



NCERT Solutions for Class 10th Mathematics: Chapter 7 Coordinate Geometry



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NCERT Solutions for Class 10th Maths Chapter 7 - Coordinate Geometry

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NCERT 10th Mathematics Chapter 7, class 10 Mathematics Chapter 7 solutions

Page No. 161

Exercise 7.1

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1. Find the distance between the following pairs of points:

(i) (2, 3), (4, 1) (ii) (-5, 7), (-1, 3) (iii) (a, b), (-a, -b)

Answer

(i) Distance between the points is given by

$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Therefore, the distance between (2,3) and (4,1) is given by

$$\begin{aligned}l &= \sqrt{(2 - 4)^2 + (3 - 1)^2} \\ &= \sqrt{(-2)^2 + (2)^2} \\ &= \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2}\end{aligned}$$

(ii) Distance between (-5, 7) and (-1, 3) is given by

$$\begin{aligned}l &= \sqrt{(-5 - (-1))^2 + (7 - 3)^2} \\ &= \sqrt{(-4)^2 + (4)^2} \\ &= \sqrt{16 + 16} = \sqrt{32} = 4\sqrt{2}\end{aligned}$$

(iii) Distance between (a, b) and (-a, -b) is given by

$$\begin{aligned}l &= \sqrt{(a - (-a))^2 + (b - (-b))^2} \\ &= \sqrt{(2a)^2 + (2b)^2} \\ &= \sqrt{4a^2 + 4b^2} = 2\sqrt{a^2 + b^2}\end{aligned}$$

2. Find the distance between the points (0, 0) and (36, 15). Can you now find the distance between the two towns A and B discussed in Section 7.2.

Answer

Distance between points (0, 0) and (36, 15)

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$$\begin{aligned} &= \sqrt{(36 - 0)^2 + (15 - 0)^2} \\ &= \sqrt{36^2 + 15^2} \\ &= \sqrt{1296 + 225} = \sqrt{1521} = 39 \end{aligned}$$

Yes, Assume town A at origin point (0, 0).

Therefore, town B will be at point (36, 15) with respect to town A.

And hence, as calculated above, the distance between town A and B will be 39 km.

3. Determine if the points (1, 5), (2, 3) and (-2, -11) are collinear.

Answer

Let the points (1, 5), (2, 3), and (-2, -11) be representing the vertices A, B, and C of the given triangle respectively. Let A = (1, 5), B = (2, 3) and C = (-2, -11)

$$\begin{aligned} \therefore AB &= \sqrt{(1 - 2)^2 + (5 - 3)^2} = \sqrt{5} \\ BC &= \sqrt{(2 - (-2))^2 + (3 - (-11))^2} = \sqrt{4^2 + 14^2} = \sqrt{16 + 196} = \sqrt{212} \\ CA &= \sqrt{(1 - (-2))^2 + (5 - (-11))^2} = \sqrt{3^2 + 16^2} = \sqrt{9 + 256} = \sqrt{265} \end{aligned}$$

Since $AB + BC \neq CA$

Therefore, the points (1, 5), (2, 3), and (-2, -11) are not collinear.

4. Check whether (5, -2), (6, 4) and (7, -2) are the vertices of an isosceles triangle.

Answer

Let the points (5, -2), (6, 4), and (7, -2) are representing the vertices A, B, and C of the given triangle respectively.

$$\begin{aligned} AB &= \sqrt{(5 - 6)^2 + (-2 - 4)^2} = \sqrt{(-1)^2 + (6)^2} = \sqrt{1 + 36} = \sqrt{37} \\ BC &= \sqrt{(6 - 7)^2 + (4 - (-2))^2} = \sqrt{(-1)^2 + (6)^2} = \sqrt{1 + 36} = \sqrt{37} \\ CA &= \sqrt{(5 - 7)^2 + (-2 - (-2))^2} = \sqrt{(-2)^2 + 0^2} = 2 \end{aligned}$$

Therefore, $AB = BC$

As two sides are equal in length, therefore, ABC is an isosceles triangle.

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5. In a classroom, 4 friends are seated at the points A, B, C and D as shown in the following figure. Champa and Chameli walk into the class and after observing for a few minutes Champa asks Chameli, “Don't you think ABCD is a square?” Chameli disagrees.

Using distance formula, find which of them is correct.

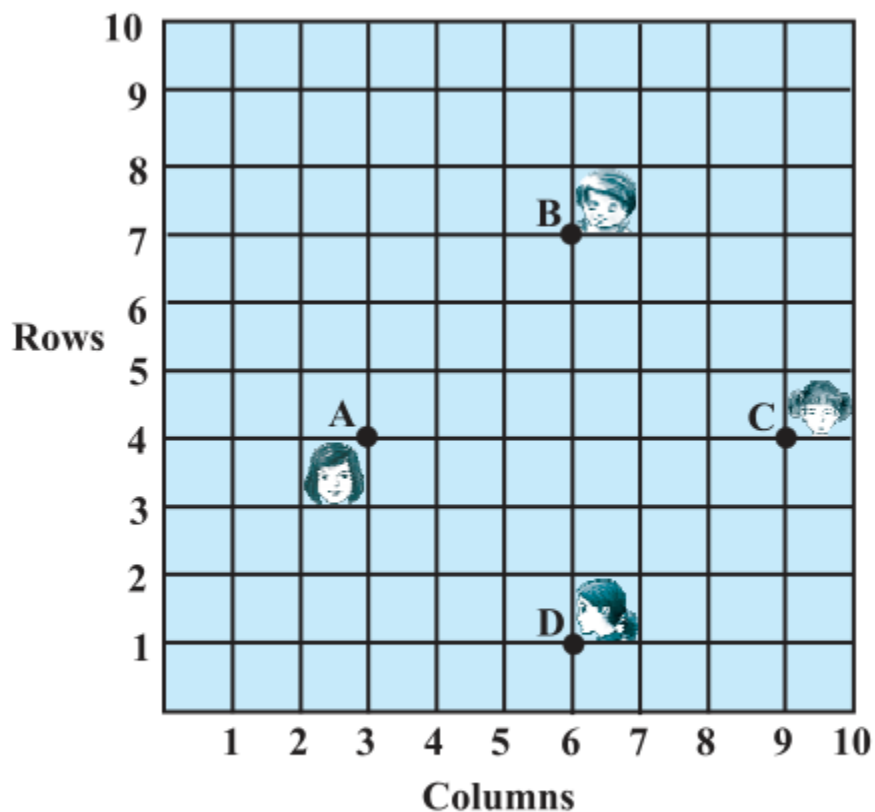


Fig. 7.8

Answer

Clearly from the figure, the coordinates of points A, B, C and D are (3, 4), (6, 7), (9, 4) and (6, 1).

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By using distance formula, we get

$$AB = \sqrt{(3-6)^2 + (4-7)^2} = \sqrt{(-3)^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$BC = \sqrt{(6-9)^2 + (7-4)^2} = \sqrt{(-3)^2 + 3^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$CB = \sqrt{(9-6)^2 + (4-1)^2} = \sqrt{(3)^2 + (3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$AD = \sqrt{(3-6)^2 + (4-1)^2} = \sqrt{(-3)^2 + (3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$\text{Diagonal AC} = \sqrt{(3-9)^2 + (4-4)^2} = \sqrt{(-6)^2 + 0^2} = 6$$

$$\text{Diagonal BD} = \sqrt{(6-6)^2 + (7-1)^2} = \sqrt{0^2 + (6)^2} = 6$$

It can be observed that all sides of this quadrilateral ABCD are of the same length and also the diagonals are of the same length.

Therefore, ABCD is a square and hence, Champa was correct

6. Name the type of quadrilateral formed, if any, by the following points, and give reasons for your answer:

(i) (-1, -2), (1, 0), (-1, 2), (-3, 0)

(ii) (-3, 5), (3, 1), (0, 3), (-1, -4)

(iii) (4, 5), (7, 6), (4, 3), (1, 2)

Answer

Let the points (-1, -2), (1, 0), (-1, 2), and (-3, 0) be representing the vertices A, B, C, and D of the given quadrilateral respectively.

$$\therefore AB = \sqrt{(-1-1)^2 + (-2-0)^2} = \sqrt{(-2)^2 + (-2)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$BC = \sqrt{(1-(-1))^2 + (0-2)^2} = \sqrt{(2)^2 + (-2)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$CD = \sqrt{(-1-(-3))^2 + (2-0)^2} = \sqrt{(2)^2 + (2)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$AD = \sqrt{(-1-(-3))^2 + (-2-0)^2} = \sqrt{(2)^2 + (-2)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$\text{Diagonal AC} = \sqrt{(-1-(-1))^2 + (-2-2)^2} = \sqrt{0^2 + (-4)^2} = \sqrt{16} = 4$$

$$\text{Diagonal BD} = \sqrt{(1-(-3))^2 + (0-0)^2} = \sqrt{4^2 + 0^2} = \sqrt{16} = 4$$

It can be observed that all sides of this quadrilateral are of the same length and also, the diagonals are of the same length. Therefore, the given points are the vertices of a square.

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(ii) Let the points $(-3, 5)$, $(3, 1)$, $(0, 3)$, and $(-1, -4)$ be representing the vertices A, B, C, and D of the given quadrilateral respectively.

$$\therefore AB = \sqrt{(-3 - 3)^2 + (5 - 1)^2} = \sqrt{(-6)^2 + (4)^2} = \sqrt{36 + 16} = \sqrt{52} = 2\sqrt{13}$$

$$BC = \sqrt{(3 - 0)^2 + (1 - 3)^2} = \sqrt{(3)^2 + (-2)^2} = \sqrt{9 + 4} = \sqrt{13}$$

$$CD = \sqrt{(0 - (-1))^2 + (3 - (-4))^2} = \sqrt{(1)^2 + (7)^2} = \sqrt{1 + 49} = \sqrt{50} = 5\sqrt{2}$$

$$AD = \sqrt{(-3 - (-1))^2 + (5 - (-4))^2} = \sqrt{(-2)^2 + (9)^2} = \sqrt{4 + 81} = \sqrt{85}$$

It can be observed that all sides of this quadrilateral are of different lengths. Therefore, it can be said that it is only a general quadrilateral, and not specific such as square, rectangle, etc.

(iii) Let the points $(4, 5)$, $(7, 6)$, $(4, 3)$, and $(1, 2)$ be representing the vertices A, B, C, and D of the given quadrilateral respectively.

$$\therefore AB = \sqrt{(4 - 7)^2 + (5 - 6)^2} = \sqrt{(-3)^2 + (-1)^2} = \sqrt{9 + 1} = \sqrt{10}$$

$$BC = \sqrt{(7 - 4)^2 + (6 - 3)^2} = \sqrt{(3)^2 + (3)^2} = \sqrt{9 + 9} = \sqrt{18}$$

$$CD = \sqrt{(4 - 1)^2 + (3 - 2)^2} = \sqrt{(3)^2 + (1)^2} = \sqrt{9 + 1} = \sqrt{10}$$

$$AD = \sqrt{(4 - 1)^2 + (5 - 2)^2} = \sqrt{(3)^2 + (3)^2} = \sqrt{9 + 9} = \sqrt{18}$$

$$\text{Diagonal AC} = \sqrt{(4 - 4)^2 + (5 - 3)^2} = \sqrt{(0)^2 + (2)^2} = \sqrt{0 + 4} = 2$$

$$\text{Diagonal BD} = \sqrt{(7 - 1)^2 + (6 - 2)^2} = \sqrt{(6)^2 + (4)^2} = \sqrt{36 + 16} = \sqrt{52} = 2\sqrt{13}$$

It can be observed that opposite sides of this quadrilateral are of the same length. However, the diagonals are of different lengths. Therefore, the given points are the vertices of a parallelogram.

7. Find the point on the x-axis which is equidistant from $(2, -5)$ and $(-2, 9)$.

Answer

We have to find a point on x-axis. Therefore, its y-coordinate will be 0.

Let the point on x-axis be $(x, 0)$

$$\text{Distance between } (x, 0) \text{ and } (2, -5) = \sqrt{(x - 2)^2 + (0 - (-5))^2} = \sqrt{(x - 2)^2 + (5)^2}$$

$$\text{Distance between } (x, 0) \text{ and } (-2, 9) = \sqrt{(x - (-2))^2 + (0 - (-9))^2} = \sqrt{(x + 2)^2 + (9)^2}$$

By the given condition, these distances are equal in measure.

$$\sqrt{(x - 2)^2 + (5)^2} = \sqrt{(x + 2)^2 + (9)^2}$$

$$(x - 2)^2 + 25 = (x + 2)^2 + 81$$

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$$x^2 + 4 - 4x + 25 = x^2 + 4 + 4x + 81$$

$$8x = 25 - 81$$

$$8x = -56$$

$$x = -7$$

Therefore, the point is $(-7, 0)$.

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8. Find the values of y for which the distance between the points P $(2, -3)$ and Q $(10, y)$ is 10 units.

Answer

It is given that the distance between $(2, -3)$ and $(10, y)$ is 10.

$$\text{Therefore, } \sqrt{(2 - 10)^2 + (-3 - y)^2} = 10$$

$$\sqrt{(-8)^2 + (3 + y)^2} = 10$$

$$64 + (y + 3)^2 = 100$$

$$(y + 3)^2 = 36$$

$$y + 3 = \pm 6$$

$$y + 3 = +6 \text{ or } y + 3 = -6$$

Therefore, $y = 3$ or -9

9. If Q $(0, 1)$ is equidistant from P $(5, -3)$ and R $(x, 6)$, find the values of x . Also find the distance QR and PR.

Answer

$$PQ = QR$$

$$\sqrt{(5 - 0)^2 + (-3 - 1)^2} = \sqrt{(0 - x)^2 + (1 - 6)^2}$$

$$\sqrt{(-5)^2 + (-4)^2} = \sqrt{(-x)^2 + (-5)^2}$$

$$\sqrt{25 + 16} = \sqrt{x^2 + 25}$$

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$$41 = x^2 + 25$$

$$16 = x^2$$

$$x = \pm 4$$

Therefore, point R is (4, 6) or (-4, 6).

When point R is (4, 6),

$$PR = \sqrt{(5-4)^2 + (-3-6)^2} = \sqrt{1^2 + (-9)^2} = \sqrt{1+81} = \sqrt{82}$$

$$QR = \sqrt{(0-4)^2 + (1-6)^2} = \sqrt{(-4)^2 + (-5)^2} = \sqrt{16+25} = \sqrt{41}$$

When point R is (-4, 6),

$$PR = \sqrt{(5-(-4))^2 + (-3-6)^2} = \sqrt{(9)^2 + (-9)^2} = \sqrt{81+81} = 9\sqrt{2}$$

$$QR = \sqrt{(0-(-4))^2 + (1-6)^2} = \sqrt{(4)^2 + (-5)^2} = \sqrt{16+25} = \sqrt{41}$$

10. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (-3, 4).

Answer

Point (x, y) is equidistant from (3, 6) and (-3, 4).

$$\therefore \sqrt{(x-3)^2 + (y-6)^2} = \sqrt{(x-(-3))^2 + (y-4)^2}$$

$$\sqrt{(x-3)^2 + (y-6)^2} = \sqrt{(x+3)^2 + (y-4)^2}$$

$$(x-3)^2 + (y-6)^2 = (x+3)^2 + (y-4)^2$$

$$x^2 + 9 - 6x + y^2 + 36 - 12y = x^2 + 9 + 6x + y^2 + 16 - 8y$$

$$36 - 16 = 6x + 6x + 12y - 8y$$

$$20 = 12x + 4y$$

$$3x + y = 5$$

$$3x + y - 5 = 0$$

Exercise 7.2

NCERT Solutions for Class 10th Maths Chapter 7: Exercise 7.2

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1. Find the coordinates of the point which divides the join of $(-1, 7)$ and $(4, -3)$ in the ratio 2:3.

Answer

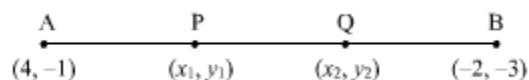
Let $P(x, y)$ be the required point. Using the section formula, we get

$$x = \frac{2 \times 4 + 3 \times (-1)}{2 + 3} = \frac{8 - 3}{5} = \frac{5}{5} = 1$$
$$y = \frac{2 \times (-3) + 3 \times 7}{2 + 3} = \frac{-6 + 21}{5} = \frac{15}{5} = 3$$

Therefore, the point is $(1, 3)$.

2. Find the coordinates of the points of trisection of the line segment joining $(4, -1)$ and $(-2, -3)$.

Answer



Let $P(x_1, y_1)$ and $Q(x_2, y_2)$ are the points of trisection of the line segment joining the given points i.e., $AP = PQ = QB$

Therefore, point P divides AB internally in the ratio 1:2.

$$x_1 = \frac{1 \times (-2) + 2 \times 4}{1 + 2}, y_1 = \frac{1 \times (-3) + 2 \times (-1)}{1 + 2}$$
$$x_1 = \frac{-2 + 8}{3} = \frac{6}{3} = 2, y_1 = \frac{-3 - 2}{3} = \frac{-5}{3}$$

Therefore, $P(x_1, y_1) = \left(2, \frac{-5}{3}\right)$

Point Q divides AB internally in the ratio 2:1.

$$x_2 = \frac{2 \times (-2) + 1 \times 4}{2 + 1}, y_2 = \frac{2 \times (-3) + 1 \times (-1)}{2 + 1}$$
$$x_2 = \frac{-4 + 4}{3} = 0, y_2 = \frac{-6 - 1}{3} = \frac{-7}{3}$$

$P(x_2, y_2) = \left(0, -\frac{7}{3}\right)$

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3. To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in the following figure. Niharika runs $\frac{1}{4}$ th the distance AD on the 2nd line and posts a green flag. Preet runs $\frac{1}{5}$ th the distance AD on the eighth line and posts a red flag. What is the distance between both the flags? If Rashmi has to post a blue flag exactly halfway between the line segment joining the two flags, where should she post her flag?

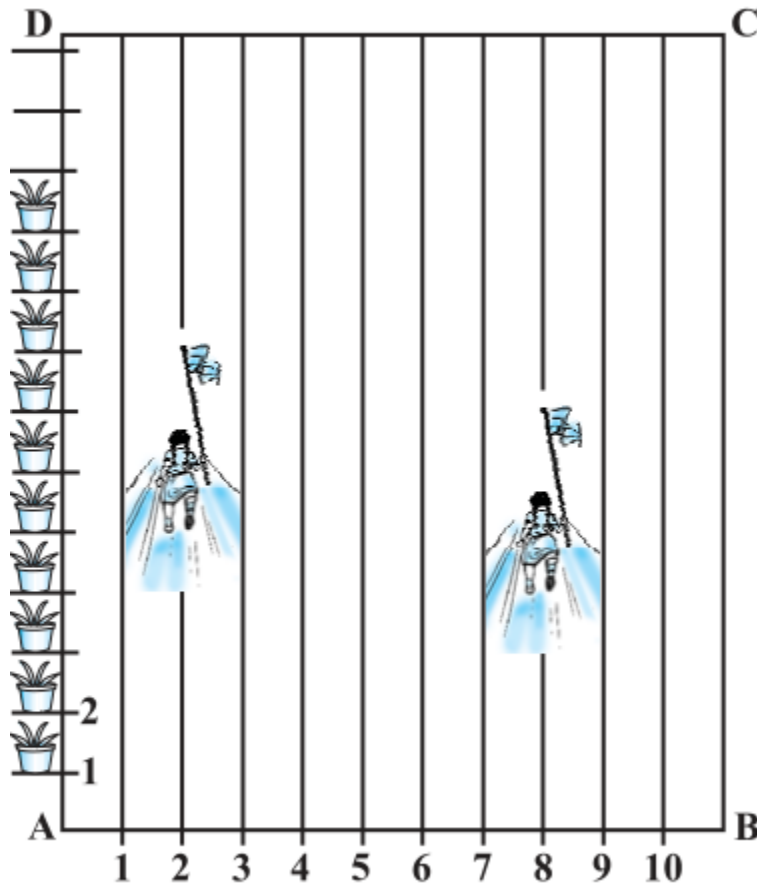


Fig. 7.12

Answer

It can be observed that Niharika posted the green flag at $\frac{1}{4}$ th of the distance AD i.e., $(1 \times 100/4)m = 25m$ from the starting point of 2nd line. Therefore, the coordinates of this point G is (2, 25).

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Similarly, Preet posted red flag at $\frac{1}{5}$ of the distance AD i.e., $(1 \times 100/5)$ m = 20m from the starting point of 8th line. Therefore, the coordinates of this point R are (8, 20).

Distance between these flags by using distance formula = GR

$$= \sqrt{(8 - 2)^2 + (25 - 20)^2} = \sqrt{36 + 25} = \sqrt{61}\text{m}$$

The point at which Rashmi should post her blue flag is the mid-point of the line joining these points. Let this point be $A(x, y)$.

$$x = \frac{2 + 8}{2}, y = \frac{25 + 20}{2}$$

$$x = \frac{10}{2}, y = \frac{45}{2} = 22.5$$

Hence, $A(x, y) = (5, 22.5)$

Therefore, Rashmi should post her blue flag at 22.5m on 5th line.

4. Find the ratio in which the line segment joining the points (-3, 10) and (6, -8) is divided by (-1, 6).

Answer

Let the ratio in which the line segment joining (-3, 10) and (6, -8) is divided by point (-1, 6) be $k:1$.

$$\text{Therefore, } -1 = \frac{6k - 3}{k + 1}$$

$$-k - 1 = 6k - 3$$

$$7k = 2$$

$$k = \frac{2}{7}$$

Therefore, the required ratio is 2:7.

NCERT 10th Mathematics Chapter 7, class 10 Mathematics Chapter 7 solutions

5. Find the ratio in which the line segment joining A (1, -5) and B (-4, 5) is divided by the x-axis. Also find the coordinates of the point of division.

Answer

Let the ratio in which the line segment joining A (1, -5) and B (-4, 5) is divided by x-axis be $k:1$.

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Therefore, the coordinates of the point of division is $(-4k+1/k+1, 5k-5/k+1)$.

We know that y-coordinate of any point on x-axis is 0.

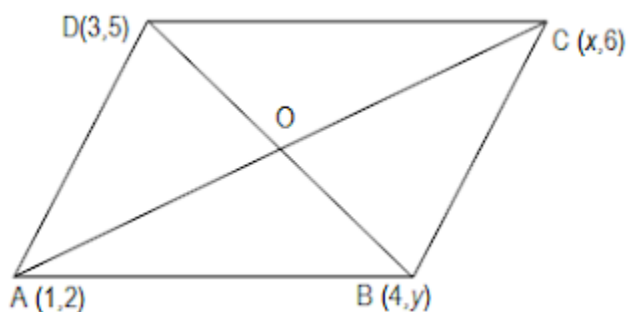
$$\therefore 5k-5/k+1 = 0$$

Therefore, x-axis divides it in the ratio 1:1.

$$\text{Division Point} = \left(\frac{-4(1)+1}{1+1}, \frac{5(1)-5}{1+1} \right) = \left(\frac{-4+1}{2}, \frac{5-5}{2} \right) = \left(\frac{-3}{2}, 0 \right)$$

6. If $(1, 2)$, $(4, y)$, $(x, 6)$ and $(3, 5)$ are the vertices of a parallelogram taken in order, find x and y .

Answer



Let A,B,C and D be the points $(1,2)$ $(4,y)$, $(x,6)$ and $(3,5)$ respectively.

$$\text{Mid point of diagonal AC is } \left(\frac{1+x}{2}, \frac{2+6}{2} \right) \Rightarrow \left(\frac{x+1}{2}, 4 \right)$$

$$\text{and Mid point of Diagonal BD is } \left(\frac{4+3}{2}, \frac{5+y}{2} \right) \Rightarrow \left(\frac{7}{2}, \frac{5+y}{2} \right)$$

Since the diagonals of a parallelogram bisect each other, the mid point of AC and BD are same.

$$\therefore x+1/2 = 7/2 \text{ and } 4 = 5+y/2$$

$$\Rightarrow x + 1 = 7 \text{ and } 5 + y = 8$$

$$\Rightarrow x = 6 \text{ and } y = 3$$

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7. Find the coordinates of a point A, where AB is the diameter of circle whose centre is (2, -3) and B is (1, 4).

Answer

Let the coordinates of point A be (x, y).

Mid-point of AB is (2, -3), which is the center of the circle.

$$\begin{aligned}\therefore (2, -3) &= \left(\frac{x+1}{2}, \frac{y+4}{2} \right) \\ \Rightarrow \frac{x+1}{2} &= 2 \text{ and } \frac{y+4}{2} = -3\end{aligned}$$

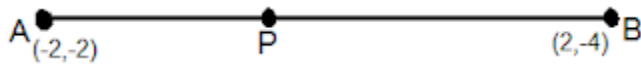
$$\Rightarrow x + 1 = 4 \text{ and } y + 4 = -6$$

$$\Rightarrow x = 3 \text{ and } y = -10$$

Therefore, the coordinates of A are (3, -10).

8. If A and B are (-2, -2) and (2, -4), respectively, find the coordinates of P such that $AP = \frac{3}{7} AB$ and P lies on the line segment AB.

Answer



The coordinates of point A and B are (-2, -2) and (2, -4) respectively.

Since $AP = \frac{3}{7} AB$

Therefore, $AP:PB = 3:4$

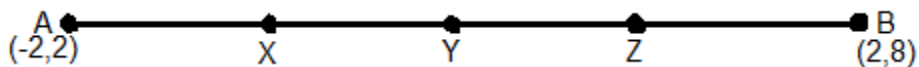
Point P divides the line segment AB in the ratio 3:4.

$$\begin{aligned}\text{Coordinates of P} &= \left(\frac{3 \times 2 + 4 \times (-2)}{3+4}, \frac{3 \times (-4) + 4 \times 2}{3+4} \right) \\ &= \left(\frac{6-8}{7}, \frac{-12-8}{7} \right) \\ &= \left(\frac{-2}{7}, \frac{-20}{7} \right)\end{aligned}$$

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9. Find the coordinates of the points which divide the line segment joining A (- 2, 2) and B (2, 8) into four equal parts.

Answer



From the figure, it can be observed that points X, Y, Z are dividing the line segment in a ratio 1:3, 1:1, 3:1 respectively.

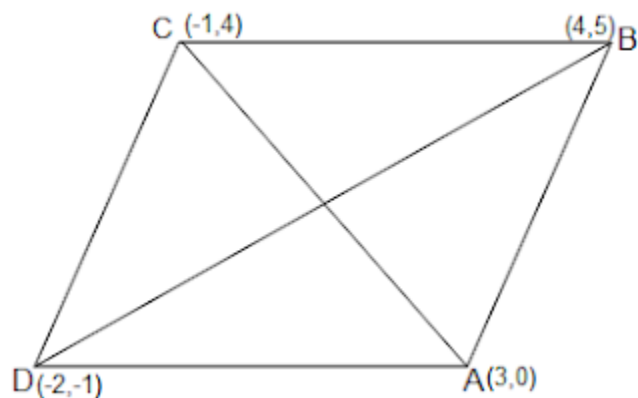
$$\begin{aligned} \text{Coordinates of X} &= \left(\frac{1 \times 2 + 3 \times (-2)}{1+3}, \frac{1 \times 8 + 3 \times 2}{1+3} \right) \\ &= \left(-1, \frac{7}{2} \right) \end{aligned}$$

$$\begin{aligned} \text{Coordinates of Y} &= \left(\frac{2 + (-2)}{2}, \frac{2+8}{2} \right) \\ &= (0, 5) \end{aligned}$$

$$\begin{aligned} \text{Coordinates of Z} &= \left(\frac{3 \times 2 + 1 \times (-2)}{3+1}, \frac{3 \times 8 + 1 \times 2}{3+1} \right) \\ &= \left(1, \frac{13}{2} \right) \end{aligned}$$

10. Find the area of a rhombus if its vertices are (3, 0), (4, 5), (-1, 4) and (-2,-1) taken in order. [Hint: Area of a rhombus = 1/2(product of its diagonals)]

Answer



Let (3, 0), (4, 5), (- 1, 4) and (- 2, - 1) are the vertices A, B, C, D of a rhombus ABCD.

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$$\begin{aligned}\text{Length of diagonal AC} &= \sqrt{[3 - (-1)]^2 + (0 - 4)^2} \\ &= \sqrt{16 + 16} = 4\sqrt{2}\end{aligned}$$

$$\begin{aligned}\text{Length of diagonal BD} &= \sqrt{[4 - (-2)]^2 + [5 - (-1)]^2} \\ &= \sqrt{36 + 36} = 6\sqrt{2}\end{aligned}$$

$$\begin{aligned}\text{Therefore, area of rhombus ABCD} &= \frac{1}{2} \times 4\sqrt{2} \times 6\sqrt{2} \\ &= 24 \text{ Square units}\end{aligned}$$

Exercises 7.3

NCERT 10th Mathematics Chapter 7, class 10 Mathematics Chapter 7 solutions

1. Find the area of the triangle whose vertices are:

(i) (2, 3), (-1, 0), (2, -4)

(ii) (-5, -1), (3, -5), (5, 2)

Answer

(i) Area of a triangle is given by

$$\text{Area of triangle} = \frac{1}{2} \{x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)\}$$

$$\text{Area of the given triangle} = \frac{1}{2} [2 \{0 - (-4)\} + (-1) \{(-4) - (3)\} + 2 \{3 - 0\}]$$

$$= \frac{1}{2} \{8 + 7 + 6\}$$

$$= 2\frac{1}{2} \text{ square units.}$$

$$\text{(ii) Area of the given triangle} = \frac{1}{2} [-5 \{(-5) - (4)\} + 3\{2 - (-1)\} + 5\{-1 - (-5)\}]$$

$$= \frac{1}{2} \{35 + 9 + 20\}$$

$$= 32 \text{ square units}$$

2. In each of the following find the value of 'k', for which the points are collinear.

(i) (7, -2), (5, 1), (3, -k)

(ii) (8, 1), (k, -4), (2, -5)

Answer

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(i) For collinear points, area of triangle formed by them is zero.

Therefore, for points (7, -2) (5, 1), and (3, k), area = 0

$$\frac{1}{2} [7 \{ 1 - k \} + 5(k - (-2)) + 3\{(-2) + 1\}] = 0$$

$$7 - 7k + 5k + 10 - 9 = 0$$

$$-2k + 8 = 0$$

$$k = 4$$

(ii) For collinear points, area of triangle formed by them is zero.

Therefore, for points (8, 1), (k, -4), and (2, -5), area = 0

$$\frac{1}{2} [8 \{ -4 - (-5) \} + k\{(-5) - (1)\} + 2\{1 - (-4)\}] = 0$$

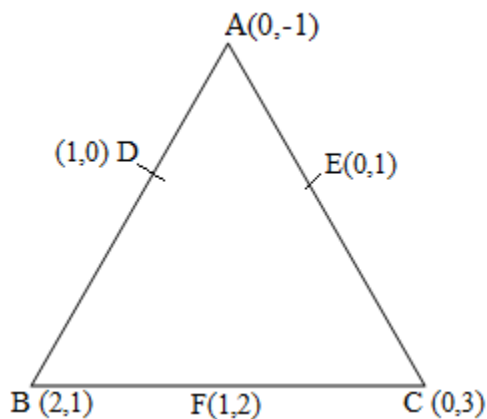
$$8 - 6k + 10 = 0$$

$$6k = 18$$

$$k = 3$$

3. Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are (0, -1), (2, 1) and (0, 3). Find the ratio of this area to the area of the given triangle.

Answer



Let the vertices of the triangle be A (0, -1), B (2, 1), C (0, 3).

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Let D, E, F be the mid-points of the sides of this triangle. Coordinates of D, E, and F are given by

$$D = (0+2/2, -1+1/2) = (1,0)$$

$$E = (0+0/2, -3-1/2) = (0,1)$$

$$F = (2+0/2, 1+3/2) = (1,2)$$

$$\text{Area of a triangle} = 1/2 \{x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)\}$$

$$\text{Area of } \triangle DEF = 1/2 \{1(2-1) + 1(1-0) + 0(0-2)\}$$

$$= 1/2 (1+1) = 1 \text{ square units}$$

$$\text{Area of } \triangle ABC = 1/2 [0(1-3) + 2\{3-(-1)\} + 0(-1-1)]$$

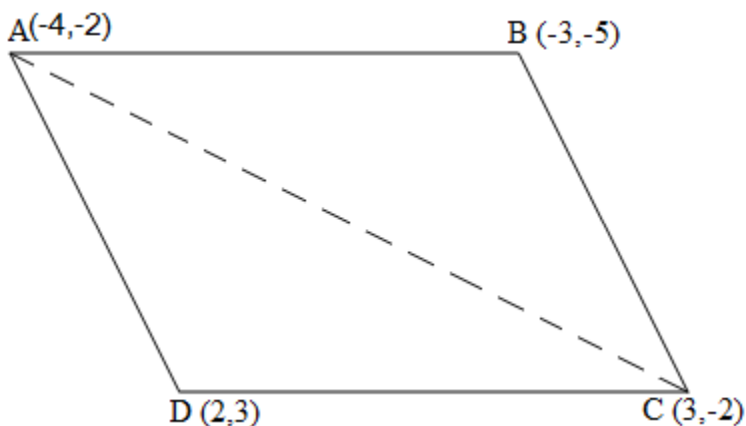
$$= 1/2 \{8\} = 4 \text{ square units}$$

Therefore, the required ratio is 1:4.

NCERT 10th Mathematics Chapter 7, class 10 Mathematics Chapter 7 solutions

4. Find the area of the quadrilateral whose vertices, taken in order, are (-4, -2), (-3, -5), (3, -2) and (2, 3).

Answer



Let the vertices of the quadrilateral be A (- 4, - 2), B (- 3, - 5), C (3, - 2), and D (2, 3). Join AC to form two triangles $\triangle ABC$ and $\triangle ACD$.

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$$\text{Area of a triangle} = \frac{1}{2} \{x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)\}$$

$$\text{Area of } \triangle ABC = \frac{1}{2} [(-4) \{(-5) - (-2)\} + (-3) \{(-2) - (-2)\} + 3 \{(-2) - (-5)\}]$$

$$= \frac{1}{2} (12+0+9)$$

$$= \frac{21}{2} \text{ square units}$$

$$\text{Area of } \triangle ACD = \frac{1}{2} [(-4) \{(-2) - (3)\} + 3\{(3) - (-2)\} + 2 \{(-2) - (-2)\}]$$

$$= \frac{1}{2} (20+15+0)$$

$$= \frac{35}{2} \text{ square units}$$

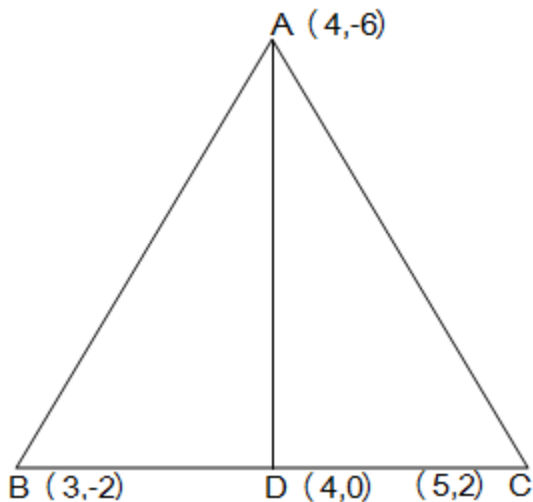
$$\text{Area of } \square ABCD = \text{Area of } \triangle ABC + \text{Area of } \triangle ACD$$

$$= (\frac{21}{2} + \frac{35}{2}) \text{ square units} = 28 \text{ square units}$$

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5. You have studied in Class IX that a median of a triangle divides it into two triangles of equal areas. Verify this result for $\triangle ABC$ whose vertices are A (4, -6), B (3, -2) and C (5, 2).

Answer



Let the vertices of the triangle be A (4, -6), B (3, -2), and C (5, 2).

Let D be the mid-point of side BC of $\triangle ABC$. Therefore, AD is the median in $\triangle ABC$.

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Coordinates of point D = $(3+5/2, -2+2/2) = (4,0)$

Area of a triangle = $1/2 \{x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)\}$

Area of $\Delta ABD = 1/2 [(4) \{(-2) - (0)\} + 3\{(0) - (-6)\} + (4) \{(-6) - (-2)\}]$

$$= 1/2 (-8+18-16)$$

$$= -3 \text{ square units}$$

However, area cannot be negative. Therefore, area of ΔABD is 3 square units.

Area of $\Delta ABD = 1/2 [(4) \{0 - (2)\} + 4\{(2) - (-6)\} + (5) \{(-6) - (0)\}]$

$$= 1/2 (-8+32-30)$$

$$= -3 \text{ square units}$$

However, area cannot be negative. Therefore, area of ΔABD is 3 square units.

The area of both sides is same. Thus, median AD has divided ΔABC in two triangles of equal areas.

NCERT 10th Mathematics Chapter 7, class 10 Mathematics Chapter 7 solutions



Chapterwise NCERT Solutions for Class 10 Maths:

- Chapter 1 Real Numbers
- Chapter 2 Polynomials
- Chapter 3 Pair of Linear Equations in Two Variables
- Chapter 4 Quadratic Equations
- Chapter 5 Arithmetic Progressions
- Chapter 6 Triangles
- Chapter 7 Coordinate Geometry
- Chapter 8 Introduction to Trigonometry
- Chapter 9 Applications of Trigonometry
- Chapter 10 Circle
- Chapter 11 Constructions
- Chapter 12 Areas related to Circles
- Chapter 13 Surface Areas and Volumes
- Chapter 14 Statistics
- Chapter 15 Probability

<https://www.indcareer.com/schools/ncert-solutions-for-class-10th-mathematics-chapter-7-coordinate-geometry/>

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