXS$ and parallelogram ABRS are lying on the same base AS and between the same parallel lines AS and BR.

$$\therefore \text{ar}(\triangle AXS) = \frac{1}{2} \text{ar}(\text{ABRS}) \text{ --- (ii)}$$

From (i) and (ii),

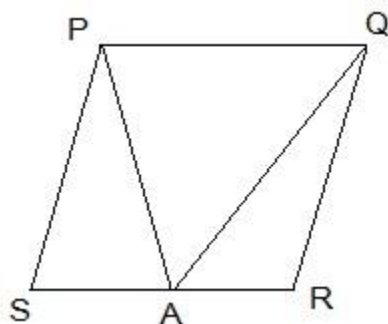
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$$\text{ar}(\triangle AXS) = 1/2 \text{ ar}(PQRS)$$

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6. A farmer was having a field in the form of a parallelogram PQRS. She took any point A on RS and joined it to points P and Q. In how many parts the fields is divided? What are the shapes of these parts? The farmer wants to sow wheat and pulses in equal portions of the field separately. How should she do it?

Answer



The field is divided into three parts. The three parts are in the shape of triangle. $\triangle PSA$, $\triangle PAQ$ and $\triangle QAR$.

$$\text{Area of } \triangle PSA + \triangle PAQ + \triangle QAR = \text{Area of PQRS} \text{ --- (i)}$$

$$\text{Area of } \triangle PAQ = 1/2 \text{ area of PQRS} \text{ --- (ii)}$$

Triangle and parallelogram on the same base and between the same parallel lines.

From (i) and (ii),

$$\text{Area of } \triangle PSA + \text{Area of } \triangle QAR = 1/2 \text{ area of PQRS} \text{ --- (iii)}$$

Clearly from (ii) and (iii),

Farmer must sow wheat or pulses in $\triangle PAQ$ or either in both $\triangle PSA$ and $\triangle QAR$.

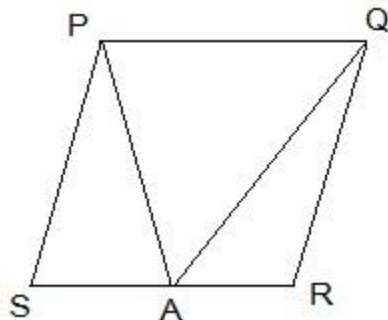
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Exercise 9.3

1. In Fig.9.23, E is any point on median AD of a ΔABC . Show that $\text{ar}(\text{ABE}) = \text{ar}(\text{ACE})$.

**Answer**

Given,

AD is median of ΔABC . Thus, it will divide ΔABC into two triangles of equal area.

$$\therefore \text{ar}(\text{ABD}) = \text{ar}(\text{ACD}) \text{ --- (i)}$$

also,

ED is the median of ΔABC .

$$\therefore \text{ar}(\text{EBD}) = \text{ar}(\text{ECD}) \text{ --- (ii)}$$

Subtracting (ii) from (i),

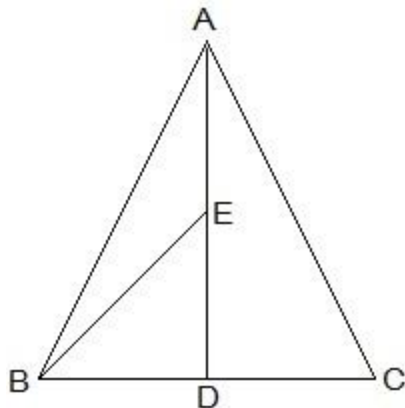
$$\text{ar}(\text{ABD}) - \text{ar}(\text{EBD}) = \text{ar}(\text{ACD}) - \text{ar}(\text{ECD})$$

$$\Rightarrow \text{ar}(\text{ABE}) = \text{ar}(\text{ACE})$$

2. In a triangle ABC, E is the mid-point of median AD. Show that $\text{ar}(\text{BED}) = \frac{1}{4} \text{ar}(\text{ABC})$.

Answer

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$$\text{ar}(\text{BED}) = \left(\frac{1}{2}\right) \times \text{BD} \times \text{DE}$$

As E is the mid-point of AD,

Thus, $\text{AE} = \text{DE}$

As AD is the median on side BC of triangle ABC,

Thus, $\text{BD} = \text{DC}$

Therefore,

$$\text{DE} = \left(\frac{1}{2}\right)\text{AD} \text{ --- (i)}$$

$$\text{BD} = \left(\frac{1}{2}\right)\text{BC} \text{ --- (ii)}$$

From (i) and (ii),

$$\text{ar}(\text{BED}) = \left(\frac{1}{2}\right) \times \left(\frac{1}{2}\right) \text{BC} \times \left(\frac{1}{2}\right)\text{AD}$$

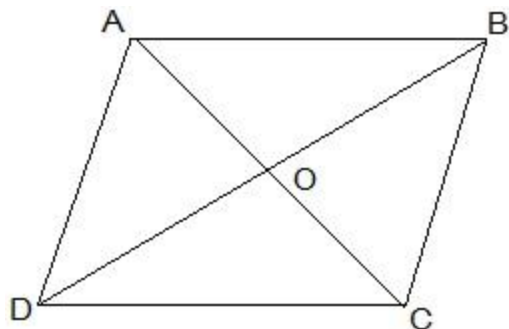
$$\Rightarrow \text{ar}(\text{BED}) = \left(\frac{1}{2}\right) \times \left(\frac{1}{2}\right) \text{ar}(\text{ABC})$$

$$\Rightarrow \text{ar}(\text{BED}) = \frac{1}{4} \text{ar}(\text{ABC})$$

3. Show that the diagonals of a parallelogram divide it into four triangles of equal area.

Answer

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O is the mid point of AC and BD. (diagonals of bisect each other)

In $\triangle ABC$, BO is the median.

$$\therefore \text{ar}(\triangle AOB) = \text{ar}(\triangle BOC) \text{ --- (i)}$$

also,

In $\triangle BCD$, CO is the median.

$$\therefore \text{ar}(\triangle BOC) = \text{ar}(\triangle COD) \text{ --- (ii)}$$

In $\triangle ACD$, OD is the median.

$$\therefore \text{ar}(\triangle AOD) = \text{ar}(\triangle COD) \text{ --- (iii)}$$

In $\triangle ABD$, AO is the median.

$$\therefore \text{ar}(\triangle AOD) = \text{ar}(\triangle AOB) \text{ --- (iv)}$$

From equations (i), (ii), (iii) and (iv),

$$\text{ar}(\triangle BOC) = \text{ar}(\triangle COD) = \text{ar}(\triangle AOD) = \text{ar}(\triangle AOB)$$

So, the diagonals of a parallelogram divide it into four triangles of equal area.

4. In Fig. 9.24, ABC and ABD are two triangles on the same base AB. If line-segment CD is bisected by AB at O, show that:

$$\text{ar}(\triangle ABC) = \text{ar}(\triangle ABD).$$

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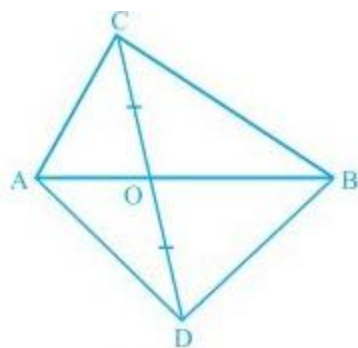


Fig. 9.24

Answer

In $\triangle ABC$,

AO is the median. (CD is bisected by AB at O)

$$\therefore \text{ar}(\triangle AOC) = \text{ar}(\triangle AOD) \text{ --- (i)}$$

also,

In $\triangle BCD$,

BO is the median. (CD is bisected by AB at O)

$$\therefore \text{ar}(\triangle BOC) = \text{ar}(\triangle BOD) \text{ --- (ii)}$$

Adding (i) and (ii) we get,

$$\text{ar}(\triangle AOC) + \text{ar}(\triangle BOC) = \text{ar}(\triangle AOD) + \text{ar}(\triangle BOD)$$

$$\Rightarrow \text{ar}(\triangle ABC) = \text{ar}(\triangle ABD)$$

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5. D, E and F are respectively the mid-points of the sides BC, CA and AB of a $\triangle ABC$.

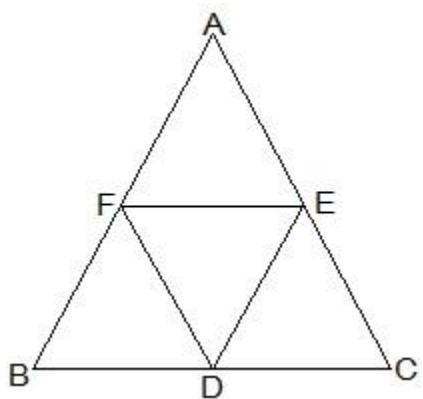
Show that

- (i) BDEF is a parallelogram. (ii) $\text{ar}(\triangle DEF) = \frac{1}{4} \text{ar}(\triangle ABC)$

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(iii) $\text{ar}(\text{BDEF}) = \frac{1}{2} \text{ar}(\text{ABC})$

Answer



(i) In $\triangle ABC$,

$EF \parallel BC$ and $EF = \frac{1}{2} BC$ (by mid point theorem)

also,

$BD = \frac{1}{2} BC$ (D is the mid point)

So, $BD = EF$

also,

BF and DE will also parallel and equal to each other.

Thus, the pair opposite sides are equal in length and parallel to each other.

$\therefore$ BDEF is a parallelogram.

(ii) Proceeding from the result of (i),

BDEF, DCEF, AFDE are parallelograms.

Diagonal of a parallelogram divides it into two triangles of equal area.

$\therefore \text{ar}(\triangle BFD) = \text{ar}(\triangle DEF)$ (For parallelogram BDEF) --- (i)

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also,

$$\text{ar}(\triangle AFE) = \text{ar}(\triangle DEF) \text{ (For parallelogram DCEF) --- (ii)}$$

$$\text{ar}(\triangle CDE) = \text{ar}(\triangle DEF) \text{ (For parallelogram AFDE) --- (iii)}$$

From (i), (ii) and (iii)

$$\text{ar}(\triangle BFD) = \text{ar}(\triangle AFE) = \text{ar}(\triangle CDE) = \text{ar}(\triangle DEF)$$

$$\Rightarrow \text{ar}(\triangle BFD) + \text{ar}(\triangle AFE) + \text{ar}(\triangle CDE) + \text{ar}(\triangle DEF) = \text{ar}(\triangle ABC)$$

$$\Rightarrow 4 \text{ar}(\triangle DEF) = \text{ar}(\triangle ABC)$$

$$\Rightarrow \text{ar}(\triangle DEF) = \frac{1}{4} \text{ar}(\triangle ABC)$$

$$\text{(iii) Area (parallelogram BDEF) = ar}(\triangle DEF) + \text{ar}(\triangle BDE)$$

$$\Rightarrow \text{ar}(\text{parallelogram BDEF}) = \text{ar}(\triangle DEF) + \text{ar}(\triangle DEF)$$

$$\Rightarrow \text{ar}(\text{parallelogram BDEF}) = 2 \times \text{ar}(\triangle DEF) \Rightarrow \text{ar}(\text{parallelogram BDEF}) = 2 \times \frac{1}{4} \text{ar}(\triangle ABC) \Rightarrow \text{ar}(\text{parallelogram BDEF}) = \frac{1}{2} \text{ar}(\triangle ABC)$$

6. In Fig. 9.25, diagonals AC and BD of quadrilateral ABCD intersect at O such that OB = OD.

If AB = CD, then show that:

$$\text{(i) ar}(\triangle DOC) = \text{ar}(\triangle AOB)$$

$$\text{(ii) ar}(\triangle DCB) = \text{ar}(\triangle ACB)$$

$$\text{(iii) DA} \parallel \text{CB or ABCD is a parallelogram.}$$

[Hint : From D and B, draw perpendiculars to AC.]

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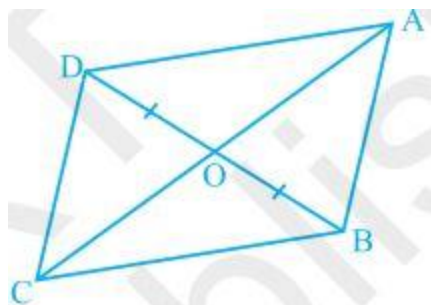


Fig. 9.25

Answer

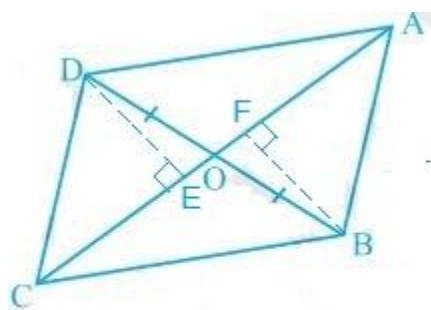


Fig. 9.25

Given,

$OB = OD$ and $AB = CD$

Construction,

$DE \perp AC$ and $BF \perp AC$ are drawn.

Proof:

(i) In $\triangle DOE$ and $\triangle BOF$,

$\angle DEO = \angle BFO$ (Perpendiculars)

$\angle DOE = \angle BOF$ (Vertically opposite angles)

$OD = OB$ (Given)

Therefore, $\triangle DOE \cong \triangle BOF$ by AAS congruence condition.

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Thus, $DE = BF$ (By CPCT) --- (i)

also, $\text{ar}(\triangle DOE) = \text{ar}(\triangle BOF)$ (Congruent triangles) --- (ii)

Now,

In $\triangle DEC$ and $\triangle BFA$,

$\angle DEC = \angle BFA$ (Perpendiculars)

$CD = AB$ (Given)

$DE = BF$ (From i)

Therefore, $\triangle DEC \cong \triangle BFA$ by RHS congruence condition.

Thus, $\text{ar}(\triangle DEC) = \text{ar}(\triangle BFA)$ (Congruent triangles) --- (iii)

Adding (ii) and (iii),

$\text{ar}(\triangle DOE) + \text{ar}(\triangle DEC) = \text{ar}(\triangle BOF) + \text{ar}(\triangle BFA)$

$\Rightarrow \text{ar}(\triangle DOC) = \text{ar}(\triangle AOB)$

(ii) $\text{ar}(\triangle DOC) = \text{ar}(\triangle AOB)$

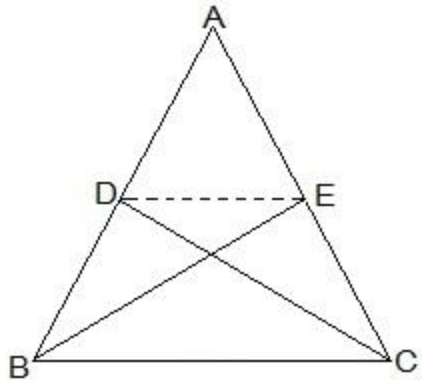
$\Rightarrow \text{ar}(\triangle DOC) + \text{ar}(\triangle OCB) = \text{ar}(\triangle AOB) + \text{ar}(\triangle OCB)$ (Adding $\text{ar}(\triangle OCB)$ to both sides)

$\Rightarrow \text{ar}(\triangle DCB) = \text{ar}(\triangle ACB)$ (iii) $\text{ar}(\triangle DCB) = \text{ar}(\triangle ACB)$ If two triangles are having same base and equal areas, these will be between same parallels $DA \parallel BC$ --- (iv) For quadrilateral ABCD, one pair of opposite sides are equal ($AB = CD$) and other pair of opposite sides are parallel. Therefore, ABCD is parallelogram.

7. D and E are points on sides AB and AC respectively of $\triangle ABC$ such that $\text{ar}(\triangle DBC) = \text{ar}(\triangle EBC)$. Prove that $DE \parallel BC$.

Answer

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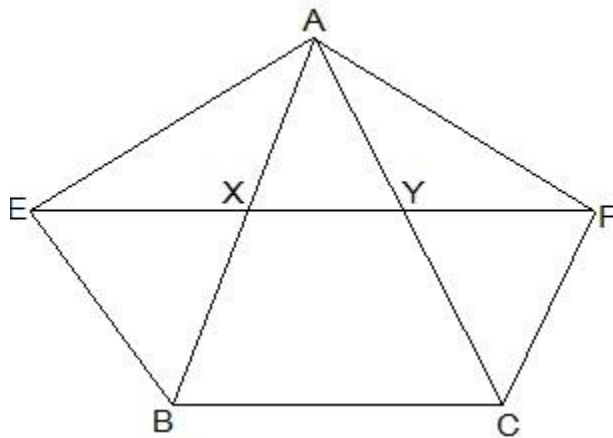


$\triangle DBC$ and $\triangle ECB$ are on the same base BC and also having equal areas. Therefore, they will lie between the same parallel lines. Thus, $DE \parallel BC$.

8. XY is a line parallel to side BC of a triangle ABC . If $BE \parallel AC$ and $CF \parallel AB$ meet XY at E and F respectively, show that

$$\text{ar}(\triangle ABE) = \text{ar}(\triangle ACF)$$

Answer



Given,

$XY \parallel BC$, $BE \parallel AC$ and $CF \parallel AB$

To show,

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$$\text{ar}(\triangle ABE) = \text{ar}(\triangle AC)$$

Proof:

$$EY \parallel BC \text{ (XY \parallel BC) --- (i)}$$

also,

$$BE \parallel CY \text{ (BE \parallel AC) --- (ii)}$$

From (i) and (ii),

BEYC is a parallelogram. (Both the pairs of opposite sides are parallel.)

Similarly,

BXFC is a parallelogram.

Parallelograms on the same base BC and between the same parallels EF and BC.

$$\Rightarrow \text{ar}(\triangle BEYC) = \text{ar}(\triangle BXFC) \text{ (Parallelograms on the same base BC and between the same parallels EF and BC) --- (iii)}$$

Also,

$\triangle AEB$ and parallelogram BEYC are on the same base BE and between the same parallels BE and AC.

$$\Rightarrow \text{ar}(\triangle AEB) = \frac{1}{2}\text{ar}(\triangle BEYC) \text{ --- (iv)}$$

Similarly,

$\triangle ACF$ and parallelogram BXFC on the same base CF and between the same parallels CF and AB.

$$\Rightarrow \text{ar}(\triangle ACF) = \frac{1}{2}\text{ar}(\triangle BXFC) \text{ --- (v)}$$

From (iii), (iv) and (v),

$$\text{ar}(\triangle AEB) = \text{ar}(\triangle ACF)$$

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9. The side AB of a parallelogram ABCD is produced to any point P. A line through A and parallel to CP meets CB produced at Q and then parallelogram PBQR is completed (see Fig. 9.26). Show that

$$\text{ar}(\text{ABCD}) = \text{ar}(\text{PBQR}).$$

[Hint : Join AC and PQ. Now compare $\text{ar}(\triangle ACQ)$ and $\text{ar}(\triangle APQ)$.]

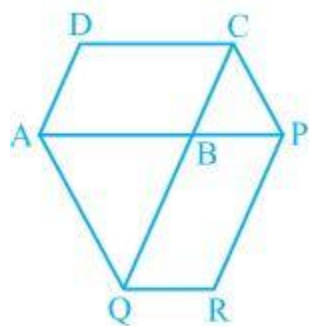


Fig. 9.26

Answer

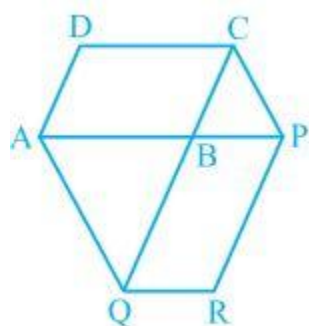


Fig. 9.26

AC and PQ are joined.

$\text{ar}(\triangle ACQ) = \text{ar}(\triangle APQ)$ (On the same base AQ and between the same parallel lines AQ and CP)

$$\Rightarrow \text{ar}(\triangle ACQ) - \text{ar}(\triangle ABQ) = \text{ar}(\triangle APQ) - \text{ar}(\triangle ABQ)$$

$$\Rightarrow \text{ar}(\triangle ABC) = \text{ar}(\triangle QBP) \text{ --- (i)}$$

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AC and QP are diagonals ABCD and PBQR. Thus,

$$\text{ar}(\triangle ABC) = \frac{1}{2} \text{ar}(\text{ABCD}) \text{ --- (ii)}$$

$$\text{ar}(\triangle QBP) = \frac{1}{2} \text{ar}(\text{PBQR}) \text{ --- (iii)}$$

From (ii) and (iii),

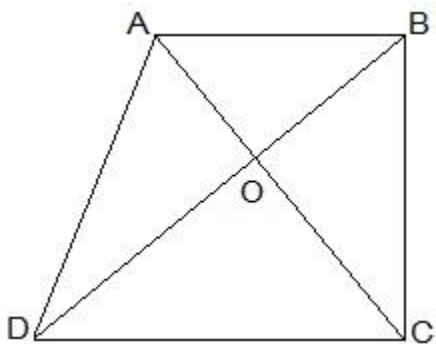
$$\frac{1}{2} \text{ar}(\text{ABCD}) = \frac{1}{2} \text{ar}(\text{PBQR})$$

$$\Rightarrow \text{ar}(\text{ABCD}) = \text{ar}(\text{PBQR})$$

NCERT 9th Maths Chapter 9, class 9 Maths Chapter 9 solutions

10. Diagonals AC and BD of a trapezium ABCD with $AB \parallel DC$ intersect each other at O. Prove that $\text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$.

Answer



$\triangle DAC$ and $\triangle DBC$ lie on the same base DC and between the same parallels AB and CD.

$$\therefore \text{ar}(\triangle DAC) = \text{ar}(\triangle DBC)$$

$$\Rightarrow \text{ar}(\triangle DAC) - \text{ar}(\triangle DOC) = \text{ar}(\triangle DBC) - \text{ar}(\triangle DOC)$$

$$\Rightarrow \text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$$

11. In Fig. 9.27, ABCDE is a pentagon. A line through B parallel to AC meets DC produced at F.

Show that

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(i) $\text{ar}(\triangle ACB) = \text{ar}(\triangle ACF)$

(ii) $\text{ar}(\triangle AEDF) = \text{ar}(\triangle ABCDE)$

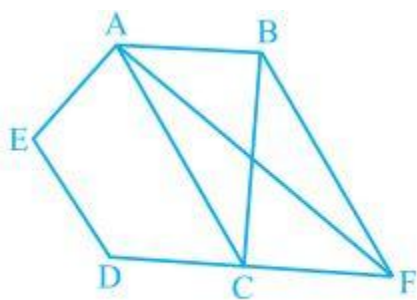


Fig. 9.27

Answer

(i) $\triangle ACB$ and $\triangle ACF$ lie on the same base AC and between the same parallels AC and BF .

$$\therefore \text{ar}(\triangle ACB) = \text{ar}(\triangle ACF)$$

$$(ii) \text{ar}(\triangle ACB) = \text{ar}(\triangle ACF)$$

$$\Rightarrow \text{ar}(\triangle ACB) + \text{ar}(\triangle ACDE) = \text{ar}(\triangle ACF) + \text{ar}(\triangle ACDE)$$

$$\Rightarrow \text{ar}(\triangle ABCDE) = \text{ar}(\triangle AEDF)$$

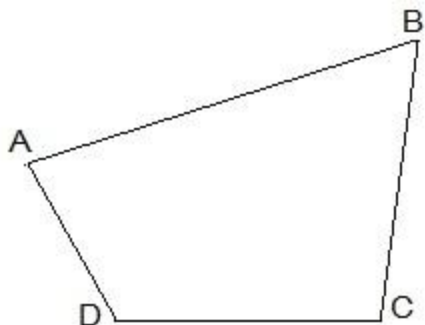
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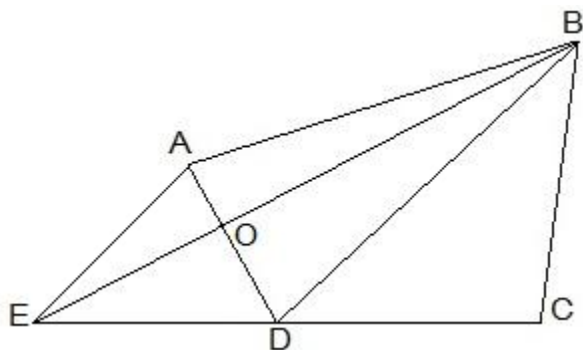
12. A villager Itwaari has a plot of land of the shape of a quadrilateral. The Gram Panchayat of the village decided to take over some portion of his plot from one of the corners to construct a Health Centre. Itwaari agrees to the above proposal with the condition that he should be given equal amount of land in lieu of his land adjoining his plot so as to form a triangular plot. Explain how this proposal will be implemented.

Answer

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Let ABCD be the plot of the land of the shape of a quadrilateral.



Construction,

Diagonal BD is joined. AE is drawn parallel BD. BE is joined which intersected AD at O. $\triangle BCE$ is the shape of the original field and $\triangle AOB$ is the area for constructing health centre. Also, $\triangle DEO$ land joined to the plot.

To prove:

$$\text{ar}(\triangle DEO) = \text{ar}(\triangle AOB)$$

Proof:

$\triangle DEB$ and $\triangle DAB$ lie on the same base BD and between the same parallel lines BD and AE.

$$\text{ar}(\triangle DEB) = \text{ar}(\triangle DAB)$$

$$\Rightarrow \text{ar}(\triangle DEB) - \text{ar}(\triangle DOB) = \text{ar}(\triangle DAB) - \text{ar}(\triangle DOB)$$

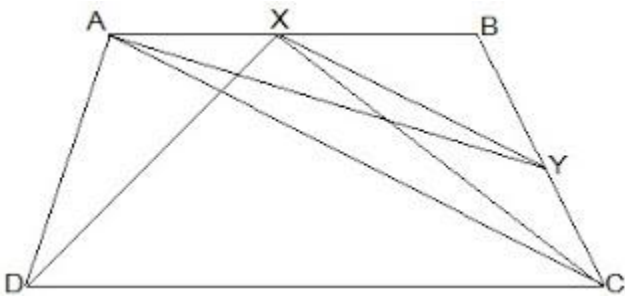
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$$\Rightarrow \text{ar}(\triangle DEO) = \text{ar}(\triangle AOB)$$

13. ABCD is a trapezium with $AB \parallel DC$. A line parallel to AC intersects AB at X and BC at Y. Prove that $\text{ar}(\triangle ADX) = \text{ar}(\triangle ACY)$.

[Hint : Join CX.]

Answer



Given,

ABCD is a trapezium with $AB \parallel DC$.

$XY \parallel AC$

Construction,

CX is joined.

To Prove,

$$\text{ar}(\triangle ADX) = \text{ar}(\triangle ACY)$$

Proof:

$\text{ar}(\triangle ADX) = \text{ar}(\triangle AXC)$ --- (i) (On the same base AX and between the same parallels AB and CD)

also,

$\text{ar}(\triangle AXC) = \text{ar}(\triangle ACY)$ --- (ii) (On the same base AC and between the same parallels XY and AC.)

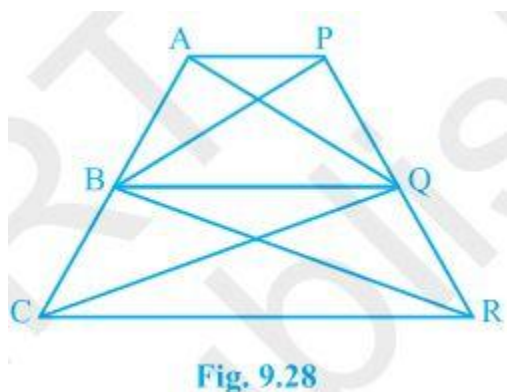
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From (i) and (ii),

$$\text{ar}(\triangle ADX) = \text{ar}(\triangle ACY)$$

14. In Fig.9.28, $AP \parallel BQ \parallel CR$. Prove that

$$\text{ar}(\triangle AQC) = \text{ar}(\triangle PBR).$$



Answer

Given,

$$AP \parallel BQ \parallel CR$$

To Prove,

$$\text{ar}(\triangle AQC) = \text{ar}(\triangle PBR)$$

Proof:

$\text{ar}(\triangle AQB) = \text{ar}(\triangle PBQ)$ --- (i) (On the same base BQ and between the same parallels AP and BQ.)

also,

$\text{ar}(\triangle BQC) = \text{ar}(\triangle BQR)$ --- (ii) (On the same base BQ and between the same parallels BQ and CR.)

Adding (i) and (ii),

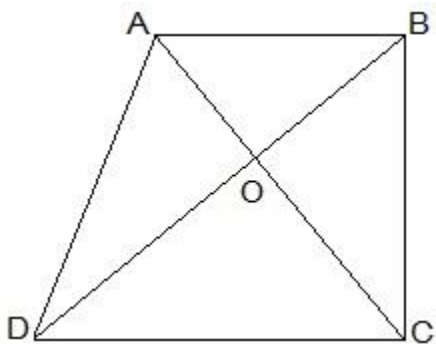
$$\text{ar}(\triangle AQB) + \text{ar}(\triangle BQC) = \text{ar}(\triangle PBQ) + \text{ar}(\triangle BQR)$$

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$$\Rightarrow \text{ar}(\triangle AQC) = \text{ar}(\triangle PBR)$$

15. Diagonals AC and BD of a quadrilateral ABCD intersect at O in such a way that $\text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$. Prove that ABCD is a trapezium.

Answer



Given,

$$\text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$$

To Prove,

ABCD is a trapezium.

Proof:

$$\text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$$

$$\Rightarrow \text{ar}(\triangle AOD) + \text{ar}(\triangle AOB) = \text{ar}(\triangle BOC) + \text{ar}(\triangle AOB)$$

$$\Rightarrow \text{ar}(\triangle ADB) = \text{ar}(\triangle ACB)$$

Areas of $\triangle ADB$ and $\triangle ACB$ are equal. Therefore, they must lie between the same parallel lines.

Thus, $AB \parallel CD$

Therefore, ABCD is a trapezium.

16. In Fig.9.29, $\text{ar}(\triangle DRC) = \text{ar}(\triangle DPC)$ and $\text{ar}(\triangle BDP) = \text{ar}(\triangle ARC)$. Show that both the quadrilaterals ABCD and DCPR are trapeziums.

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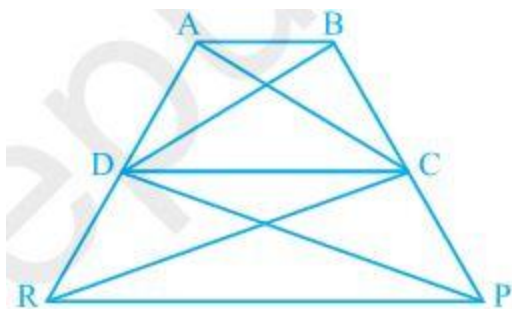


Fig. 9.29

Answer

Given,

$$\text{ar}(\triangle DRC) = \text{ar}(\triangle DPC) \text{ and } \text{ar}(\triangle BDP) = \text{ar}(\triangle ARC)$$

To Prove,

ABCD and DCPR are trapeziums.

Proof:

$$\text{ar}(\triangle BDP) = \text{ar}(\triangle ARC)$$

$$\Rightarrow \text{ar}(\triangle BDP) - \text{ar}(\triangle DPC) = \text{ar}(\triangle DRC)$$

$$\Rightarrow \text{ar}(\triangle BDC) = \text{ar}(\triangle ADC)$$

$\text{ar}(\triangle BDC) = \text{ar}(\triangle ADC)$. Therefore, they must lying between the same parallel lines.

Thus, $AB \parallel CD$

Therefore, ABCD is a trapezium.

also,

$\text{ar}(\triangle DRC) = \text{ar}(\triangle DPC)$. Therefore, they must lying between the same parallel lines.

Thus, $DC \parallel RP$

Therefore, DCPR is a trapezium.

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In the Chapter 9 Areas of Parallelograms and Triangles, we are focused on the relationship between the areas of these geometric figures under the condition when they lie on the same base and between the same parallels.

- **Figures on the Same Base and Between the Same Parallels:** Two figures are said to be on the same base and between the same parallels, if they have a common base (side) and the vertices (or the vertex) opposite to the common base of each figure lie on a line parallel to the base.
- **Parallelograms on the same Base and Between the same Parallels:** Parallelograms on the same base and between the same parallels are equal in area.
- **Triangles on the same Base and between the same Parallels:** Two triangles on the same base (or equal bases) and between the same parallels are equal in area. Two triangles having the same base (or equal bases) and equal areas lie between the same parallels.

There are total 4 exercises in the **Chapter 9 Class 9 Maths NCERT Solutions** which are very important for examinations purpose. We have prepared exercisewise NCERT Solutions of every questions which can find from the given links.

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NCERT Solutions is one of the best way through which one can understand all the topics given in the Chapter 9 Class 9 Maths. Through the help of these solutions, one will be able to solve supplementary books and exemplar questions as well.

What is the Area of a parallelogram?

Area of a parallelogram = base $\times$ height.

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- Chapter 7 Triangles
- Chapter 8 Quadrilaterals
- Chapter 9 Areas of Parallelograms and Triangles
- Chapter 10 Circles
- Chapter 11 Constructions
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