

## NCERT Solutions for 11th Class Physics:Chapter 8-Gravitation









# NCERT Solutions for 11th Class Physics: Chapter 8-Gravitation

Class 11: Physics Chapter 8 solutions. Complete Class 11 Physics Chapter 8 Notes.

# NCERT Solutions for 11th Class Physics: Chapter 8-Gravitation

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#### **Excercises**



#### 8.1. Answer the following:

- (a)You can shield a charge from electrical forces by putting it inside a hollow conductor. Can you shield a body from the gravitational influence of nearby matter by putting it inside a hollow sphere or by some other means?
- (b) An astronaut inside a small space ship orbiting around the earth cannot detect gravity. If the space station orbiting around the earth has a large size, can he hope to detect gravity?
- (c) If you compare the gravitational force on the earth due to the sun to that due to the moon, you would find that the Sun's pull is greater than the moon's pull. (You can check this yourself using the data available in the succeeding exercises). However, the tidal effect of the moon's pull is greater than the tidal effect of sun. Why?

#### **Answer**

- (a) We cannot shiwld a body from the gravitational influence of nearby matter, because the gravitational force on a body due to nearby matter is independent of the presence of other matter, whereas it is not so in case of electric forces. It means the gravitational screens are not possible.
- (b) Yes, if the size of the space station is large enough, then the astronaut will detect the change in Earth's gravity (a).
- (c) Tidal effect depends inversely upon the cube of the distance while, gravitational force depends inversely on the square of the distance. Since the distance between the Moon and the Earth is smaller than the distance between the Sun and the Earth, the tidal effect of the Moon's pull is greater than the tidal effect of the Sun's pull.

#### 8.2. Choose the correct alternative:





- (a) Acceleration due to gravity increases/decreases with increasing altitude.
- (b)Acceleration due to gravity increases/decreases with increasing depth. (assume the earth to be a sphere of uniform density).
- (c)Acceleration due to gravity is independent of mass of the earth/mass of the body.
- (d)The formula  $-G Mm(1/r_2-1/r_1)$  is more/less accurate than the formula  $mg(r_2-r_1)$  for the difference of potential energy between two points  $r_2$  and  $r_1$  distance away from the centre of the earth.

- (a) decreases
- (b) decreases
- (c) mass of the body
- (d) more.
- 8.3. Suppose there existed a planet that went around the sun twice as fast as the earth. What would be its orbital size as compared to that of the earth?

#### Answer

Time taken by the Earth to complete one revolution around the Sun,

$$T_{\rm e}$$
 = 1 year

Orbital radius of the Earth in its orbit,  $R_e = 1 \text{ AU}$ 

Time taken by the planet to complete one revolution around the Sun,  $T_P = \frac{1}{2}T_e = \frac{1}{2}$  year





Orbital radius of the planet =  $R_p$ 

From Kepler's third law of planetary motion, we can write:

$$(R_{\rm p}/R_{\rm e})^3 = (T_{\rm p}/T_{\rm e})^2$$

$$(R_{\rm p}/R_{\rm e}) = (T_{\rm p}/T_{\rm e})^{2/3}$$

$$= (1/2 / 1)^{2/3} = 0.5^{2/3} = 0.63$$

Hence, the orbital radius of the planet will be 0.63 times smaller than that of the Earth.

8.4. Io, one of the satellites of Jupiter, has an orbital period of 1.769 days and the radius of the orbit is  $4.22 \times 10^8$  m. Show that the mass of Jupiter is about one-thousandth that of the sun.

#### **Answer**

Orbital period of  $I_0$ ,  $T_{I0} = 1.769$  days =  $1.769 \times 24 \times 60 \times 60$  s

Orbital radius of  $I_0$ ,  $R_{I0} = 4.22 \times 10^8$  m

Satellite  $I_o$  is revolving around the Jupiter

Mass of the latter is given by the relation:

$$M_{\rm J} = 4\pi^2 R_{\rm Io}^3 / G T_{\rm Io}^2$$
 .....(i)

Where,

 $M_{\rm J}$  = Mass of Jupiter

G = Universal gravitational constant

Orbital period of the earth,

$$T_e = 365.25 \text{ days} = 365.25 \times 24 \times 60 \times 60 \text{ s}$$





Orbital radius of the Earth,

$$R_{\rm e} = 1 \, {\rm AU} = 1.496 \times 10^{11} \, {\rm m}$$

Mass of sun is given as:

$$M_{\rm s} = 4\pi^2 R_{\rm e}^3 / G T_{\rm e}^2$$
 .....(ii)

$$\therefore M_{\rm s} / M_{\rm J} = (4\pi^2 R_{\rm e}^3 / G T_{\rm e}^2) \times (G T_{\rm Io}^2 / 4\pi^2 R_{\rm Io}^3) = (R_{\rm e}^3 \times T_{\rm Io}^2) / (R_{\rm Io}^3 \times T_{\rm e}^2)$$

Substituting the values, we get:

= 
$$(1.769 \times 24 \times 60 \times 60 / 365.25 \times 24 \times 60 \times 60)^2 \times (1.496 \times 10^{11} / 4.22 \times 10^8)^3$$

$$= 1045.04$$

$$\therefore M_{\rm s}/M_{\rm J} \sim 1000$$

$$M_{\rm s} \sim 1000 \times M_{\rm J}$$

Hence, it can be inferred that the mass of Jupiter is about one-thousandth that of the Sun.

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8.5. Let us assume that our galaxy consists of  $2.5 \times 10^{11}$  stars each of one solar mass. How long will a star at a distance of 50,000 ly from the galactic centre take to complete one revolution? Take the diameter of the Milky Way to be  $10^5$  ly.

#### Answer

Mass of our galaxy Milky Way,  $M = 2.5 \times 10^{11}$  solar mass

Solar mass = Mass of Sun =  $2.0 \times 10^{36}$  kg

Mass of our galaxy,  $M = 2.5 \times 10^{11} \times 2 \times 10^{36} = 5 \times 10^{41} \text{ kg}$ 





Diameter of Milky Way,  $d = 10^5$  ly

Radius of Milky Way,  $r = 5 \times 10^4 \text{ ly}$ 

$$1 \text{ ly} = 9.46 \times 10^{15} \text{ m}$$

$$\therefore r = 5 \times 10^4 \times 9.46 \times 10^{15}$$

$$= 4.73 \times 10^{20} \text{ m}$$

Since a star revolves around the galactic centre of the Milky Way, its time period is given by the relation:

$$T = (4\pi^{2}r^{3} / GM)^{1/2}$$

$$= [(4 \times 3.14^{2} \times 4.73^{3} \times 10^{60}) / (6.67 \times 10^{-11} \times 5 \times 10^{41})]^{1/2}$$

$$= (39.48 \times 105.82 \times 10^{30} / 33.35)^{1/2}$$

$$= 1.12 \times 10^{16} \text{ s}$$

$$1 \text{ year} = 365 \times 324 \times 60 \times 60 \text{ s}$$

$$1s = 1 / (365 \times 324 \times 60 \times 60) \text{ years}$$

$$\therefore 1.12 \times 10^{16} \text{ s} = 1.12 \times 10^{16} / (365 \times 24 \times 60 \times 60) = 3.55 \times 10^{8} \text{ years.}$$

#### 8.6. Choose the correct alternative:

- (a) If the zero of potential energy is at infinity, the total energy of an orbiting satellite is negative of its kinetic/potential energy.
- (b) The energy required to launch an orbiting satellite out of earth's gravitational influence is more/less than the energy required to project a stationary object at the same height (as the satellite) out of earth's influence.

#### **Answer**





- (a) Kinetic energy
- (b) Less
- 8.7. Does the escape speed of a body from the earth depend on
- (a) the mass of the body,
- (b) the location from where it is projected,
- (c) the direction of projection,
- (d) the height of the location from where the body is launched?

The escape velocity is indpendent of the mass of the body and the direction of projection. It depends upon the gravitational potential at the point from where the body is launched. Since, this potential depends slightly on the latitude and height of the point, therefore, the escape velocity depends slightly on these factors.

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8.8. A comet orbits the Sun in a highly elliptical orbit. Does the comet have a constant (a) linear speed, (b) angular speed, (c) angular momentum, (d) kinetic energy, (e) potential energy, (f) total energy throughout its orbit? Neglect any mass loss of the comet when it comes very close to the Sun.

#### Answer

A comet while going on elliptical orbit around the Sun has constant angular momentum and totaal energy at all locations but other quantities vary with locations.





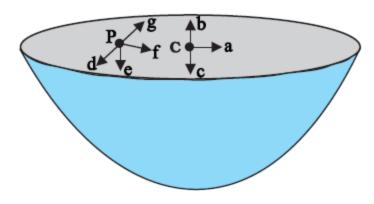
# 8.9. Which of the following symptoms is likely to afflict an astronaut in space (a) swollen feet, (b) swollen face, (c) headache, (d) orientational problem?

#### Answer

- (a) Legs hold the entire mass of a body in standing position due to gravitational pull. In space, an astronaut feels weightlessness because of the absence of gravity. Therefore, swollen feet of an astronaut do not affect him/her in space.
- (b) A swollen face is caused generally because of apparent weightlessness in space. Sense organs such as eyes, ears nose, and mouth constitute a person's face. This symptom can affect an astronaut in space.
- (c) Headaches are caused because of mental strain. It can affect the working of an astronaut in space.
- (d) Space has different orientations. Therefore, orientational problem can affect an astronaut in space.
- 8.10. Choose the correct answer from among the given ones: The gravitational intensity at the centre of a hemispherical shell of uniform mass density has the direction indicated by the arrow (see Fig 8.12) (i) a, (ii) b, (iii) c, (iv) O.





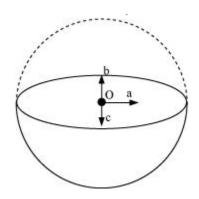


#### Fig. 8.12

#### **Answer**

Gravitational potential (V) is constant at all points in a spherical shell. Hence, the gravitational potential gradient (dV/dR) is zero everywhere inside the spherical shell. The gravitational potential gradient is equal to the negative of gravitational intensity. Hence, intensity is also zero at all points inside the spherical shell. This indicates that gravitational forces acting at a point in a spherical shell are symmetric.

If the upper half of a spherical shell is cut out (as shown in the given figure), then the net gravitational force acting on a particle located at centre O will be in the downward direction.







Since gravitational intensity at a point is defined as the gravitational force per unit mass at that point, it will also act in the downward direction. Thus, the gravitational intensity at centre O of the given hemispherical shell has the direction as indicated by arrow  ${\bf c}$ .

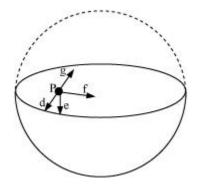
#### 8.11. Choose the correct answer from among the given ones:

For the problem 8.10, the direction of the gravitational intensity at an arbitrary point P is indicated by the arrow (i) d, (ii) e, (iii) f, (iv) g.

#### **Answer**

Gravitational potential (V) is constant at all points in a spherical shell. Hence, the gravitational potential gradient (dV/dR) is zero everywhere inside the spherical shell. The gravitational potential gradient is equal to the negative of gravitational intensity. Hence, intensity is also zero at all points inside the spherical shell. This indicates that gravitational forces acting at a point in a spherical shell are symmetric.

If the upper half of a spherical shell is cut out (as shown in the given figure), then the net gravitational force acting on a particle at an arbitrary point P will be in the downward direction.



Since gravitational intensity at a point is defined as the gravitational force per unit mass at that point, it will also act in the downward direction. Thus,





the gravitational intensity at an arbitrary point P of the hemispherical shell has the direction as indicated by arrow  $\mathbf{e}$ .

Hence, the correct answer is (ii).

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8.12. A rocket is fired from the earth towards the sun. At what distance from the earth's centre is the gravitational force on the rocket zero? Mass of the sun =  $2 \times 10^{30}$  kg, mass of the earth =  $6 \times 10^{24}$  kg. Neglect the effect of other planets etc. (orbital radius =  $1.5 \times 10^{11}$  m).

#### Answer

Mass of the Sun,  $M_s = 2 \times 10^{30}$  kg

Mass of the Earth,  $M_{\rm e}$  = 6 × 10 <sup>24</sup> kg

Orbital radius,  $r = 1.5 \times 10^{11} \text{ m}$ 

Mass of the rocket = m

Let *x* be the distance from the centre of the Earth where the gravitational force acting on satellite P becomes zero.

From Newton's law of gravitation, we can equate gravitational forces acting on satellite P under the influence of the Sun and the Earth as:

$$GmM_{\rm s}/(r-x)^2 = GmM_{\rm e}/x^2$$

$$[(r-x)/x]^2 = M_s/M_e$$

$$(r-x)/x = [2 \times 10^{30}/60 \times 10^{24}]^{1/2} = 577.35$$

$$1.5 \times 10^{11} - x = 577.35x$$

$$578.35x = 1.5 \times 10^{11}$$





$$x = 1.5 \times 10^{11} / 578.35 = 2.59 \times 10^{8} \text{ m}.$$

## 8.13.How will you 'weigh the sun', that is estimate its mass? The mean orbital radius of the earth around the sun is $1.5 \times 10^8$ km.

#### Answer

Orbital radius of the Earth around the Sun,  $r = 1.5 \times 10^{11}$  m

Time taken by the Earth to complete one revolution around the Sun,

$$T = 1 \text{ year} = 365.25 \text{ days}$$

$$= 365.25 \times 24 \times 60 \times 60 \text{ s}$$

Universal gravitational constant,  $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$ 

Thus, mass of the Sun can be calculated using the relation,

$$M = 4\pi^2 r^3 / GT^2$$

= 
$$4 \times 3.14^{2} \times (1.5 \times 10^{11})^{3} / [6.67 \times 10^{-11} \times (365.25 \times 24 \times 60 \times 60)^{2}]$$

$$= 2 \times 10^{30} \text{ kg}$$

Hence, the mass of the Sun is  $2 \times 10^{30}$  kg.

8.14. A Saturn year is 29.5 times the earth year. How far is the Saturn from the sun if the earth is  $1.50 \times 10^8$  km away from the sun?

#### **Answer**







We know that  $T^2 \propto R^3$ 

$$\therefore \frac{T_s^2}{T_e^2} = \frac{R_s^3}{R_e^3}$$

where subscripts s and e refer to the Saturn and Earth respectively.

Now  $\frac{T_s}{T_e} = 29.5 \text{ [given]}; \quad R_e = 1.50 \times 10^8 \text{ km}$   $\left(\frac{R_s}{R_e}\right)^3 = \left(\frac{T_s}{T_e}\right)^2$   $R_s = R_e \times [(29.5)^2]^{1/3} = 1.50 \times 10^8 \times (870.25)^{1/3} \text{ km}$   $= 1.43 \times 10^9 \text{ km} = 1.43 \times 10^{12} \text{ m}$ 

.. Distance of Saturn from Sun = 1.43 × 10<sup>12</sup> m.

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Question 8. 15. A body weighs 63 N on the surface of the Earth. What is the gravitational force on it due to the Earth at a height equal to half the radius of the Earth?

#### **Answer**

Let  $g_h$  be the acceleration due to gravity at a height equal to half the radius of the Earth (h = R/2) and g its value on Earth's surface. Let the body have mass m.





We know that

$$\frac{g_h}{g} = \left(\frac{R}{R+h}\right)^2 \quad \text{or} \quad \frac{g_h}{g} = \left(\frac{R}{R+\frac{R}{2}}\right)^2 = \left(\frac{2}{3}\right)^2 = \frac{4}{9}$$

Let W be the weight of body on the surface of Earth and  $W_h$  the weight of the body at height h.

Then, 
$$\frac{W_h}{W} = \frac{mg_h}{mg} = \frac{g_h}{g} = \frac{4}{9}$$
  
or  $W_h = \frac{4}{9}W = \frac{4}{9} \times 63 N = 28 N$ .

Question 8. 16. Assuming the earth to be a sphere of uniform mass density, how much would a body weigh half way down to the centre of the earth if it weighed 250 N on the surface?

#### **Answer**

As 
$$g_d = g\left(1 - \frac{d}{R}\right) \implies mg_d = mg\left(1 - \frac{d}{R}\right)$$
Here 
$$d = \frac{R}{2}$$

$$\therefore mg_d = (250) \times \left(1 - \frac{R/2}{R}\right) = 250 \times \frac{1}{2} = 125 \text{ N}.$$

Question 8. 17. A rocket is fired vertically with a speed of 5 km s<sup>-1</sup> from the earth's surface. How far from the earth does the rocket go before returning to the earth? Mass of the earth =  $6.0 \times 10^{-24}$  kg; mean radius of the earth =  $6.4 \times 10^6$  m; G =  $6.67 \times 10^{-11}$  N m<sup>2</sup> kg<sup>-2</sup>.





Initial kinetic energy of rocket =  $1/2 \text{ mv}^2 = 1/2 \text{ x m x } (5000)2 = 1.25 \text{ x } 10^7 \text{ mJ}$ 

At distance r from centre of earth, kinetic energy becomes zero

.•. Change in kinetic energy =  $1.25 \times 10^7 - 0 = 1.25 \times 10^7 \text{ m J}$ 

This energy changes into potential energy.

Initial potential energy at the surface of earth =  $GM_em/r$ 

$$= \frac{-(6.67 \times 10^{-11}) \times (6 \times 10^{24}) m}{6.4 \times 10^6} = -6.25 m \times 10^7 \text{ J}$$

Final potential energy at distance,  $r = -\frac{GM_e m}{r}$ 

$$= \frac{-(6.67 \times 10^{-11}) \times (6 \times 10^{24}) m}{r} = -4 \times 10^{14} \frac{m}{r} J$$

 $\therefore$  Change in potential energy = 6.25 × 10<sup>7</sup>  $m - 4 \times 10^{14} \frac{m}{r}$ 

Using law of conservation of energy,

$$6.25 \times 10^7 \ m - \frac{4 \times 10^{14} \ m}{r} = 1.25 \times 10^7 \ m$$
i.e.,
$$r = \frac{4 \times 10^{14}}{5 \times 10^7} \ m = 8 \times 10^{16} \ m.$$

Question 8. 18. The escape speed of a projectile on the Earth's surface is 11.2 km s $^{-1}$ . A body is projected out with thrice this speed. What is the speed of the body far away from the Earth? Ignore the presence of the Sun and other planets.





Let  $v_{\rm es}$  be the escape speed from surface of Earth having a value  $v_{\rm es}$  = 11.2 kg s<sup>-1</sup> = 11.2 × 10<sup>3</sup> m s<sup>-1</sup>. By definition

$$\frac{1}{2}mv_e^2 = \frac{GMm}{R^2} \qquad ...(i)$$

When a body is projected with a speed  $v_i = 3v_{es} = 3 \times 11.2 \times 10^3$  m/s, then it will have a final speed  $v_f$  such that

$$\frac{1}{2}mv_f^2 = \frac{1}{2}mv_i^2 - \frac{GMm}{R^2} = \frac{1}{2}mv_i^2 - \frac{1}{2}mv_e^2$$

$$\Rightarrow v_f = \sqrt{v_i^2 - v_e^2}$$

$$= \sqrt{(3 \times 11.2 \times 10^3) - (11.2 \times 10^3)^2}$$

$$= 11.2 \times 10^3 \times \sqrt{8}$$

$$= 31.7 \times 10^3 \text{ ms}^{-1} \text{ or } 31.7 \text{ km s}^{-1}.$$

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Question 8. 19. A satellite orbits the earth at a height of 400 km above the surface. How much energy must be expended to rocket the satellite out of the earth's gravitational influence? Mass of the satellite = 200 kg; mass of the earth =  $6.0 \times 10^{24}$  kg; radius of the earth =  $6.4 \times 10^6$  m; G =  $6.67 \times 10^{-11}$  N m<sup>2</sup> kg<sup>-2</sup>.

#### **Answer**







Total energy of orbiting satellite at a height h

$$= -\frac{GMm}{(R+h)} + \frac{1}{2}mv^{2} = -\frac{GMm}{(R+h)} + \frac{1}{2}m\frac{GM}{(R+h)}$$
$$= -\frac{GMm}{2(R+h)}$$

Energy expended to rocket the satellite out of the earth's gravitational field

= - (total energy of the orbiting satellite)

$$= \frac{GMm}{2(R+h)} = \frac{\left(6.67 \times 10^{-11}\right) \times \left(6 \times 10^{24}\right) \times 200}{2 \times \left(6.4 \times 10^6 + 4 \times 10^5\right)}$$
$$= 5.9 \times 10^9 \text{ J.}$$

Question 8. 20. Two stars each of one solar mass (=2 x  $10^{30}$  kg) are approaching each other for a head on collision. When they are at a distance  $10^9$  km, their speeds are negligible. What is the speed with which they collide? The radius of each star is  $10^4$  km. Assume the stars to remain undistorted until they collide. (Use the known value of G).

#### **Answer**

Here, mass of each star,  $M = 2 \times 10^{30} \text{ kg}$ 

Initial potential between two stars,  $r = 10^9 \text{ km} = 10^{12} \text{ m}$ .

Initial potential energy of the system = -GMm/r

Total K.E. of the stars =  $1/2Mv^2 + 1/2Mv^2$ 

where v is the speed of stars with which they collide. When the stars are about to collide, the distance between their centres, r' = 2 R.

:. Final potential energy of two stars = -GMm/2R





Since gain in K.E. is at the cost of loss in P.E

$$Mv^{2} = -\frac{GMM}{r} - \left(-\frac{GMM}{2R}\right) = -\frac{GMM}{r} + \frac{GMM}{2R}$$
or
$$2 \times 10^{30} v^{2} = -\frac{6.67 \times 10^{-11} \times \left(2 \times 10^{30}\right)^{2}}{10^{12}} + \frac{6.67 \times 10^{-11} \times \left(2 \times 10^{30}\right)^{2}}{2 \times 10^{7}}$$

$$= -2.668 \times 10^{38} + 1.334 \times 10^{43}$$

$$= 1.334 \times 10^{43} \text{ J}$$

$$v = \sqrt{\frac{1.334 \times 10^{43}}{2 \times 10^{30}}} = 2.583 \times 10^{6} \text{ ms}^{-1}.$$

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Question 8. 21. Two heavy spheres each of mass 100 kg and radius 0.10 mare placed 1.0 m apart on ahorizontal table. What is the gravitational field and potential at the mid point of the line joining the centres of the spheres? Is an object placed at that point in equilibrium? If so, is the equilibrium stable or unstable?

#### Answer

Here  $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$ ; M = 100 kg; R = 0.1 m, distance between the two spheres, d = 1.0 m

Suppose that the distance of either sphere from the mid-point of the line joining their centre is r. Then r=d/2=0.5 m. The gravitational field at the mid-point due to two spheres will be equal and opposite.





Hence, the resultant gravitational field at the mid point = 0

The gravitational potential at the mid point =  $\left(-\frac{GM}{r}\right) \times 2$ 

$$= -\frac{6.67 \times 10^{-11} \times 100 \times 2}{0.5} = -2.668 \times 10^{-8} \text{ J kg}^{-1}.$$

The object placed at that point would be in stable equilibrium.

Question 8. 22. As you have learnt in the text, a geostationary satellite orbits the Earth at a height of nearly 36,000 km from the surface of the Earth. What is the potential due to Earth's gravity at the site of this satellite? (Take the potential energy at infinity to be zero). Mass of the Earth =  $6.0 \times 10^{24}$  kg, radius = 6400 km.

#### **Answer**

Distance of satellite from the centre of earth = R = r + x

$$= 6400 + 36000 = 42400 \text{ km} = 4.24 \text{ x } 10^7 \text{ m}$$

Using potential, 
$$V = -\frac{GM}{R}$$
, we get 
$$V = -\frac{\left(6.67 \times 10^{-11}\right) \times \left(6 \times 10^{24}\right)}{\left(4.24 \times 10^{7}\right)} = -9.44 \times 10^{6} \text{ J kg}^{-1}$$

Question 8. 23. A star 2.5 times the mass of the sun and collapsed to a size of 12 km rotates with a speed of 1.2 rev. per second. (Extremely compact stars of this kind are known as neutron stars. Certain stellar objects called pulsars belong to this category). Will an object placed on its equator remain stuck to its surface due to gravity? (mass of the sun =  $2 \times 10^{30}$  kg).





Acceleration due to gravity of the star, g= GM/R<sup>2</sup>.....(i)

Here M is the mass and R is the radius of the star.

The outward centrifugal force acting on a body of mass m at the equator of the star  $=mv_2/R = mR w_2$ ——-(ii)

From equation (i), the acceleration due to the gravity of the star

$$= \frac{6.67 \times 10^{-11} \times 2.5 \times 2 \times 10^{30}}{\left(12 \times 10^{3}\right)^{2}} = 2.316 \times 10^{12} \text{ m/s}^{2}$$

:. Inward force due to gravity on a body of mass m

$$= m \times 2.316 \times 10^{12} \text{ N}$$

From equation (ii), the outward centrifugal force =  $mR\omega^2$ 

= 
$$m \times (12 \times 10^3) \times \left(\frac{2\pi \times 1.5}{-1}\right)^2$$
  
=  $m \times 1.06 \times 10^6 \text{ N}$ 

Since the inward force due to gravity on a body at the equator of the star is about 2.2 million times more than the outward centrifugal force, the body will remain stuck to the surface of the star.

Question 8. 24. A spaceship is stationed on Mars. How much energy must be expended on the spaceship to rocket it out of the solar system? Mass of the spaceship = 1000 kg, Mass of the Sun =  $2 \times 10^{30}$  kg. Mass of the Mars =  $6.4 \times 10^{23}$  kg, Radius of Mars = 3395 km. Radius of the orbit of Mars =  $2.28 \times 10^{11}$  m, G =  $6.67 \times 10^{-11}$  N m<sup>2</sup> kg<sup>-2</sup>.





Let R be the radius of orbit of Mars and R' be the radius of the Mars. M be the mass of the Sun and M' be the mass of Mars. If m is the mass of the space-ship, then Potential energy of space-ship due to gravitational attraction of the Sun = - GM m/R Potential energy of space-ship due to gravitational attraction of Mars = - G M' m/R' Since the K.E. of space ship is zero, therefore,

total energy of spaceship = 
$$-\frac{GM m}{R} - \frac{GM' m}{R'} = -G m \left( \frac{M}{R} + \frac{M'}{R'} \right)$$

∴ Energy required to rocket out the spaceship from the solar system = – (total energy of spaceship)

$$= -\left[-G m \left(\frac{M}{R} + \frac{M'}{R'}\right)\right] = G m \left[\frac{M}{R} + \frac{M'}{R'}\right]$$

$$= 6.67 \times 10^{-11} \times 1000 \times \left[\frac{2 \times 10^{30}}{2.28 \times 10^{11}} + \frac{6.4 \times 10^{23}}{3395 \times 10^{3}}\right]$$

$$= 6.67 \times 10^{-8} \left[\frac{20}{2.28} + \frac{6.4}{33.95}\right] \times 10^{18} \text{ J} = 5.98 \times 10^{11} \text{ J}.$$

Question 8. 25. A rocket is fired 'vertically' from the surface of Mars with a speed of 2 km s-1. If 20% of its initial energy is lost due to Martian atmospheric resistance, how far will the rocket go from the surface of mars before returning to it? Mass of Mars =  $6.4 \times 10^{23}$  kg; radius of Mars = 3395 km; G =  $6.67 \times 10^{-11}$  N m<sup>2</sup> kg<sup>-2</sup>

**Answer** 





Initial K.E. = 
$$\frac{1}{2} mv^2$$
; Initial P.E. =  $-\frac{GMm}{R}$ 

where m = Mass of rocket, M = Mass of Mars, R = Radius of Mars

$$\therefore$$
 Total initial energy =  $\frac{1}{2}mv^2 - \frac{GMm}{R}$ 

Since 20% of K.E. is lost, only 80% remains to reach the height.

.. Total initial energy available

$$= \frac{4}{5} \times \frac{1}{2} mv^2 - \frac{GMm}{R}$$
$$= 0.4 mv^2 - \frac{GMm}{R}$$

When the rocket reaches the highest point, at a height h above the surface, its K.E. is zero and P.E. =  $-\frac{GMm}{R+h}$ .

Using principle of conservation of energy.

$$0.4 \text{ mv}^2 - \frac{GMm}{R} = -\frac{GMm}{R+h}$$
or
$$\frac{GMm}{R+h} = \frac{GMm}{R} - 0.4 mv^2 \implies \frac{GM}{R+h} = \frac{GM}{R} - 0.4 v^2$$
or
$$\frac{GM}{R+h} = \frac{1}{R} [GM - 0.4 Rv^2] \implies \frac{R+h}{R} = \frac{GM}{GM - 0.4 Rv^2}$$
or
$$\frac{h}{R} = \frac{GM}{GM - 0.4 Rv^2} - 1$$
or
$$\frac{h}{R} = \frac{0.4 Rv^2}{GM - 0.4 Rv^2} \implies h = \frac{0.4 R^2 v^2}{GM - 0.4 Rv^2}$$
or
$$h = \frac{0.4 \times (2 \times 10^3)^2 \times (3.395 \times 10^6)^2}{6.67 \times 10^{-11} \times 6.4 \times 10^{23} - 0.4 \times (2 \times 10^3)^2 \times 3.395 \times 10^6} = 495 \text{ km}.$$









# **Chapterwise NCERT Solutions for Class 11 Physics:**

- Chapter 1-Physical World
- Chapter 2-Units and Measurements
- Chapter 3-Motion In A Straight Line
- Chapter 4-Motion In A Plane
- Chapter 5-Laws Of Motion
- Chapter 6-Work, Energy And Power
- Chapter 7-System Of Particles And Rotational Motion
- Chapter 8-Gravitation
- <u>Chapter 9-Mechanical properties of Solids</u>
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