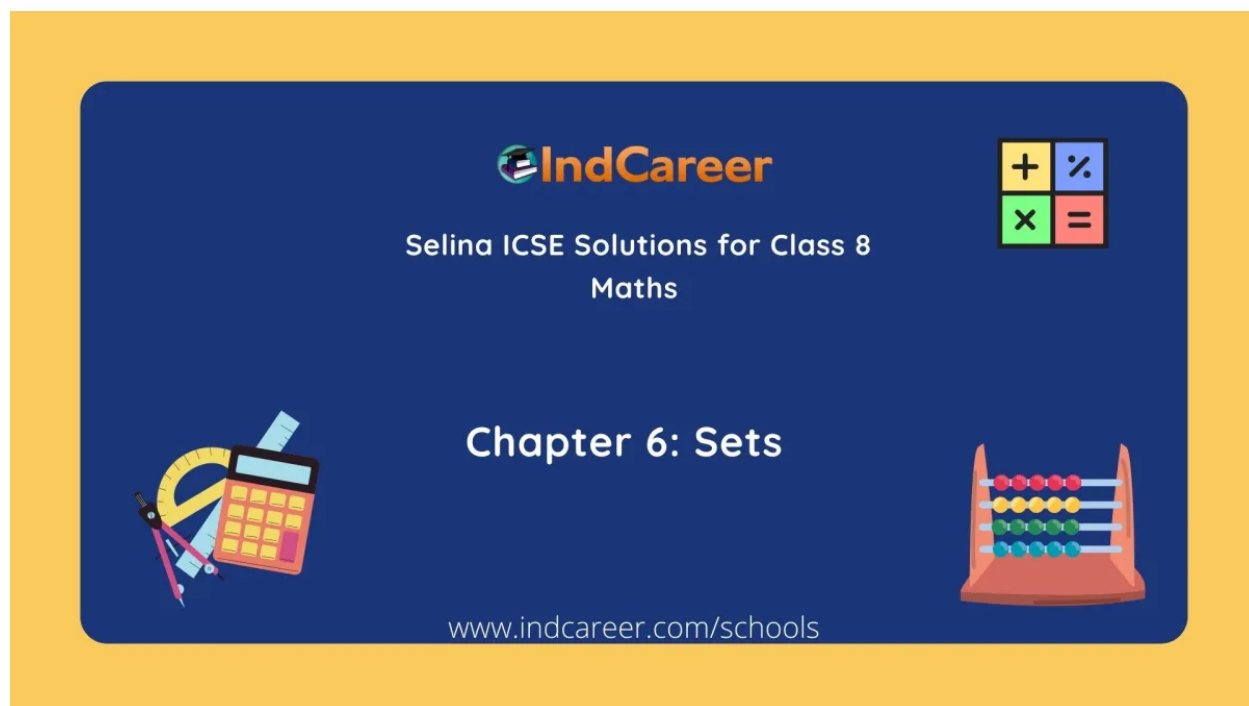


Selina Class 8 ICSE Solutions Mathematics :

Chapter 6- Sets



For any clarifications or questions you can write to **info@indcareer.com**

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Selina Class 8 ICSE Solutions Mathematics :

Chapter 6- Sets

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Selina Class 8 ICSE Solutions Mathematics : Chapter 6- Sets

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Exercise 6A

Question 1.

Write the following sets in roster (Tabular) form :

(i) $A_1 = \{x : 2x + 3 = 11\}$

(ii) $A_2 = \{x : x^2 - 4x - 5 = 0\}$

(iii) $A_3 = \{x : x \in \mathbb{Z}, -3 \leq x < 4\}$

(iv) $A_4 = \{x : x \text{ is a two digit number and sum of digits of } x \text{ is } 7\}$

(v) $A_5 = \{x : x = 4n, n \in \mathbb{W} \text{ and } n < 4\}$

(vi) $A_6 = \{x : x = nn+2; n \in \mathbb{N} \text{ and } n > 5\}$

Solution:

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- (i) $A_1 = \{x : 2x + 3 = 11\}$
 $\therefore 2x + 3 = 11$
 $\Rightarrow 2x = 11 - 3$
 $\Rightarrow 2x = 8$
 $\Rightarrow x = \frac{8}{2} \Rightarrow x = 4$
 $\therefore$ Given set in roster (Tabular) form is
 $A_1 = \{4\}$
- (ii) $A_2 = \{x : x^2 - 4x - 5 = 0\}$
 $\therefore x^2 - 4x - 5 = 0$
 $\Rightarrow x^2 - 5x + x - 5 = 0$
 $\Rightarrow x(x - 5) + 1(x - 5) = 0$
 $\Rightarrow (x - 5)(x + 1) = 0$
 $\therefore$ Either $x - 5 = 0$ or $x + 1 = 0$
 $\Rightarrow x = 5 \quad \Rightarrow x = -1$
 $\therefore$ Given set in roster (Tabular) form is
 $A_2 = \{5, -1\}$
- (iii) $A_3 = \{x : x \in \mathbb{Z}, -3 \leq x < 4\}$
 $\therefore -3 \leq x < 4$
 $\therefore x = -3, -2, -1, 0, 1, 2, 3$
 $\therefore$ Given set in roster (Tabular) form is
 $A_3 = \{-3, -2, -1, 0, 1, 2, 3\}$

(iv) $A_4 = \{x : x \text{ is a two digit number and}$

sum of digits of x is 7}

$\therefore x$ is a two digit number and sum of digits of x is 7

$\therefore x = 16, 25, 34, 43, 52, 61, 70$

$\therefore$ Given set in roster (Tabular) form is

$$A_4 = \{16, 25, 34, 43, 52, 61, 70\}$$

(v) $A_5 = \{x : x = 4n, n \in W \text{ and } n < 4\}$

$\therefore x = 4n$

$\therefore$ When $n = 0$, $x = 4 \times 0$

$\Rightarrow x = 0$

When $n = 1$, $x = 4 \times 1$

$\Rightarrow x = 4$

When $n = 2$, $x = 4 \times 2$

$\Rightarrow x = 8$

When $n = 3$, $x = 4 \times 3$

$\Rightarrow x = 12$

$\therefore$ Given set in roster (Tabular) form is

$$A_5 = \{0, 4, 8, 12\}$$

$$(vi) \quad A_6 = \left\{ x : x = \frac{n}{n+2}; n \in \mathbb{N} \text{ \& } n > 5 \right\}$$

$$\therefore x = \frac{n}{n+2}$$

$$\therefore \text{When } n = 6, \quad x = \frac{6}{6+2}$$

$$\Rightarrow x = \frac{6}{8} \Rightarrow x = \frac{3}{4}$$

$$\text{When } n = 7, \quad x = \frac{7}{7+2} \Rightarrow x = \frac{7}{9}$$

$$\text{When } n = 8, \quad x = \frac{8}{8+2} \Rightarrow x = \frac{8}{10}$$

$$\Rightarrow x = \frac{4}{5}$$

$$\text{When } n = 9, \quad x = \frac{9}{9+2} \Rightarrow x = \frac{9}{11}$$

$\therefore$ Given set in roster (Tabular) form is

$$A_6 = \left\{ \frac{3}{4}, \frac{7}{9}, \frac{4}{5}, \frac{9}{11}, \dots \right\}$$

Question 2.

Write the following sets in set-builder (Rule Method) form :

- (i) $B_1 = \{6, 9, 12, 15, \dots\}$
(ii) $B_2 = \{11, 13, 17, 19\}$
(iii) $B_3 = \left\{\frac{1}{3}, \frac{3}{5}, \frac{5}{7}, \frac{7}{9}, \frac{9}{11}, \dots\right\}$
(iv) $B_4 = \{8, 27, 64, 125, 216\}$
(v) $B_5 = \{-5, -4, -3, -2, -1\}$
(vi) $B_6 = \{\dots, -6, -3, 0, 3, 6, \dots\}$

Solution:

- (i) $B_1 = \{6, 9, 12, 15, \dots\}$
 $= \{x : x = 3n + 3; n \in \mathbb{N}\}$
(ii) $B_2 = \{11, 13, 17, 19\}$
 $= \{x : x \text{ is a prime number between } 10 \text{ and } 20\}$
(iii) $B_3 = \left\{\frac{1}{3}, \frac{3}{5}, \frac{5}{7}, \frac{7}{9}, \frac{9}{11}, \dots\right\}$
 $= \{x : x = \frac{n}{n+2}, \text{ where } n \text{ is an odd natural number}\}$
(iv) $B_4 = \{8, 27, 64, 125, 216\}$
 $= \{x : x = n^3; n \in \mathbb{N} \text{ and } 2 \leq n \leq 6\}$
(v) $B_5 = \{-5, -4, -3, -2, -1\}$
 $= \{x : x \in \mathbb{Z}, -5 \leq x \leq -1\}$
(vi) $B_6 = \{\dots, -6, -3, 0, 3, 6, \dots\}$
 $= \{x : x = 3n, n \in \mathbb{Z}\}$

Question 3.

- (i) Is $\{1, 2, 4, 16, 64\} = \{x : x \text{ is a factor of } 32\}$? Give reason.

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(ii) Is $\{x : x \text{ is a factor of } 27\} \neq \{3, 9, 27, 54\}$? Give reason.

(iii) Write the set of even factors of 124.

(iv) Write the set of odd factors of 72.

(v) Write the set of prime factors of 3234.

(vi) Is $\{x : x^2 - 7x + 12 = 0\} = \{3, 4\}$?

(vii) Is $\{x : x^2 - 5x - 6 = 0\} = \{2, 3\}$?

Solution:

(i) No, $\{1, 2, 4, 16, 64\} \neq \{x : x \text{ is factor of } 32\}$

Because 64 is not a factor of 32

(ii) Yes, $\{x : x \text{ is a factor of } 27\} = \{3, 9, 27, 54\}$

Because 54 is not a factor of 27

(iii) $1 \times 124 = 124$

$2 \times 62 = 124$

$4 \times 31 = 124$

Factors of 124 = 1, 2, 4, 31, 62, 124

Set of even factors of 124 = $\{2, 4, 62, 124\}$

(iv) $1 \times 72 = 72$

$2 \times 36 = 72$

$3 \times 24 = 72$

$4 \times 18 = 72$

$6 \times 12 = 72$

$8 \times 9 = 72$

Factors of 72 = 1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

Set of odd factors of 72 = $\{1, 3, 9\}$

$$\begin{array}{r|l}
 2 & 3234 \\
 \hline
 3 & 1617 \\
 \hline
 7 & 539 \\
 \hline
 7 & 77 \\
 \hline
 & 11
 \end{array}$$

$$3234 = 2 \times 3 \times 7 \times 7 \times 11$$

$\therefore$ Set of prime factors of 3234 = {2, 3, 7, 11}

$$(vi) \quad x^2 - 7x + 12 = 0$$

$$\Rightarrow x^2 - 4x - 3x + 12 = 0$$

$$\Rightarrow x(x - 4) - 3(x - 4) = 0$$

$$\Rightarrow (x - 4)(x - 3) = 0$$

$$\therefore \text{ Either } x - 4 = 0 \quad \text{Or } x - 3 = 0$$

$$\Rightarrow x = 4 \quad \Rightarrow x = 3$$

$$\therefore \{x : x^2 - 7x + 12 = 0\} = \{3, 4\} \text{ is true}$$

$$(vii) \quad x^2 - 5x - 6 = 0$$

$$\Rightarrow x^2 - 6x + x - 6 = 0$$

$$\Rightarrow x(x - 6) + 1(x - 6) = 0$$

$$\Rightarrow (x - 6)(x + 1) = 0$$

$$\therefore \text{ Either } x - 6 = 0 \quad \text{Or } x + 1 = 0$$

$$i.e., \quad x = 6 \quad i.e., \quad x = -1$$

$$\therefore \{x : x^2 - 5x - 6 = 0\} \neq \{2, 3\}$$

In other words $\{x : x^2 - 5x - 6 = 0\} = \{2, 3\}$
is not true

Question 4.

Write the following sets in Roster form :

(i) The set of letters in the word 'MEERUT'.

(ii) The set of letters in the word 'UNIVERSAL'.

(iii) $A = \{x : x = y + 3, y \in \mathbb{N} \text{ and } y > 3\}$

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(iv) $B = \{p : p \in W \text{ and } p^2 < 20\}$

(v) $C = \{x : x \text{ is composite number and } 5 < x < 21\}$

Solution:

(i) Roster form of the set of letters in the word "MEERUT" = $\{m, e, r, u, t\}$

(ii) Roster form of the set of letters in the word "UNIVERSAL" = $\{u, n, i, v, e, r, s, a, l\}$

(iii) $A = \{x : x = y + 3, y \in N \text{ and } y > 3\}$

$$x = y + 3$$

$$\text{When } y = 4, \quad x = 4 + 3 = 7$$

$$\text{When } y = 5, \quad x = 5 + 3 = 8$$

$$\text{When } y = 6, \quad x = 6 + 3 = 9$$

$$\text{When } y = 7, \quad x = 7 + 3 = 10$$

$$\text{When } y = 8, \quad x = 8 + 3 = 11$$

.....

.....

.....

.....

$\therefore$ Roster form of the given set $A = \{7, 8, 9, 10, 11, \dots\}$

(iv) $B = \{P : P \in W \text{ and } P^2 < 20\}$

When $P^2 = 0$

$$P = \sqrt{0} = 0$$

When $P^2 = 1$

$$P = \sqrt{1} = 1$$

When $P^2 = 4$

$$P = \sqrt{4} = 2$$

When $P^2 = 9$

$$P = \sqrt{9} = 3$$

When $P^2 = 16$

$$P = \sqrt{16} = 4$$

$\therefore$ Roster form of the given set $B = \{0, 1, 2, 3, 4\}$

(v) $C = \{x : x \text{ is composite number and } 5 \leq x \leq 21\}$

$5 \leq x \leq 21$ means $x = 5, 6, 7, 8, 9, 10, \dots, 21$

But we are given that x is a composite number

$\therefore x = 6, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21$

$\therefore$ Roster form of the given set $C = \{6, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21\}$

Note : Composite numbers : The natural numbers (greater than 1), which are not prime, are called composite numbers.

Question 5.

List the elements of the following sets :

(i) $\{x : x^2 - 2x - 3 = 0\}$

(ii) $\{x : x = 2y + 5; y \in \mathbb{N} \text{ and } 2 \leq y < 6\}$

(iii) $\{x : x \text{ is a factor of } 24\}$

(iv) $\{x : x \in \mathbb{Z} \text{ and } x^2 \leq 4\}$

(v) $\{x : 3x - 2 \leq 10, x \in \mathbb{N}\}$

(vi) $\{x : 4 - 2x > -6, x \in \mathbb{Z}\}$

Solution:

$$(i) \{x : x^2 - 2x - 3 = 0\}$$

$$x^2 - 2x - 3 = 0$$

$$\Rightarrow x^2 - 3x + x - 3 = 0$$

$$\Rightarrow x(x-3) + 1(x-3) = 0$$

$$\Rightarrow (x+1)(x-3) = 0$$

$$\therefore \text{Either } x - 3 = 0 \quad \text{Or } x + 1 = 0$$

$$\therefore x = 3 \quad \text{Or } x = -1$$

$\therefore$ Elements of the set $\{x : x^2 - 2x - 3 = 0\}$ are 3 and -1

$$(ii) \{x : x = 2y + 5; y \in \mathbb{N} \text{ and } 2 \leq y < 6\}$$

$$x = 2y + 5$$

$$\text{When } y = 2, \quad x = 2 \times 2 + 5$$

$$= 4 + 5 = 9$$

$$\text{When } y = 3, \quad x = 2 \times 3 + 5$$

$$= 6 + 5 = 11$$

$$\text{When } y = 4, \quad x = 2 \times 4 + 5$$

$$= 8 + 5 = 13$$

$$\text{When } y = 5, \quad x = 2 \times 5 + 5$$

$$= 10 + 5 = 15$$

$\therefore$ Elements of the given set $\{x : x = 2y + 5; y \in \mathbb{N} \text{ and } 2 \leq y < 6\}$ are 9, 11, 13, 15

(iii) $\{x : x \text{ is a factor of } 24\}$

$$24 = 1 \times 24$$

$$24 = 2 \times 12$$

$$24 = 3 \times 8$$

$$24 = 4 \times 6$$

$\therefore$ Elements of the given set $\{x : x \text{ is a factor of } 24\}$ are 1, 2, 3, 4, 6, 8, 12, 24

(iv) $\{x : x \in \mathbb{Z} \text{ and } x^2 \leq 4\}$

When $x^2 = 4$

$$x = \pm \sqrt{4} = \pm 2$$

When $x^2 = 1$

$$x = \pm \sqrt{1} = \pm 1$$

When $x^2 = 0$

$$x = \sqrt{0} = 0$$

$\therefore$ Elements of the given set $\{x : x \in \mathbb{Z} \text{ and } x^2 \leq 4\}$ are +2, -2, +1, -1, 0 or are -2, -1, 0, 1, 2

(v) $\{x : 3x-2 \leq 10, x \in \mathbb{N}\}$

$$3x-2 \leq 10$$

$$\Rightarrow 3x \leq 10+2$$

$$\Rightarrow 3x \leq 12$$

$$\Rightarrow x \leq \frac{12}{3}$$

$$\leq x \leq 4$$

$\therefore$ Elements of the given set $\{x : 3x-2 \leq 10, x \in \mathbb{N}\}$ are 1,2,3 and 4

(vi) $\{x : 4-2x > -6, x \in \mathbb{Z}\}$

$$4-2x > -6$$

$$-4+4-2x > -6-4$$

(Subtracting 4 from both sides)

$$-2x > -10$$

$$-2x+2x+10 > -10+2x+10$$

[Adding $2x+10$ to both sides]

$$+10 > 2x$$

$$\frac{10}{2} > x$$

$$5 > x$$

$\therefore$ Elements of the given set $\{x : 4-2x > -6, x \in \mathbb{Z}\}$ are 4,3,2,1,0,-1.....

Exercise 6B

Question 1.

Find the cardinal number of the following sets :

(i) $A_1 = \{-2, -1, 1, 3, 5\}$

(ii) $A_2 = \{x : x \in \mathbb{N} \text{ and } 3 \leq x < 7\}$

(iii) $A_3 = \{p : p \in \mathbb{W} \text{ and } 2p - 3 < 8\}$

(iv) $A_4 = \{b : b \in \mathbb{Z} \text{ and } -7 < 3b - 1 \leq 2\}$

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Cardinal Number of a set; The number of elements in a set is called is Cardinal Number.

Solution:

$$\begin{aligned} (i) \quad A_1 &= \{-2, -1, 1, 3, 5\} \\ \text{Cardinal number of set } A_1 &= 5 \\ (ii) \quad A_2 &= \{x : x \in \mathbb{N} \text{ and } 3 \leq x < 7\} \\ &= \{3, 4, 5, 6\} \\ \therefore \text{Cardinal number of set } A_2 &= 4 \\ (iii) \quad A_3 &= \{P : P \in \mathbb{W} \text{ and } 2P - 3 < 8\} \\ &\quad 2P - 3 < 8 \\ \Rightarrow 2P - 3 + 3 &< 8 + 3 \\ &\quad \text{(Adding 3 to both sides)} \\ \Rightarrow 2P &< 11 \\ \Rightarrow P &< \frac{11}{2} \\ &\quad \text{(Dividing both sides by 2)} \\ \Rightarrow P &< 5.5 \\ \therefore A_3 &= \{0, 1, 2, 3, 4, 5\} \\ \therefore \text{Cardinal number of set } A_3 &= 6 \\ (iv) \quad A_4 &= \{b : b \in \mathbb{Z} \text{ and } -7 < 3b - 1 \leq 2\} \\ &\quad -7 < 3b - 1 \\ \Rightarrow -7 + 1 &< 3b - 1 + 1 \\ &\quad \text{(Adding 1 to both sides)} \\ \Rightarrow -6 &< 3b \\ \Rightarrow -\frac{6}{3} &< b \end{aligned}$$

$$\Rightarrow \quad \text{(Dividing both sides by 3)} \\ -2 < b$$

$$\text{Again } 3b-1 \leq 2$$

$$\Rightarrow \quad 3b-1+1 \leq 2+1$$

(Adding 1 to both sides)

$$\Rightarrow \quad 3b \leq 3$$

$$\Rightarrow \quad b \leq \frac{3}{3}$$

(Dividing both sides by 3)

$$\Rightarrow \quad b \leq 1$$

$$\therefore \quad -2 < b \leq 1$$

$$\therefore \quad \text{Given set } A_4 = \{-1, 0, 1\}$$

$$\therefore \quad \text{Cardinal number of set } A_4 = 3$$

Question 2.

If $P = \{P : P \text{ is a letter in the word "PERMANENT"}\}$. Find $n(P)$.

Solution:

$$P = \{P : P \text{ is a letter in the word "PERMANENT"}\}$$

$$\text{or } P = \{p, e, r, m, a, n, t\}$$

$$n(P) = 7$$

Question 3.

State, which of the following sets are finite and which are infinite :

- (i) $A = \{x : x \in \mathbb{Z} \text{ and } x < 10\}$
(ii) $B = \{x : x \in \mathbb{W} \text{ and } 5x-3 \leq 20\}$
(iii) $P = \{y : y = 3x-2, x \in \mathbb{N} \text{ \& } x > 5\}$
(iv) $M = \{r : r = \frac{3}{n}; n \in \mathbb{W} \text{ and } 6 < n \leq 15\}$

Note : (i) A set with finite (limited) number of elements in it, is called a finite set, (ii) A set which is not finite is called an infinite set.

Solution:

- (i) $A = \{x : x \in \mathbb{Z} \text{ and } x < 10\}$
 $= \{\dots, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$
 $= \{9, 8, 7, 6, 5, 4, 3, 2, 1, 0, -1, -2, -3, -4, \dots\}$
 $\therefore$ It is an infinite set.
- (ii) $B = \{x : x \in \mathbb{W} \text{ and } 5x-3 \leq 20\}$
 $5x - 3 \leq 20$
 $\Rightarrow 5x-3+3 \leq 20+3$
 $\hspace{10em} \text{(Adding 3 to both sides)}$
 $\Rightarrow 5x \leq 20+3$
 $\Rightarrow 5x \leq 23$
 $\Rightarrow x \leq \frac{23}{5}$
 $\hspace{10em} \text{(Dividing both sides by 5)}$
 $\Rightarrow x \leq 4.6$
 $\therefore B = \{0, 1, 2, 3, 4\}$
 $\therefore$ It is a finite set.

$$(iii) \quad P = \{y : y = 3x - 2, x \in \mathbb{N} \text{ and } x > 5\}$$
$$y = 3x - 2$$

$$\text{When } x = 6, \quad y = 3 \times 6 - 2$$
$$= 18 - 2 = 16$$

$$\text{When } x = 7, \quad y = 3 \times 7 - 2$$
$$= 21 - 2 = 19$$

$$\text{When } x = 8, \quad y = 3 \times 8 - 2$$
$$= 24 - 2 = 22$$

$$\text{When } x = 9, \quad y = 3 \times 9 - 2$$
$$= 27 - 2 = 25$$

$$\therefore P = \{16, 19, 22, 25, \dots\}$$

$\therefore$ It is an infinite set.

$$(iv) \quad M = \left\{r : r = \frac{3}{n}; n \in \mathbb{W} \text{ and } 6 < n \leq 15\right\}$$

$$r = \frac{3}{n}$$

$$\text{When } n = 7, \quad r = \frac{3}{7}$$

$$\text{When } n = 8, \quad r = \frac{3}{8}$$

$$\text{When } n = 9, \quad r = \frac{3}{9}$$

$$\text{When } n = 10, \quad r = \frac{3}{10}$$

$$\text{When } n = 11, \quad r = \frac{3}{11}$$

$$\text{When } n = 12, \quad r = \frac{3}{12}$$

$$\text{When } n = 13, \quad r = \frac{3}{13}$$

$$\text{When } n = 14, \quad r = \frac{3}{14}$$

$$\text{When } n = 15, \quad r = \frac{3}{15}$$

$$\therefore M = \left\{ \frac{3}{7}, \frac{3}{8}, \frac{3}{9}, \frac{3}{10}, \frac{3}{11}, \frac{3}{12}, \frac{3}{13}, \frac{3}{14}, \frac{3}{15} \right\}$$

$\therefore$ It is a finite set.

Question 4.

Find, which of the following sets are singleton sets :

(i) The set of points of intersection of two non-parallel st. lines in the same plane

(ii) $A = \{x : 7x - 3 = 11\}$

(iii) $B = \{y : 2y + 1 < 3 \text{ and } y \in W\}$

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Note : A set, which has only one element in it, is called a SINGLETON or unit set.

Solution:

(i) The set of points of intersection of two non-parallel st. lines in the same plane.....singleton set.

(ii) $A = \{x : 7x - 3 = 11\}$

$$7x - 3 = 11$$

$$\Rightarrow 7x = 11 + 3$$

$$\Rightarrow 7x = 14$$

$$\Rightarrow x = \frac{14}{7} = 2$$

$$\therefore A = \{2\}$$

Hence given set A is a singleton set.

(iii) $B = \{y : 2y + 1 < 3 \text{ and } y \in W\}$

$$2y + 1 < 3$$

$$\Rightarrow 2y + 1 - 1 < 3 - 1$$

(Subtracting 1 from both sides)

$$\Rightarrow 2y < 2$$

$$\Rightarrow y < \frac{2}{2}$$

(Dividing both sides by 2)

$$\Rightarrow y < 1$$

$$\therefore B = \{0\}$$

Hence it is a singleton set.

Question 5.

Find, which of the following sets are empty :

(i) The set of points of intersection of two parallel lines.

(ii) $A = \{x : x \in N \text{ and } 5 < x < 6\}$

(iii) $B = \{x : x^2 + 4 = 0, x \in N\}$

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(iv) $C = \{\text{even numbers between 6 \& 10}\}$

(v) $D = \{\text{prime numbers between 7 \& 11}\}$

Note : The set, which has no element in it, is called the empty or null set.

Solution:

(i) “The set of points of intersection of two parallel lines” is **an empty set** because two parallel lines do not intersect anywhere.

(ii) $A = \{x : x \in \mathbb{N} \text{ and } 5 < x \leq 6\}$

As $5 < x \leq 6$

$$\therefore x = 6$$

$$\therefore A = \{6\}$$

Hence given set A is not an empty set.

(iii) $B = \{x : x^2 + 4 = 0, x \in \mathbb{N}\}$

$$x^2 + 4 = 0$$

$$\Rightarrow x^2 = -4$$

$$\Rightarrow x = \sqrt{-4} \text{ which is not a natural number.}$$

But $x \in \mathbb{N}$

$$\therefore B = \{ \}$$

$\therefore$ Given set B is an empty set.

(iv) $C = \{\text{Even numbers between 6 and 10}\}$

$$\therefore C = \{8\}$$

Hence it is not an empty set.

(v) $D = \{\text{Prime numbers between 7 and 11}\}$

Because there is no prime number between 7 and 11.

$$\therefore D = \{ \}$$

Hence it is an empty set.

Question 6.

(i) Are the sets $A = \{4, 5, 6\}$ and $B = \{x : x^2 - 5x - 6 = 0\}$ disjoint ?

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(ii) Are the sets $A = \{b, c, d, e\}$ and $B = \{x : x \text{ is a letter in the word 'MASTER'}\}$ joint ?

Note :

(i) Two sets are said to be joint sets, if they have atleast one element in common.

(ii) Two sets are said to be disjoint, if they have no element in common.

Solution:

$$\begin{aligned}(i) \quad A &= \{4, 5, 6\} \\ B &= \{x : x^2 - 5x - 6 = 0\} \\ x^2 - 5x - 6 &= 0 \\ \Rightarrow x^2 - 6x + x - 6 &= 0 \\ \Rightarrow x(x-6) + 1(x-6) &= 0 \\ \Rightarrow (x-6)(x+1) &= 0 \\ \therefore \text{Either } x-6 &= 0 & \text{Or } x+1 &= 0 \\ \Rightarrow x &= 6 & \Rightarrow x &= -1 \\ \therefore B &= \{6, -1\}\end{aligned}$$

Hence set A and set B are not disjoint because these sets have element 6 in common.

$$\begin{aligned}(ii) \quad A &= \{b, c, d, e\} \\ B &= \{x : x \text{ is a letter in the word "MASTER"}\} \\ \therefore B &= \{m, a, s, t, e, r\}\end{aligned}$$

Hence set A and set B are joint because these sets have element e in common.

Question 7.

State, whether the following pairs of sets are equivalent or not :

(i) $A = \{x : x \in \mathbb{N} \text{ and } 11 \geq 2x - 1\}$ and $B = \{y : y \in \mathbb{W} \text{ and } 3 \leq y \leq 9\}$

(ii) Set of integers and set of natural numbers.

(iii) Set of whole numbers and set of multiples of 3.

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(iv) $P = \{5, 6, 7, 8\}$ and $M = \{x : x \in W \text{ and } x < 4\}$

Note : Two sets are said to be equivalent, if they contain the same number of elements.

Solution:

$$(i) A = \{x : x \in N \text{ and } 11 \geq 2x - 1\}$$

$$11 \geq 2x - 1$$

$$\Rightarrow 11 + 1 \geq 2x - 1 + 1$$

$$\Rightarrow 12 \geq 2x$$

$$\Rightarrow \frac{12}{2} \geq x$$

$$\Rightarrow 6 \geq x$$

$$\therefore A = \{1, 2, 3, 4, 5, 6\}$$

$$\therefore n(A) = 6$$

$$B = \{y : y \in W \text{ and } 3 \leq y \leq 9\}$$

$$\therefore 3 \leq y \leq 9$$

$$B = \{3, 4, 5, 6, 7, 8, 9\}$$

$$n(B) = 7$$

Cardinal number of set A = 6 and cardinal number of set B = 7

Set A and set B are not equivalent.

(ii) Set of integers has infinite number of elements.

Set of natural numbers has infinite number of elements.

Set of integers and set of natural numbers are equivalent because both these sets have infinite number of elements.

(iii) Set of whole numbers, has infinite number of elements.

Set of multiples of 3, has infinite number of element.

Set of whole numbers and set of multiples of 3 are equivalent because both these sets have infinite number of elements.

(iv) $P = \{5, 6, 7, 8\}$

$n(P) = 4$

$M = \{x : x \in W \text{ and } x \leq 4\}$

$M = \{0, 1, 2, 3, 4\}$

$n(M) = 5$

Now Cardinal number of set $P = 4$ and

Cardinal number of set $M = 5$

These sets are not equivalent.

Question 8.

State, whether the following pairs of sets are equal or not :

(i) $A = \{2, 4, 6, 8\}$ and

$B = \{2n : n \in N \text{ and } n < 5\}$

(ii) $M = \{x : x \in W \text{ and } x + 3 < 8\}$ and

$N = \{y : y = 2n - 1, n \in N \text{ and } n < 5\}$

(iii) $E = \{x : x^2 + 8x - 9 = 0\}$ and

$F = \{1, -9\}$

(iv) $A = \{x : x \in n, x < 3\}$ and

$B = \{y : y^2 - 3y + 2 = 0\}$

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Note: Two sets are equal, if both the sets have same (identical) elements.

Solution:

$$(i) \quad A = \{2, 4, 6, 8\}$$

$$B = \{2n : n \in \mathbb{N} \text{ and } n < 5\}$$

$$\text{When } n = 1, 2n = 2 \times 1 = 2$$

$$\text{When } n = 2, 2n = 2 \times 2 = 4$$

$$\text{When } n = 3, 2n = 2 \times 3 = 6$$

$$\text{When } n = 4, 2n = 2 \times 4 = 8$$

$$\therefore B = \{2, 4, 6, 8\}$$

Now we see that elements of sets A and B are the same (identical)

$\therefore$ Sets A and B are equal.

$$(ii) \quad M = \{x : x \in \mathbb{W} \text{ and } x+3 < 8\}$$

$$x+3 < 8$$

$$\Rightarrow x < 8-3$$

$$\Rightarrow x < 5$$

$$\therefore M = \{0, 1, 2, 3, 4\}$$

$$N = \{y : y = 2n-1, n \in \mathbb{N} \text{ and } n < 5\}$$

$$y = 2n - 1$$

$$\text{When } n = 1, \quad y = 2 \times 1 - 1$$

$$\Rightarrow y = 2 - 1 = 1$$

$$\text{When } n = 2, \quad y = 2 \times 2 - 1$$

$$\Rightarrow y = 4 - 1 = 3$$

$$\text{When } n = 3, \quad y = 2 \times 3 - 1$$

$$\Rightarrow y = 6 - 1 = 5$$

$$\text{When } n = 4, \quad y = 2 \times 4 - 1$$

$$\Rightarrow y = 8 - 1 = 7$$

$$\therefore N = \{1, 3, 5, 7\}$$

Now we see that elements of sets M and N are not the same (identical).

$\therefore$ Sets M and N are **not equal**.

$$(iii) E = \{x : x^2 + 8x - 9 = 0\}$$

$$x^2 + 8x - 9 = 0$$

$$\Rightarrow x^2 + 9x - x - 9 = 0$$

$$\Rightarrow x(x+9) - 1(x+9) = 0$$

$$\Rightarrow (x-1)(x+9) = 0$$

$$\therefore \text{Either } x + 9 = 0 \text{ Or } x - 1 = 0$$

$$\Rightarrow x = -9 \Rightarrow x = 1$$

$$\therefore E = \{-9, 1\}$$

$$F = \{1, -9\}$$

Now we see that the elements of sets E and F are the same (identical)

$\therefore$ Sets E and F are **equal**.

$$(iv) A = \{x : x \in N, x < 3\}$$

$$= \{1, 2\}$$

$$B = \{y : y^2 - 3y + 2 = 0\}$$

$$y^2 - 3y + 2 = 0$$

$$\Rightarrow y^2 - 2y - y + 2 = 0$$

$$\Rightarrow y(y-2) - 1(y-2) = 0$$

$$\Rightarrow (y-2)(y-1) = 0$$

$$\therefore \text{Either } y - 2 = 0 \text{ or } y - 1 = 0$$

$$\Rightarrow y = 2 \Rightarrow y = 1$$

$$\therefore B = \{1, 2\}$$

Now we see that elements of sets A and B are the same (identical).

$\therefore$ Sets A and B are **equal**.

Question 9.

State whether each of the following sets is a finite set or an infinite set:

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- (i) The set of multiples of 8.
- (ii) The set of integers less than 10.
- (iii) The set of whole numbers less than 12.
- (iv) $\{x : x = 3n - 2, n \in W, n \leq 8\}$
- (v) $\{x : x = 3n - 2, n \in Z, n \leq 8\}$
- (vi) $\{x : x = n - 2n + 1, n \in w\}$

Solution:

(i) The set of multiples of 8

$$= \{8, 16, 24, 32, \dots\}$$

It is an infinite set.

(ii) The set of integers less than 10

$$= \{9, 8, 7, 6, 5, 4, 3, 2, 1, -1, -2, \dots\}$$

It is an infinite set.

(iii) The set of whole numbers less than 12

$$= \{11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1, 0\}$$

It is a finite set.

(iv) $\{x : x = 3n - 2, n \in \mathbb{W}, n \leq 8\}$

Substituting the value of $n = (0, 1, 2, 3, 4, 5, 6, 7 \text{ and } 8)$ we get

$$= \{-2, 1, 4, 7, 10, 13, 16, 19, 22\}$$

It is finite set.

(v) $\{x : x = 3n - 2, n \in \mathbb{Z}, n \leq 8\}$

$$= \{22, 19, 16, 13, 10, 7, 4, 1, -2, -5, \dots\}$$

It is infinite set.

(vi) $\{x : x = \frac{n-2}{n+1}, n \in \mathbb{W}\}$

$$\{-2, -\frac{1}{2}, 0, \frac{1}{4}, \frac{2}{5}, \dots\}$$

It is infinite set.

Question 10.

Answer, whether the following statements are true or false. Give reasons.

(i) The set of even natural numbers less than 21 and the set of odd natural numbers less than 21 are equivalent sets.

(ii) If $E = \{\text{factors of } 16\}$ and $F = \{\text{factors of } 20\}$, then $E = F$.

(iii) The set $A = \{\text{integers less than } 20\}$ is a finite set.

(iv) If $A = \{x : x \text{ is an even prime number}\}$, then set A is empty.

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- (v) The set of odd prime numbers is the empty set.
- (vi) The set of squares of integers and the set of whole numbers are equal sets.
- (vii) In $n(P) = n(M)$, then $P \rightarrow M$.
- (viii) If set $P =$ set M , then $n(P) = n(M)$.
- (ix) $n(A) = n(B) \Rightarrow A = B$.

Solution:

(i) Set of even natural number less than 21
= $\{2, 4, 6, 8, 10, 12, 14, 16, 18, 20\}$

$\therefore$ Cardinal Number of this set = 10

Set of odd natural numbers less than 21
= $\{1, 3, 5, 7, 9, 11, 13, 15, 17, 19\}$

$\therefore$ Cardinal number of this set = 10

Now we see that cardinal numbers of both these sets = 10

$\therefore$ "The set of even natural numbers less than 21 and the set of odd natural numbers less than 21 are **equivalent sets**".....is a **True** statement.

Ans.

(ii) $E = \{\text{Factors of } 16\}$ $1 \times 16 = 16$
= $\{1, 2, 4, 8, 16\}$ $2 \times 8 = 16$
 $4 \times 4 = 16$

$F = \{\text{Factors of } 20\}$ $1 \times 20 = 20$
= $\{1, 2, 4, 5, 10, 20\}$ $2 \times 10 = 20$
 $4 \times 5 = 20$

Now we see that elements of set E and set F are not the same (identical)

$\therefore$ "If $E = \{\text{Factors of } 16\}$ and $F = \{\text{Factors of } 20\}$,

then $E = F$ ".....is a **False** statement.

- (iii) $A = \{\text{Integers less than } 20\}$
 $= \{19, 18, 17, 16, \dots, 0, -1, -2, -3, \dots\}$
 $\therefore$ "The set $A = \{\text{Integers less than } 20\}$ is a finite set".....
is a **False** statement.
- (iv) $A = \{x : x \text{ is an even prime number}\} = \{2\}$
 $\therefore$ "If $A = \{x : x \text{ is an even prime number}\}$, then set A is empty"..... is a **false** statement.
- (v) Set of odd prime numbers
 $= \{3, 5, 7, 11, 13, 17, 19, 23, \dots\}$
 $\therefore$ "The set of odd prime numbers is the empty set".....is a **False** statement.
- (vi) **Integer Square of Integer Whole No.**

0	:	$(0)^2 = 0$	0
± 1	:	$(\pm 1)^2 = 1$	1
± 2	:	$(\pm 2)^2 = 4$	2
± 3	:	$(\pm 3)^2 = 9$	3
± 4	:	$(\pm 4)^2 = 16$	4
± 5	:	$(\pm 5)^2 = 25$	5
.....	:		
.....	:		

$\therefore$ Set of squares of integers
 $= \{0, 1, 4, 9, 16, 25, \dots\}$

Set of whole numbers $= \{0, 1, 2, 3, 4, 5, 6, 7, \dots\}$

Hence "The set of squares of integers and the set of whole numbers are equal..." **False statement.**

(vii) $n(P) = n(M)$

It means number of elements of set P

$=$ Number of elements of set M.

$\therefore$ Sets P and M are equivalent.

$\therefore$ "If $n(P) = n(M)$, then $P \leftrightarrow M$ " ... is a **True Statement.**

(viii) Set P = Set M

It means sets P and M are equal. Equal sets are equivalent also.

$\therefore$ Number of elements of set P = Number of elements of set M

$\therefore$ "If set P = set M, then $n(P) = n(M)$ "is a **True statement.**

(ix) $n(A) = n(B)$

$\Rightarrow$ Number of elements of set A

$=$ Number of elements of set B

$\therefore$ Given sets are equivalent but not equal.

$\therefore$ " $n(A) = n(B) \Rightarrow A = B$ "is a **False statement.**

Exercise 6C

Question 1.

Find all the subsets of each of the following sets :

(i) $A = \{5, 7\}$

(ii) $B = \{a, b, c\}$

(iii) $C = \{x : x \in W, x \leq 2\}$

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(iv) $\{p : p \text{ is a letter in the word 'poor'}\}$

Solution:

(i) $A = \{5, 7\}$

Subsets of set $A = \{ \}, \{5\}, \{7\}, \{5, 7\}$

(ii) $B = \{a, b, c\}$

Subsets of set $B = \{ \}, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, \{a, b, c\}$

(iii) $C = \{x : x \in W, x \leq 2\}$
 $= \{0, 1, 2\}$

$\therefore$ Subsets of set $C = \phi, \{0\}, \{1\}, \{2\}, \{0, 1\}, \{0, 2\}, \{1, 2\}, \{0, 1, 2\}$

(iv) $\{P : P \text{ is a letter in the word 'POOR'}\}$
 $= \{p, o, r\}$

$\therefore$ Subsets of the given set $= \phi, \{p\}, \{o\}, \{r\}, \{p, o\}, \{p, r\}, \{o, r\}, \{p, o, r\}$

Question 2.

If C is the set of letters in the word "cooler", find :

(i) Set C

(ii) $n(C)$

(iii) Number of its subsets

(iv) Number of its proper subsets.

Note : (i) If a set has n elements, the number of its subsets $= 2^n$

(ii) If a set has n elements, the number of its proper subsets $= 2^n - 1$

Solution:

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(i) $C = \{c, o, l, e, r\}$

(ii) $n(C) = 5$

(iii) Number of its subsets : $2^5 = 2 \times 2 \times 2 \times 2 \times 2 = 32$

(iv) Number of its proper subsets = $2^5 - 1 = 32 - 1 = 31$

Question 3.

If $T = \{x : x \text{ is a letter in the word 'TEETH'}\}$, find all its subsets.

Solution:

$$T = \{t, e, h\}$$

Subsets of set $T = \phi, \{r\}, \{e\}, \{h\}, \{t, e\}, \{t, h\}, \{e, h\}, \{t, e, h\}$

Question 4.

Given the universal set = $\{-7, -3, -1, 0, 5, 6, 8, 9\}$, find :

(i) $A = \{x : x < 2\}$

(ii) $B = \{x : -4 < x < 6\}$

Solution:

Universal set = $\{-7, -3, -1, 0, 5, 6, 8, 9\}$,

(i) $A = \{x : x < 2\} = \{-7, -3, -1, 0\}$

(ii) $B = \{x : -4 < x < 6\} = \{-3, -1, 0, 5\}$

Question 5.

Given the universal set = $\{x : x \in \mathbb{N} \text{ and } x < 20\}$, find :

(i) $A = \{x : x = 3p ; p \in \mathbb{N}\}$

(ii) $B = \{y : y = 2n + 3, n \in \mathbb{N}\}$

(iii) $C = \{x : x \text{ is divisible by } 4\}$

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Solution:

$$\begin{aligned}\text{Universal set} &= \{x : x \in \mathbb{N} \text{ and } x < 20\} \\ &= \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, \dots, 19\}\end{aligned}$$

$$(i) \quad A = \{x : x = 3p ; p \in \mathbb{N}\}$$
$$x = 3p$$

$$\text{When } p = 1, \quad x = 3 \times 1 = 3$$

$$\text{When } p = 2, \quad x = 3 \times 2 = 6$$

$$\text{When } p = 3, \quad x = 3 \times 3 = 9$$

$$\text{When } p = 4, \quad x = 3 \times 4 = 12$$

$$\text{When } p = 5, \quad x = 3 \times 5 = 15$$

$$\text{When } p = 6, \quad x = 3 \times 6 = 18$$

$$\therefore A = \{3, 6, 9, 12, 15, 18\}$$

$$(ii) \quad B = \{y : y = 2n+3, n \in \mathbb{N}\}$$

$$y = 2n+3$$

Question 6.

Find the proper subsets of $\{x : x^2 - 9x - 10 = 0\}$

Solution:

$$x^2 - 9x - 10 = 0$$

$$\Rightarrow x^2 - 10x + x - 10 = 0$$

$$\Rightarrow x(x-10) + 1(x-10) = 0$$

$$\Rightarrow (x-10)(x+1) = 0$$

$$\therefore \text{ Either } x-10 = 0 \quad \text{ or } \quad x+1 = 0$$

$$x = 10$$

$$\Rightarrow x = -1$$

$$\text{Given set} = \{-1, 10\}$$

$$\text{Proper subsets of this set} = \phi, \{-1\}, \{10\}$$

Question 7.

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Given, $A = \{\text{Triangles}\}$, $B = \{\text{Isosceles triangles}\}$, $C = \{\text{Equilateral triangles}\}$. State whether the following are true or false. Give reasons.

(i) $A \subseteq B$

(ii) $B \subseteq A$

(iii) $C \subseteq B$

(iv) $B \subset A$

(v) $C \subset A$

(vi) $C \subseteq B \subseteq A$

Solution:

$$A = \{\text{Triangles}\}$$

$$B = \{\text{Isosceles triangles}\}$$

$$C = \{\text{Equilateral triangles}\}$$

(i) Since each triangle is not isosceles.

$\therefore A \subset B$ **False**

(ii) $B \subseteq A$ **True**

$\because$ Isosceles Δ is one of the triangles.

(iii) Since each equilateral triangle is isosceles also,

$\therefore C \subseteq B$ **True**

(iv) $B \subset A$ **True**

$\because$ isosceles Δ is one of the triangles.

(v) $C \subset A$ **True**

$\because$ Equilateral Δ is one of the triangles.

(vi) $C \subseteq B \subseteq A$ **True**

$\because$ Each equilateral triangle is isosceles also and each isosceles Δ is a form of triangles.

Question 8.

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Given, $A = \{\text{Quadrilaterals}\}$, $B = \{\text{Rectangles}\}$, $C = \{\text{Squares}\}$, $D = \{\text{Rhombuses}\}$. State, giving reasons, whether the following are true or false.

(i) $B \subset C$

(ii) $D \subset B$

(iii) $C \subseteq B \subseteq A$

(iv) $D \subset A$

(v) $B \supseteq C$

(vi) $A \supseteq B \supseteq D$

Solution:

$$A = \{\text{Quadrilaterals}\}$$

$$B = \{\text{Rectangles}\}$$

$$C = \{\text{Square}\}$$

$$D = \{\text{Rhombuses}\}$$

(i) $B \subset C$ is a **False**.

$\because$ Rectangle is not a square also.

(ii) $D \subset B$ is a **False**.

$\because$ Rhombus is not a rectangle also.

(iii) $C \subseteq B \subseteq A$ **True**

$\because$ Every square is a rectangle also and every rectangle is a quadrilateral also

(iv) $D \subset A$ **True**

$\because$ Rhombus is one of the quadrilaterals.

(v) $B \supseteq C$ **True**

$\because$ Square is a rectangle also.

(vi) $A \supseteq B \supseteq D$ **False**

$\because$ Rhombus is not a rectangle also.

Question 9.

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Given, universal set = $\{x : x \in \mathbb{N}, 10 \leq x \leq 35\}$.

A = $\{x \in \mathbb{N} : x \leq 16\}$ and

B = $\{x : x > 29\}$ Find :

(i) A' (ii) B' .

Solution:

Universal set = $\{x : x \in \mathbb{N}, 10 \leq x \leq 35\}$

= $\{10, 11, 12, 13, 14, 15, \dots, 34, 35\}$

A = $\{x \in \mathbb{N}, x \leq 16\}$

= $\{10, 11, 12, 13, 14, 15, 16\}$

B = $\{x : x > 29\}$

= $\{30, 31, 32, 33, 34, 35\}$

(i) $A' = \{17, 18, 19, 20, 21, 22, \dots, 33, 34, 35\}$

= $\{x : x \in \mathbb{N} ; 17 \leq x \leq 35\}$

(ii) $B' = \{10, 11, 12, 13, 14, 15, \dots, 29\}$

= $\{x : x \leq 29\}$

Question 10.

Given universal set = $\{x \in \mathbb{Z} : -6 < x \leq 6\}$, $N = \{n : n \text{ is a non-negative number}\}$
and

P = $\{x : x \text{ is a non-positive number}\}$

Find : (i) N' (ii) P'

Solution:

$$\text{Universal set} = \{x \in \mathbb{Z}; -6 < x \leq 6\}$$

$$= \{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6\}$$

$$N = \{n : n \text{ is a non-negative number}\}$$

$$= \{0, 1, 2, 3, 4, 5, 6\}$$

$$P = \{x : x \text{ is a non-positive number}\}$$

$$= \{-5, -4, -3, -2, -1, 0\}$$

$$(i) \quad N' = \{-5, -4, -3, -2, -1\}$$

$$(ii) \quad P' = \{1, 2, 3, 4, 5, 6\}$$

Question 11.

Let $M = \{\text{letters of the word REAL}\}$
and $N = \{\text{letters of the word LARE}\}$. Write sets M and N in roster form and then state whether;

(i) $M \subseteq N$ is true. (ii) $N \subseteq M$ is true.

(iii) $M = N$ is true.

Solution:

$$M = \{\text{letters of the word REAL}\}$$

$$= \{R, E, A, L\}$$

$$\text{and } N = \{\text{letters of the word LARE}\}$$

$$= \{L, A, R, E\}$$

(i) $M \subseteq N$ is true : Yes

(ii) $N \subseteq M$ is true : Yes

(iii) $M = N$ is true : Yes

Q. No. 12. Write two sets A and B such that $A \subseteq B$ and $B \subseteq A$. State the relationship between sets A and B .

Sol. Let $A = \{\text{Letters of TALE}\}$

$$B = \{\text{Letters of LATE}\}$$

Here $A \subseteq B$, and $B \subseteq A$

$$\therefore A = B$$

Question 12.

<https://www.indcareer.com/schools/selina-class-8-icse-solutions-mathematics-chapter-6-sets/>

Write two sets A and B such that $A \subseteq B$ and $B \subseteq A$. State the relationship between sets A and B.

Solution:

Let $A = \{\text{Letters of TALE}\}$

$B = \{\text{Letters of LATE}\}$

Here $A \subseteq B$, and $B \subseteq A$

$\therefore A = B$

Exercise 6D

Question 1.

Given $A = \{x : x \in \mathbb{N} \text{ and } 3 < x \leq 6\}$ and $B = \{x : x \in \mathbb{W} \text{ and } x < 4\}$. Find :

(i) Sets A and B in roster form

(ii) $A \cup B$ (iii) $A \cap B$.

(iv) $A - B$ (v) $B - A$

Solution:

(i) $A = \{4, 5, 6\}$

$B = \{0, 1, 2, 3\}$

(ii) $A \cup B = \{0, 1, 2, 3, 4, 5, 6\}$

(iii) $A \cap B = \{\phi\}$

(iv) $A - B = \{4, 5, 6\}$

(v) $B - A = \{0, 1, 2, 3\}$

Question 2.

If $P = \{x : x \in W \text{ and } 4 \leq x \leq 8\}$,
and $Q = \{x : x \in N \text{ and } x < 6\}$. Find :

- (i) $P \cup Q$ and $P \cap Q$.
- (ii) Is $(P \cup Q) \supset (P \cap Q)$?

Solution:

- (i) $P = (4, 5, 6, 7, 8)$
 $Q = (1, 2, 3, 4, 5)$
 $P \cup Q = (1, 2, 3, 4, 5, 6, 7, 8)$
 $P \cap Q = (4, 5)$
- (ii) Yes, all the element of set $P \cup Q$ are contained in the set $P \cap Q$. Therefore $P \cup Q$ is a proper subset of $P \cap Q$.

Question 3.

If $A = \{5, 6, 7, 8, 9\}$, $B = \{x : 3 < x < 8 \text{ and } x \in W\}$ and $C = \{x : x \leq 5 \text{ and } x \in N\}$. Find :

- (i) $A \cup B$ and $(A \cup B) \cup C$
 - (ii) $B \cup C$ and $A \cup (B \cup C)$
 - (iii) $A \cap B$ and $(A \cap B) \cap C$
 - (iv) $B \cap C$ and $A \cap (B \cap C)$
- Is $(A \cup B) \cup C = A \cup (B \cup C)$?
- Is $(A \cap B) \cap C = A \cap (B \cap C)$?

Solution:

$$A = (5, 6, 7, 8, 9)$$

$$B = (4, 5, 6, 7)$$

$$C = (1, 2, 3, 4, 5)$$

$$(i) A \cup B = (4, 5, 6, 7, 8, 9)$$

$$(A \cup B) \cup C = (1, 2, 3, 4, 5, 6, 7, 8, 9)$$

$$(ii) B \cup C = (1, 2, 3, 4, 5, 6, 7)$$

$$A \cup (B \cup C) = (1, 2, 3, 4, 5, 6, 7, 8, 9)$$

$$(iii) A \cap B = (5, 6, 7)$$

$$(A \cap B) \cap C = (5)$$

$$(iv) B \cap C = (4, 5)$$

$$A \cap (B \cap C) = (5)$$

$$(v) (A \cup B) \cup C = (1, 2, 3, 4, 5, 6, 7, 8, 9)$$

$$A \cup (B \cup C) = (1, 2, 3, 4, 5, 6, 7, 8, 9)$$

Yes, these are equal.

$$(vi) (A \cap B) \cap C = A \cap (B \cap C)$$

$$\{5\} = \{5\}$$

Yes, these are equal.

Question 4.

$$\text{Given } A = \{0, 1, 2, 4, 5\},$$

$$B = \{0, 2, 4, 6, 8\} \text{ and } C = \{0, 3, 6, 9\}. \text{ Show that}$$

$$(i) A \cup (B \cup C) = (A \cup B) \cup C \text{ i.e. the union of sets is associative.}$$

$$(ii) A \cap (B \cap C) = (A \cap B) \cap C \text{ i.e. the intersection of sets is associative.}$$

Solution:

$$A = \{0,1,2,4,5\}$$

$$B = \{0,2,4,6,8\}$$

$$C = \{0,3,6,9\}$$

$$\begin{aligned}(i) \quad B \cup C &= \{0,2,4,6,8\} \cup \{0,3,6,9\} \\ &= \{0,2,3,4,6,8,9\}\end{aligned}$$

$$\begin{aligned}\therefore A \cup (B \cup C) \\ &= \{0,1,2,4,5\} \cup \{0,2,3,4,6,8,9\}\end{aligned}$$

$$\begin{aligned}\Rightarrow A \cup (B \cup C) \\ &= \{0,1,2,3,4,5,6,8,9\} \quad \dots I \\ A \cup B &= \{0,1,2,4,5\} \cup \{0,2,4,6,8\} \\ &= \{0,1,2,4,5,6,8\}\end{aligned}$$

$$\begin{aligned}\therefore (A \cup B) \cup C \\ &= \{0,1,2,4,5,6,8\} \cup \{0,3,6,9\}\end{aligned}$$

$$\Rightarrow (A \cup B) \cup C = \{0,1,2,3,4,5,6,8,9\} \quad \dots II$$

From I and II, we get

$$A \cup (B \cup C) = (A \cup B) \cup C$$

$$\begin{aligned}(ii) \quad B \cap C &= \{0,2,4,6,8\} \cap \{0,3,6,9\} \\ &= \{0,6\}\end{aligned}$$

$$\text{Now, } A \cap (B \cap C) = \{0,1,2,4,5\} \cap \{0,6\}$$

$$\Rightarrow A \cap (B \cap C) = \{0\} \quad \dots I$$

$$\begin{aligned}A \cap B &= \{0,1,2,4,5\} \cap \{0,2,4,6,8\} \\ &= \{0,2,4\}\end{aligned}$$

$$\therefore (A \cap B) \cap C = \{0,2,4\} \cap \{0,3,6,9\}$$

$$\Rightarrow (A \cap B) \cap C = \{0\} \quad \dots II$$

From I and II we get

$$A \cap (B \cap C) = (A \cap B) \cap C$$

Question 5.

If $A = \{x \in W : 5 < x < 10\}$, $B = \{3, 4, 5, 6, 7\}$ and $C = \{x = 2n; n \in N \text{ and } n \leq 4\}$. Find :

- (i) $A \cap (B \cup C)$
- (ii) $(B \cup A) \cap (B \cup C)$
- (iii) $B \cup (A \cap C)$
- (iv) $(A \cap B) \cup (A \cap C)$

Name the sets which are equal.

Solution:

$$\begin{aligned}A &= \{x \in W : 5 < x < 10\} \\ &= \{6, 7, 8, 9\}\end{aligned}$$

$$B = \{3, 4, 5, 6, 7\}$$

$$C = \{x = 2n : n \in N \text{ and } n \leq 4\}$$

$$x = 2n$$

$$\text{When } n=1, \quad x = 2 \times 1 = 2$$

$$\text{When } n=2, \quad x = 2 \times 2 = 4$$

$$\text{When } n=3, \quad x = 2 \times 3 = 6$$

$$\text{When } n=4, \quad x = 2 \times 4 = 8$$

$$\therefore C = \{2, 4, 6, 8\}$$

$$\begin{aligned}(i) \quad B \cup C &= \{3, 4, 5, 6, 7\} \cup \{2, 4, 6, 8\} \\ &= \{2, 3, 4, 5, 6, 7, 8\}\end{aligned}$$

$$A \cap (B \cup C) = \{6, 7, 8, 9\} \cap \{2, 3, 4, 5, 6, 7, 8\}$$

$$\Rightarrow A \cap (B \cup C) = \{6, 7, 8\} \text{ Ans.}$$

$$\begin{aligned}(ii) \quad B \cup A &= \{3, 4, 5, 6, 7\} \cup \{6, 7, 8, 9\} \\ &= \{3, 4, 5, 6, 7, 8, 9\}\end{aligned}$$

$$(B \cup A) \cap (B \cup C)$$

$$= \{3, 4, 5, 6, 7, 8, 9\} \cap \{2, 3, 4, 5, 6, 7, 8\}$$

$$= \{3, 4, 5, 6, 7, 8\}$$

$$\begin{aligned}(iii) \quad (A \cap C) &= \{6, 7, 8, 9\} \cap \{2, 4, 6, 8\} \\ &= \{6, 8\}\end{aligned}$$

$$\begin{aligned}B \cup (A \cap C) &= \{3, 4, 5, 6, 7\} \cup \{6, 8\} \\ &= \{3, 4, 5, 6, 7, 8\}\end{aligned}$$

$$\begin{aligned}(iv) \quad (A \cap B) &= \{6, 7, 8, 9\} \cap \{3, 4, 5, 6, 7\} \\ &= \{6, 7\}\end{aligned}$$

$$\begin{aligned}\therefore (A \cap B) \cup (A \cap C) &= \{6, 7\} \cup \{6, 8\} \\ &= \{6, 7, 8\}\end{aligned}$$

Question 6.

<https://www.indcareer.com/schools/selina-class-8-icse-solutions-mathematics-chapter-6-sets/>

If $P = \{\text{factors of } 36\}$ and $Q = \{\text{factors of } 48\}$; find :

(i) $P \cup Q$

(ii) $P \cap Q$

(iii) $Q - P$

(iv) $P' \cap Q$.

Solution:

$$1 \times 36 = 36$$

$$1 \times 48 = 48$$

$$2 \times 18 = 36$$

$$2 \times 24 = 48$$

$$3 \times 12 = 36$$

$$3 \times 16 = 48$$

$$4 \times 9 = 36$$

$$4 \times 12 = 48$$

$$6 \times 6 = 36$$

$$6 \times 8 = 48$$

$$\therefore \text{Factors of } 36 = 1, 2, 3, 4, 6, 9, 12, 18, 36$$

$$\text{Factors of } 48 = 1, 2, 3, 4, 6, 8, 12, 16, 24, 48$$

$$P = \{\text{factors of } 36\}$$

$$= \{1, 2, 3, 4, 6, 9, 12, 18, 36\}$$

$$Q = \{\text{Factors of } 48\}$$

$$= \{1, 2, 3, 4, 6, 8, 12, 16, 24, 48\}$$

$$\begin{aligned} \text{(i)} \quad P \cup Q &= \{1, 2, 3, 4, 6, 9, 12, 18, 36\} \\ &\cup \{1, 2, 3, 4, 6, 8, 12, 16, 24, 48\} \\ &= \{1, 2, 3, 4, 6, 8, 9, 12, 16, 18, 24, 36, 48\} \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad P \cap Q &= \{1, 2, 3, 4, 6, 9, 12, 18, 36\} \\ &\cap \{1, 2, 3, 4, 6, 8, 12, 16, 24, 48\} \\ &= \{1, 2, 3, 4, 6, 12\} \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad Q - P &= \{1, 2, 3, 4, 6, 8, 12, 16, 24, 48\} \\ &- \{1, 2, 3, 4, 6, 9, 12, 18, 36\} \\ &= \{8, 16, 24, 48\} \end{aligned}$$

$$\begin{aligned} (iv) \quad P' \cap Q &= \text{Only } Q \\ &= Q - P \\ &= \{1, 2, 3, 4, 6, 8, 12, 16, 24, 48\} \\ &\quad - \{1, 2, 3, 4, 6, 9, 12, 18, 36\} \\ &= \{8, 16, 24, 48\} \end{aligned}$$

Question 7.

If $A = \{6, 7, 8, 9\}$, $B = \{4, 6, 8, 10\}$ and $C = \{x : x \in \mathbb{N} : 2 < x \leq 7\}$; find

- | | |
|----------------------|-----------------------|
| (i) $A - B$ | (ii) $B - C$ |
| (iii) $B - (A - C)$ | (iv) $A - (B \cup C)$ |
| (v) $B - (A \cap C)$ | (vi) $B - B$ |

Solution:

$$A = \{6, 7, 8, 9\}$$

$$B = \{4, 6, 8, 10\}$$

$$C = \{x : x \in \mathbb{N} : 2 < x \leq 7\}$$
$$= \{3, 4, 5, 6, 7\}$$

$$(i) \quad A - B = \{6, 7, 8, 9\} - \{4, 6, 8, 10\}$$
$$= \{7, 9\}$$

$$(ii) \quad B - C = \{4, 6, 8, 10\} - \{3, 4, 5, 6, 7\}$$
$$= \{8, 10\}$$

$$(iii) \quad A - C = \{6, 7, 8, 9\} - \{3, 4, 5, 6, 7\}$$
$$= \{8, 9\}$$

$$B - (A - C) = \{4, 6, 8, 10\} - \{8, 9\}$$
$$= \{4, 6, 10\}$$

$$(iv) \quad B \cup C = \{4, 6, 8, 10\} \cup \{3, 4, 5, 6, 7\}$$
$$= \{3, 4, 5, 6, 7, 8, 10\}$$

$$A - (B \cup C) = \{6, 7, 8, 9\} - \{3, 4, 5, 6, 7, 8, 10\}$$
$$= \{9\}$$

$$(v) \quad A \cap C = \{6, 7, 8, 9\} \cap \{3, 4, 5, 6, 7\}$$
$$= \{6, 7\}$$

$$B - (A \cap C) = \{4, 6, 8, 10\} - \{6, 7\}$$
$$= \{4, 8, 10\}$$

$$(vi) \quad B - B = \{4, 6, 8, 10\} - \{4, 6, 8, 10\}$$
$$= \phi$$

Question 8.

$$\text{If } A = \{1, 2, 3, 4, 5\}$$

$$B = \{2, 4, 6, 8\}$$

$$\text{and } C = \{3, 4, 5, 6\}$$

Verify :

$$(i) \quad A - (B \cup C) = (A - B) \cap (A - C)$$

$$(ii) \quad A - (B \cap C) = (A - B) \cup (A - C)$$

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Solution:

$$A = \{1, 2, 3, 4, 5\}$$

$$B = \{2, 4, 6, 8\}$$

$$C = \{3, 4, 5, 6\}$$

$$\begin{aligned}(i) \quad B \cup C &= \{2, 4, 6, 8\} \cup \{3, 4, 5, 6\} \\ &= \{2, 3, 4, 5, 6, 8\}\end{aligned}$$

$$\begin{aligned}A - (B \cup C) &= \{1, 2, 3, 4, 5\} - \{2, 3, 4, 5, 6, 8\} \\ &= \{1\}\end{aligned}$$

$$\begin{aligned}A - B &= \{1, 2, 3, 4, 5\} - \{2, 4, 6, 8\} \\ &= \{1, 3, 5\}\end{aligned}$$

$$\begin{aligned}A - C &= \{1, 2, 3, 4, 5\} - \{3, 4, 5, 6\} \\ &= \{1, 2\}\end{aligned}$$

$$\therefore (A - B) \cap (A - C) = \{1, 3, 5\} \cap \{1, 2\} = \{1\}$$

$$\therefore A - (B \cup C) = (A - B) \cap (A - C)$$

$$\begin{aligned}(ii) \quad B \cap C &= \{2, 4, 6, 8\} \cap \{3, 4, 5, 6\} \\ &= \{4, 6\}\end{aligned}$$

$$\begin{aligned}A - (B \cap C) &= \{1, 2, 3, 4, 5\} - \{4, 6\} \\ &= \{1, 2, 3, 5\}\end{aligned}$$

$$\begin{aligned}A - B &= \{1, 2, 3, 4, 5\} - \{2, 4, 6, 8\} \\ &= \{1, 3, 5\}\end{aligned}$$

$$\begin{aligned}A - C &= \{1, 2, 3, 4, 5\} - \{3, 4, 5, 6\} \\ &= \{1, 2\}\end{aligned}$$

$$\begin{aligned}(A - B) \cup (A - C) &= \{1, 3, 5\} \cup \{1, 2\} \\ &= \{1, 2, 3, 5\}\end{aligned}$$

$$\therefore A - (B \cap C) = (A - B) \cup (A - C)$$

Question 9.

Given $A = \{x \in \mathbb{N} : x < 6\}$, $B = \{3, 6, 9\}$
and $C = \{x \in \mathbb{N} : 2x - 5 \leq 8\}$. Show that :

$$(i) \quad A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

$$(ii) \quad A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$

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Solution:

$$A = \{x \in \mathbb{N} : x < 6\}$$

$$= \{1, 2, 3, 4, 5\}$$

$$B = \{3, 6, 9\}$$

$$C = \{x \in \mathbb{N} : 2x - 5 \leq 8\}$$

$$2x - 5 \leq 8$$

$$\Rightarrow 2x \leq 8 + 5$$

$$\Rightarrow 2x \leq 13$$

$$\Rightarrow x \leq \frac{13}{2}$$

$$\Rightarrow x \leq 6.5$$

$$\therefore C = \{1, 2, 3, 4, 5, 6\}$$

$$(i) B \cap C = \{3, 6, 9\} \cap \{1, 2, 3, 4, 5, 6\}$$
$$= \{3, 6\}$$

$$\therefore A \cup (B \cap C) = \{1, 2, 3, 4, 5\} \cup \{3, 6\}$$
$$= \{1, 2, 3, 4, 5, 6\}$$

$$A \cup B = \{1, 2, 3, 4, 5\} \cup \{3, 6, 9\}$$
$$= \{1, 2, 3, 4, 5, 6, 9\}$$

$$A \cup C = \{1, 2, 3, 4, 5\} \cup \{1, 2, 3, 4, 5, 6\}$$
$$= \{1, 2, 3, 4, 5, 6\}$$

$$\therefore (A \cup B) \cap (A \cup C)$$
$$= \{1, 2, 3, 4, 5, 6, 9\} \cap \{1, 2, 3, 4, 5, 6\}$$
$$= \{1, 2, 3, 4, 5, 6\}$$

$$\therefore A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

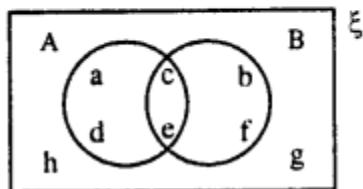
$$\begin{aligned}
 (ii) \quad B \cup C &= \{3,6,9\} \cup \{1,2,3,4,5,6\} \\
 &= \{1,2,3,4,5,6,9\} \\
 A \cap (B \cup C) &= \{1,2,3,4,5\} \cap \{1,2,3,4,5,6,9\} \\
 &= \{1,2,3,4,5\} \\
 \text{Now } A \cap C &= \{1,2,3,4,5\} \cap \{1,2,3,4,5,6\} \\
 &= \{1,2,3,4,5\} \\
 A \cap B &= \{1,2,3,4,5\} \cap \{3,6,9\} \\
 &= \{3\} \\
 \therefore (A \cap B) \cup (A \cap C) &= \{3\} \cup \{1,2,3,4,5\} \\
 &= \{1,2,3,4,5\} \\
 \therefore A \cap (B \cup C) &= (A \cap B) \cup (A \cap C)
 \end{aligned}$$

Exercise 6E

Question 1.

From the given diagram find :

- | | |
|-------------------|------------------|
| (i) $A \cup B$ | (ii) $A' \cap B$ |
| (iii) $A - B$ | (iv) $B - A$ |
| (v) $(A \cup B)'$ | |



Solution:

$$\begin{aligned}
 (i) \quad A \cup B &= \{a, c, d, e\} \cup \{b, c, e, f\} \\
 \Rightarrow A \cup B &= \{a, b, c, d, e, f\} \\
 (ii) \quad A' &= \{b, f, g, h\} \\
 A' \cap B &= \{b, f, g, h\} \cap \{b, c, e, f\} \\
 \Rightarrow A' \cap B &= \{b, f\} \\
 (iii) \quad A - B &= \{a, c, d, e\} - \{b, c, e, f\} \\
 \Rightarrow A - B &= \{a, d\} \\
 (iv) \quad B - A &= \{b, c, e, f\} - \{a, c, d, e\} \\
 &= \{b, f\} \\
 (v) \quad A \cup B &= \{a, b, c, d, e, f\} \\
 \therefore (A \cup B)' &= \{g, h\}
 \end{aligned}$$

Question 2.

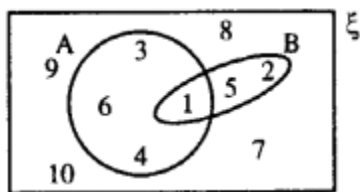
From the given diagram, find :

(i) A'

(ii) B'

(iii) $A' \cup B'$

(iv) $(A \cap B)'$



Is $A' \cup B' = (A \cap B)'$?

Also, verify if $A' \cap B' = (A \cup B)'$.

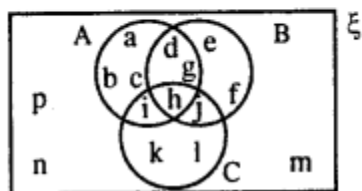
Solution:

$$\begin{aligned}
 (i) \quad A &= \{1, 3, 4, 6\} \\
 \therefore A' &= \{2, 5, 7, 8, 9, 10\} \\
 (ii) \quad B &= \{1, 2, 5\} \\
 \therefore B' &= \{3, 4, 6, 7, 8, 9, 10\} \\
 (iii) \quad A' \cup B' &= \{2, 5, 7, 8, 9, 10\} \cup \{3, 4, 6, 7, 8, 9, 10\} \\
 &= \{2, 3, 4, 5, 6, 7, 8, 9, 10\} \\
 (iv) \quad A \cap B &= \{1, 3, 4, 6\} \cap \{1, 2, 5\} \\
 &= \{1\} \\
 \therefore (A \cap B)' &= \{2, 3, 4, 5, 6, 7, 8, 9, 10\} \\
 \text{From Part (iii) and Part (iv) we conclude} \\
 A' \cup B' &= (A \cap B)' \\
 \text{Now } A \cap B &= \{2, 5, 7, 8, 9, 10\} \cap \{3, 4, 6, 7, 8, 9, 10\} \\
 \Rightarrow A' \cap B' &= \{7, 8, 9, 10\} \quad \dots I \\
 \text{Now } A \cup B &= \{1, 3, 4, 6\} \cup \{1, 2, 5\} \\
 &= \{1, 2, 3, 4, 5, 6\} \\
 \therefore (A \cup B)' &= \{7, 8, 9, 10\} \quad \dots II \\
 \text{From I and II we conclude} \\
 A' \cap B' &= (A \cup B)'
 \end{aligned}$$

Question 3.

Use the given diagram to find :

- (i) $A \cup (B \cap C)$
(ii) $B - (A - C)$
(iii) $A - B$ (iv) $A \cap B'$
Is $A \cap B' = A - B$?



Solution:

$$(i) B \cap C = \{d, e, f, g, h, j\} \cap \{h, i, j, k, l\} \\ = \{h, j\}$$

$$\therefore A \cup (B \cap C) = \{a, b, c, d, g, h, i\} \cup \{h, j\} \\ = \{a, b, c, d, g, h, i, j\}$$

$$(ii) A - C = \{a, b, c, d, g, h, i\} - \{h, i, j, k, l\} \\ = \{a, b, c, d, g\}$$

$$\therefore B - (A - C) = \{d, e, f, g, h, j\} - \{a, b, c, d, g\} \\ = \{e, f, h, j\}$$

$$(iii) A - B = \{a, b, c, d, g, h, i\} \\ - \{d, e, f, g, h, i\}$$

$$\Rightarrow A - B = \{a, b, c, i\}$$

$$(iv) B' = \{a, b, c, i, k, l, m, n, p\}$$

$$A \cap B' = \{a, b, c, d, g, h, i\} \\ \cap \{a, b, c, i, k, l, m, n, p\}$$

$$\Rightarrow A \cap B' = \{a, b, c, i\} \quad \dots II$$

From I and II we can conclude $A \cap B' = A - B$

Question 4.

Use the given Venn-diagram to find :

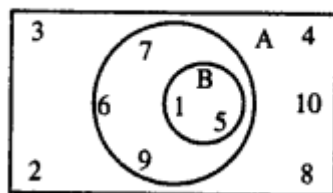
$$(i) B - A$$

$$(ii) A$$

$$(iii) B'$$

$$(iv) A \cap B$$

$$(v) A \cup B$$



Solution:

- (i) $B - A = \{1, 5\} - \{1, 5, 6, 7, 9\}$
 $= \{ \}$
- (ii) $A = \{1, 5, 6, 7, 9\}$
- (iii) $B = \{1, 5\}$
- $\therefore B' = \{2, 3, 4, 6, 7, 8, 9, 10\}$
- (iv) $A \cap B = \{1, 5, 6, 7, 9\} \cap \{1, 5\}$
 $= \{1, 5\}$
- (v) $A \cup B = \{1, 5, 6, 7, 9\} \cup \{1, 5\}$
 $= \{1, 5, 6, 7, 9\}$

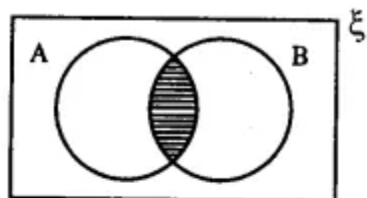
Question 5.

Draw a Venn-diagram to show the relationship between two overlapping sets A and B. Now shade the region representing :

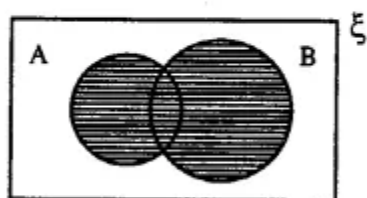
- (i) $A \cap B$ (ii) $A \cup B$
- (iii) $B - A$

Solution:

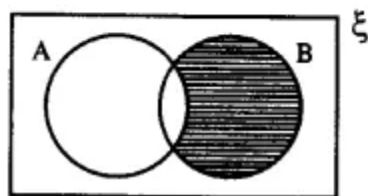
(i) $A \cap B =$



(ii) $A \cup B =$



(iii) $B - A =$



Question 6.

Draw a Venn-diagram to show the relationship between two sets A and B ; such that $A \subseteq B$, Now shade the region representing :

(i) $A \cup B$

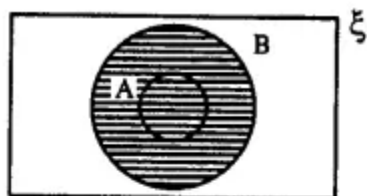
(ii) $B' \cap A$

(iii) $A \cap B$

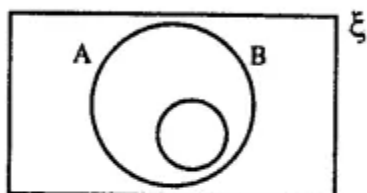
(iv) $(A \cup B)'$

Solution:

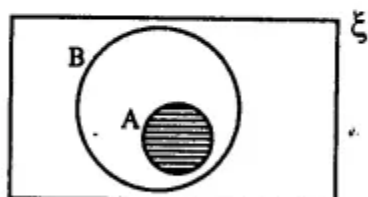
(i) $A \cup B =$



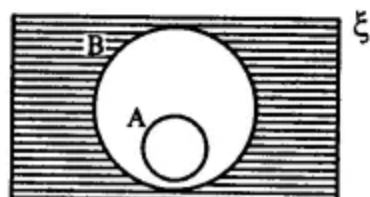
(ii) $B' \cap A =$



(iii) $A \cap B =$



(iv) $(A \cup B)' =$



Question 7.

Two sets A and B are such that $A \cap B = \phi$. Draw a venn-diagram to show the relationship between A and B. Shade the region representing :

(i) $A \cup B$

(ii) $(A \cup B)'$

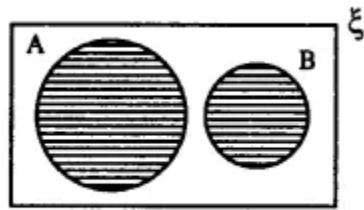
(iii) $B - A$

(iv) $B \cap A'$

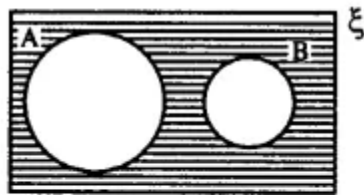
<https://www.indcareer.com/schools/selina-class-8-icse-solutions-mathematics-chapter-6-sets/>

Solution:

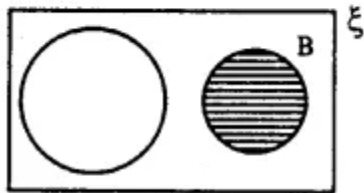
(i) $A \cup B =$



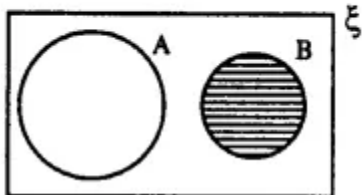
(ii) $(A \cup B)' =$



(iii) $B - A =$



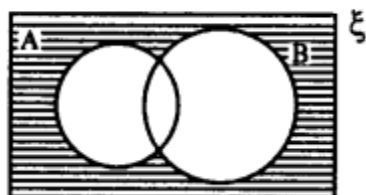
(iv) $B \cap A' =$



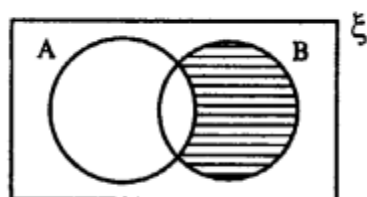
Question 8.

State the sets represented by the shaded portion of following venn-diagrams :

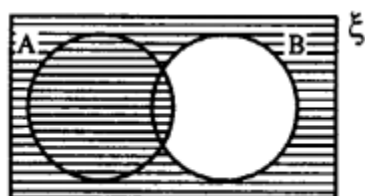
(i)



(ii)



(iii)



Solution:

(i) $(A \cup B)'$

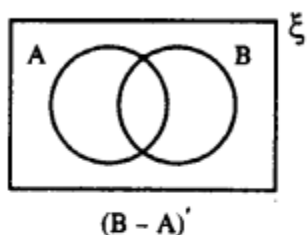
(ii) $B - A$ or $A' \cap B$

(iii) $(B - A)'$

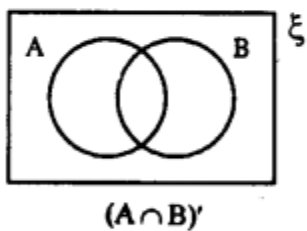
Question 9.

In each of the given diagrams, shade the region which represents the set given underneath the diagram :

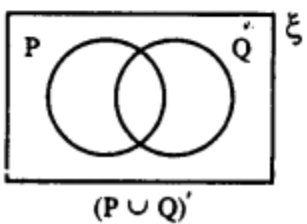
(i)



(ii)

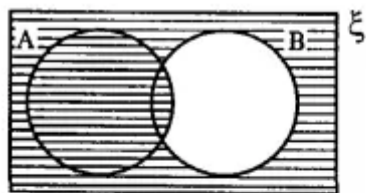


(iii)

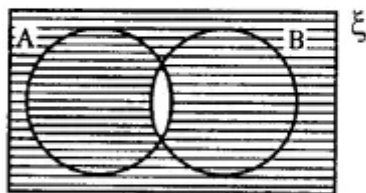


Solution:

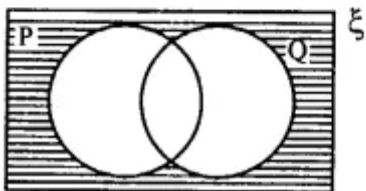
(i) $(B - A) =$



(ii) $(A \cap B)' =$



(iii) $(P \cup Q)' =$



Question 10.

From the given diagram, find :

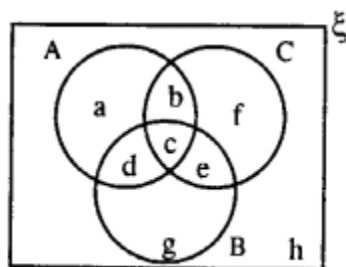
(i) $(A \cup B) - C$

(ii) $B - (A \cap C)$

(iii) $(B \cap C) \cup A$

Verify :

$$A - (B \cap C) = (A - B) \cup (A - C)$$



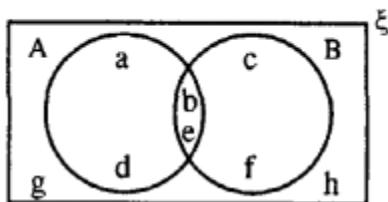
Solution:

$$\begin{aligned}
 (i) \quad A \cup B &= \{a, b, c, d\} \cup \{c, d, e, g\} \\
 &= \{a, b, c, d, e, g\} \\
 \therefore (A \cup B) - C &= \{a, b, c, d, e, g\} - \{b, c, e, f\} \\
 &= \{a, d, g\} \\
 (ii) \quad A \cap C &= \{a, b, c, d\} \cap \{b, c, e, f\} \\
 &= \{b, c\} \\
 \therefore B - (A \cap C) &= \{c, d, e, g\} - \{b, c\} \\
 &= \{d, e, g\} \\
 (iii) \quad B \cap C &= \{c, e, d, g\} \cap \{b, c, e, f\} \\
 &= \{c, e\}
 \end{aligned}$$

Question 11.

Using the given diagram, express the following sets in the terms of A and B.

- (i) $\{a, d\}$
- (ii) $\{a, d, c, f\}$
- (iii) $\{a, d, c, f, g, h\}$
- (iv) $\{a, d, g, h\}$
- (v) $\{g, h\}$



Solution:

$$(i) \quad \{a, d\} = \{a, b, e, d\} - \{b, c, e, f\} \\ = A - B$$

$$(ii) \quad \{a, d, c, f\} = (A \cup B) - \{b, e\} \\ = (A \cup B) - (A \cap B)$$

$$\text{Also } \{a, d, c, f\} = (A - B) \cup (B - A)$$

$$(iii) \quad \{a, d, c, f, g, h\} = (A \cap B)'$$

$$[\because \{b, e\} = A \cap B \therefore (A \cap B)' = \{a, d, c, f, g, h\}]$$

$$(iv) \quad \{a, d, g, h\} = B'$$

$$[\because \{b, c, e, f\} = B \therefore B' = \{a, d, g, h\}]$$

$$(v) \quad \{g, h\} = (A \cup B)'$$

$$[\because A \cup B = \{a, b, c, d, e, f\} \therefore (A \cup B)' = \{g, h\}]$$



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